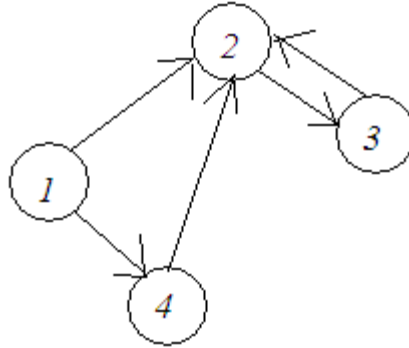


A *nontrivial cycle* is a cycle of at least two vertices. We want an algorithm to accept as input a digraph $G = (V, E)$ and a vertex $w \in V$. Your algorithm should decide whether w lies on a nontrivial cycle of G . So, for graph



if $w=1$ then your algorithm should return false, and if $w=2$ then your algorithm should return true. Your algorithm should work in worst-case time in $O(n^4)$.

SOLUTION: After computing array $E^+ = E \vee \dots \vee E^{n-1}$, vertex v_i lies on a nontrivial cycle if and only if there is a nontrivial path to itself. That is, if $E^+[i,i]=1$.

for $i \leftarrow 2$ **to** $n-1$ **do**

$$E^i \leftarrow E * E^{i-1} \quad O(n^4)$$

$$E^+ \leftarrow E \quad O(n^2)$$

for $i \leftarrow 2$ **to** $n-1$ **do**

$$E^+ \leftarrow E^+ \vee E^i \quad O(n^3)$$

if $E^+[i,i]=1$ **then return true** **else return false** $O(1)$

By the way, this problem can be solved in time in $O(m)$ using depth first search, which we did not cover in this class. You do a dfs from v_i and you return true if there is a back edge to the root v_i , and false otherwise.