

**CS 563 Advanced Topics in  
Computer Graphics**  
*Irradiance Caching and Particle Tracing*

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- Unbiased light transport algorithms can sometimes take a large number of rays to generate an image without noise
- To counter this, biased algorithms such as irradiance caching and photon mapping have been developed
  - Reuse previously computed results
  - Produce images without high-frequency noise artifacts
  - Produce good images using less additional computing power
  - Hard to do error estimation, however



## Irradiance Caching

- Based on the notion that while direct lighting changes drastically from point to point, indirect lighting does not
- Compute indirect lighting at a sparse set of sample points and interpolate the rest

# Indirect Illumination





- 1) When are new representations of indirect light computed, and how often are already existing ones interpolated?
- 2) How is the indirect lighting distribution represented and stored after being computed at a point?



## Computing Points

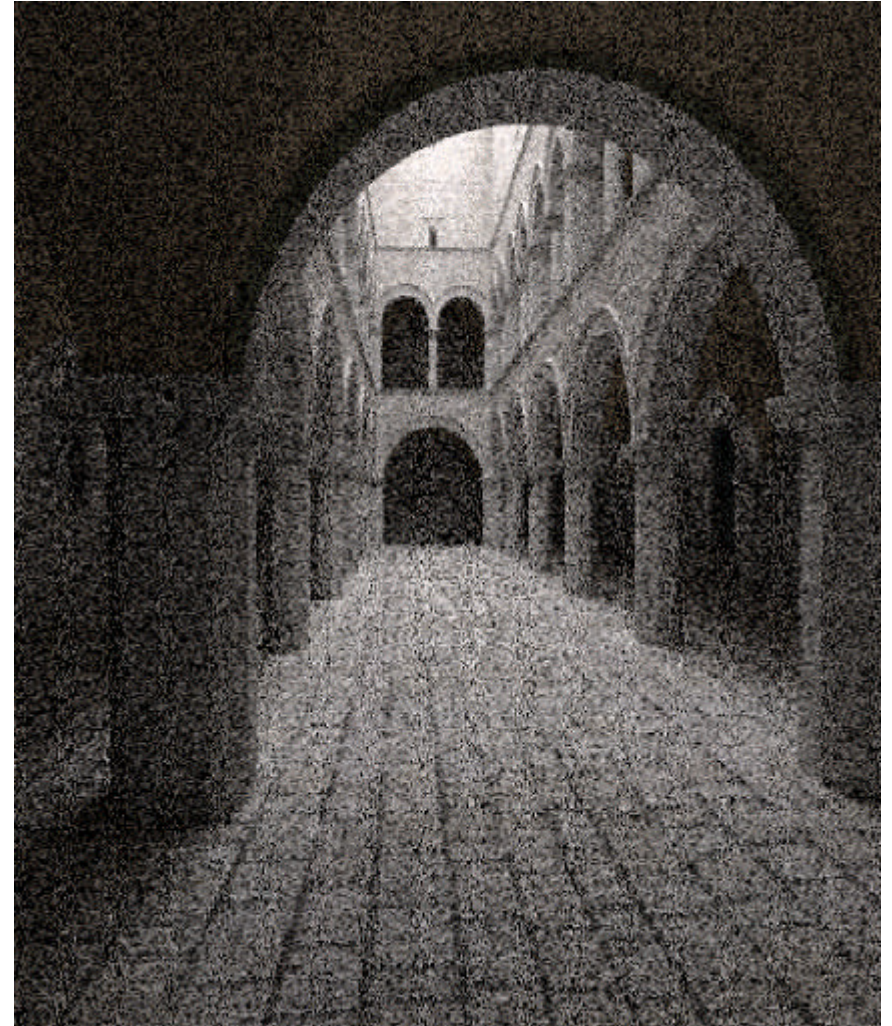
- Indirect lighting computed on-the-fly (as opposed to on a fixed set of points chosen ahead of time)
- First cache is searched for an acceptable point using a set of error metrics
- If a point cannot be found in the cache, a new point is created



## Storing Information

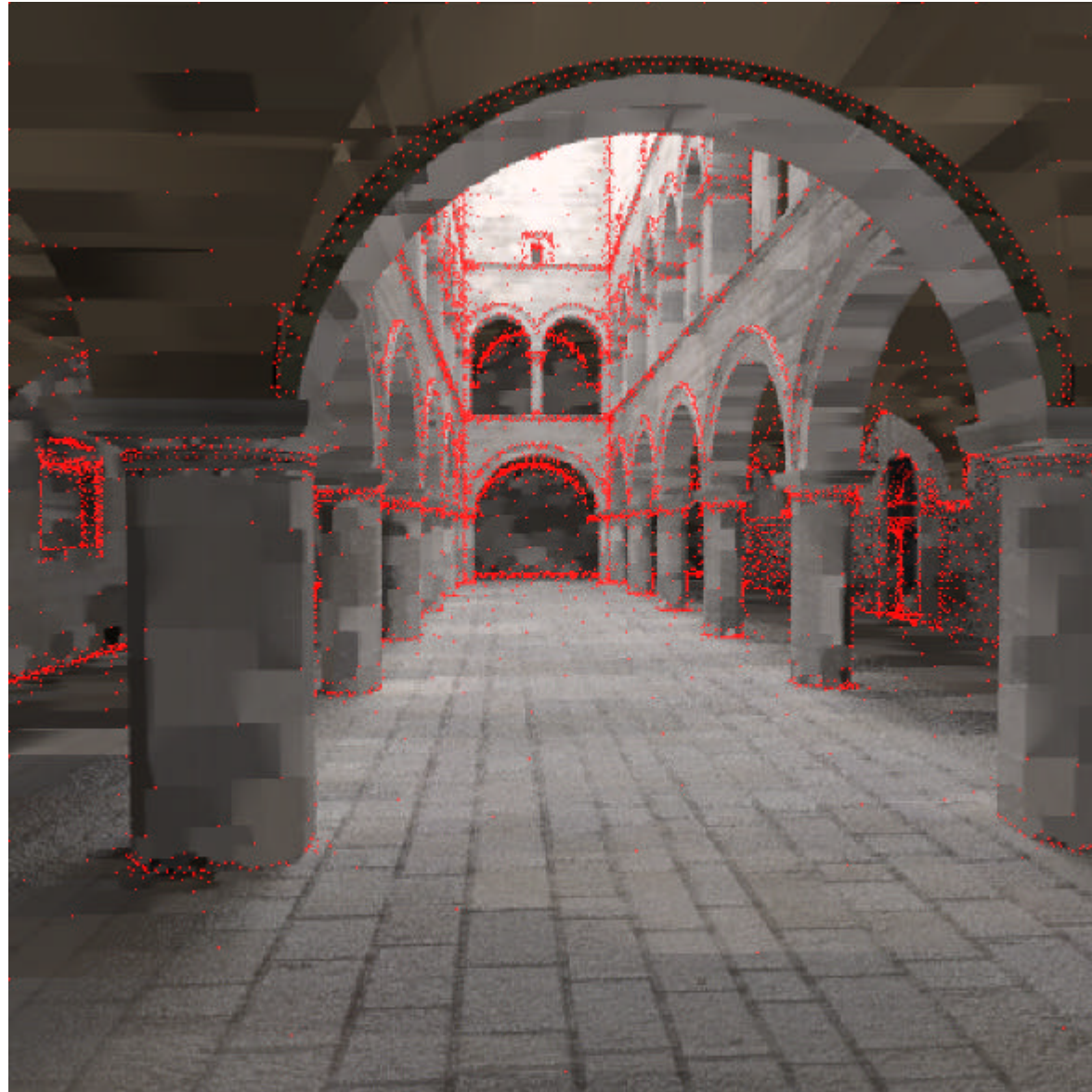
- Only irradiance is stored at each point (light representation is a single Spectrum object)
- As long as the surface is of a perfectly diffuse material, irradiance alone can exactly compute from the surface due to a particular incident lighting distribution
- A perfectly specular surface, however, can potentially introduce an arbitrarily large error

# ICaching vs. Path Tracing





# Points for IC





## Implementation Details

- Partitions BSDF for indirect lighting computation
  - Perfect specular reflection handled by sampling BSDF and recursively calling the integrator
- Implementation uses irradiance caching for both diffuse and glossy components
  - Glossy components introduce additional error
- Reflection and transmission handled separately
  - Reflective surface hemisphere completely different than transmissive surface hemisphere



## New Irradiance Values

- Uses a cosine-weighted distribution of directions
- Uses the standard Monte Carlo estimator



## Storing Values

- Uses an octree data structure to store computed estimates
- Each estimate has an axis-aligned bounding box associated with it, giving the overall area for which the sample is valid
- Bounding box clamped to make sure it is neither too large nor too small
- Boxes are smaller around groups of objects, as the more objects that are close to a sample point the greater potential for rapidly changing irradiance
- Estimate stored in IrradianceSample object





## Computing Irradiance

- Traverse the octree to find appropriate box
- Using an irradiance sample from the tree and the point to be shaded, test
  - Reject if surface normals too different
  - Reject if too far from point
  - Reject if sample in front of point
  - Compute error term
- If everything passes, weight the sample based on error term and use
- Final interpolated irradiance

$$E = (\sum_i w_i E_i) / (\sum_i w_i)$$



## Photon Mapping

- Photon Mapping is one of a family of *particle-tracing* algorithms
  - Construct paths from lights, and at each vertex the amount of incident illumination recorded
- Unlike irradiance caching, photon mapping handles both glossy and diffuse reflection well
- Can also handle perfectly specular reflection (handled separately with recursive ray tracing)



## Photon Integrator

- Photon mapping integrator traces particles into the scene
- It interpolates among particles (called photons) to approximate the incident illumination at shading points
- Integrator uses a kd-tree to store photons, which allows quick access to the photons around the point being shaded

## Photon Integrator (2)

- Adjusting the quality of results computed is easy with the photon mapper, as it partitions the LTE in a number of ways
  - Particles coming from lights are characterized: direct illumination, caustic illumination, and indirect illumination
- Partitioning allows flexibility in how reflected radiance is estimated
- Integrator also partitions the BSDF
  - Uses recursive ray tracing to handle perfectly specular components, and either photon maps or Monte Carlo ray tracing for the rest





## Photon Integrator Config

- Integrator is highly configurable
  - Desired number of photons of each type (direct, caustic, and indirect)
  - Number of photons used for interpolation
  - Whether to do “Final Gathering” or not



## Building the Photon Maps

- Particles begin at light sources and are traced through the scene until the integrator has accumulated the desired number of particle histories
- At each intersection of the path with an object a weighted particle contribution (of type *Photon*) is stored in the appropriate map
- A Halton sequence is used to generate particle rays, as they need to be well distributed but it is unknown ahead of time how many are needed

## Following the Photon

- While the photon intersects with objects in the scene
  - Handle photon/surface intersection
  - Update photon weight and photon ray direction
  - Possibly terminate photon path
    - Russian roulette



## Using the Photon Map

- At rendering time, the photon map is used to compute reflected light at each point being shaded
- Photon mapping interpolates information about illumination at the point from nearby photons
  - The more photons around the point and the higher their weights the more radiance is estimated to be incident at the point
  - Estimated radiance used in conjunction with surface BSDF to compute reflected light



# Photon Map in Action

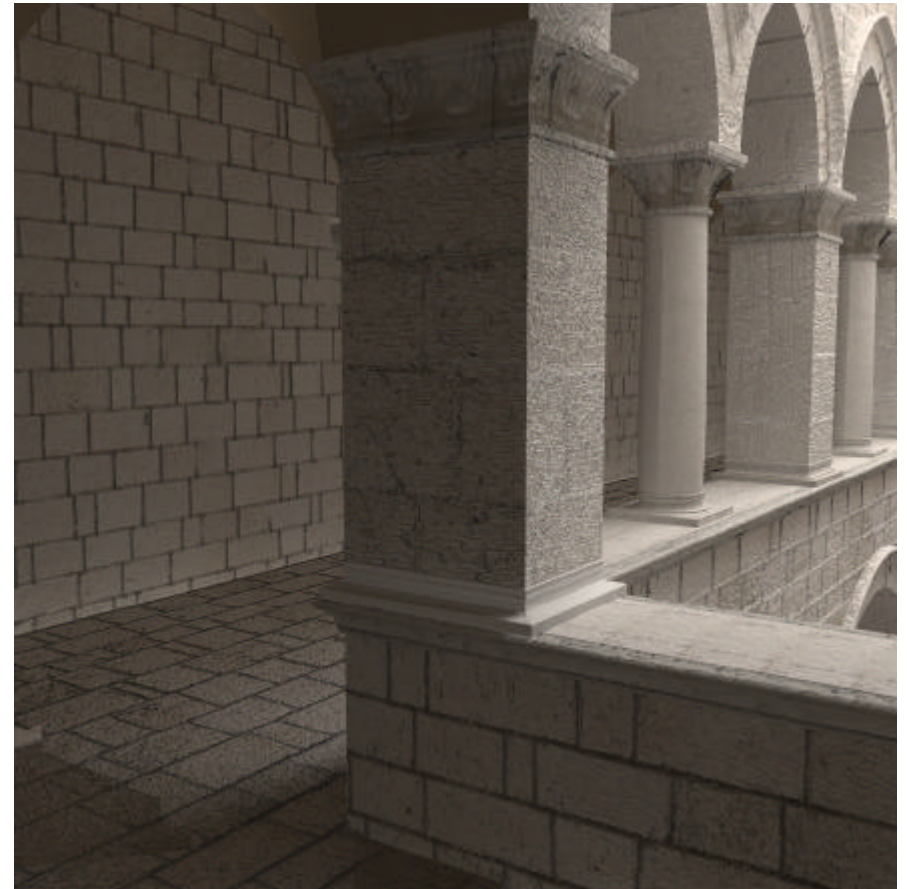
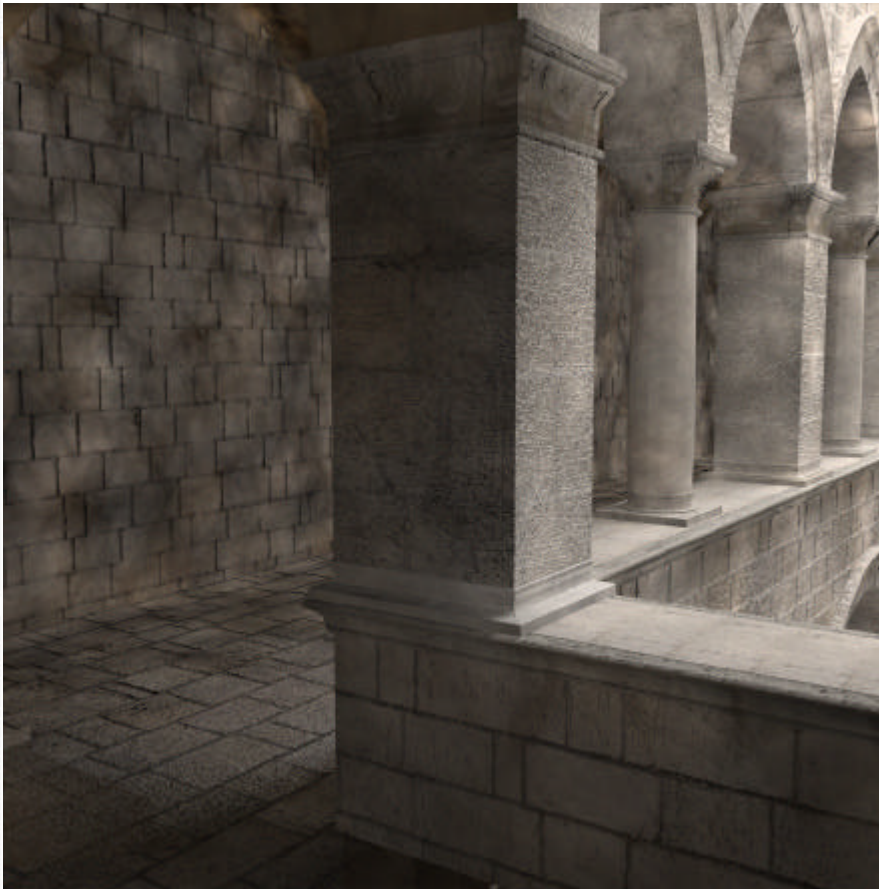




## Final Gathering

- Calculates the irradiance at selected sample points in the scene by shooting many rays and gathering light from other surfaces
- Very expensive for more than one bounce
- Can be combined with photon mapping:
  - Use photon mapping for  $N - 1$  bounces
  - Use final gathering for the final bounce

# Final Gathering Compare







## Photon Interpolation and Density Estimation

- Search the photon list for photons near the point to be shaded, and keep track of photons close to the point
  - Photons stored in kd-tree
- Need both the local density of particles and their individual weights
  - Use a kernel method to estimate density (will use a constant function)
  - Nearest-neighbor techniques can adaptively choose softening parameter based on local density

- Substituting everything into the measurement equation, the exitant radiance at point  $p$  in direction  $w$  is:

$$L_o(p, w_o) = p(p) \sum_j a_j f(p, w_o, w_j)$$

Where the sum is over the  $n$  nearest photons

## References

- Pharr, Humphreys, Physically Based Rendering, Sections 16.4 & 16.5
- Using Global Illumination in Turtle:  
<http://www.illuminate-labs.com/support/tutorial-folder/advanced-global-illumination/>