

CS3133
HW#1

DUE: Tuesday, September 5

1. (8 points)

- a*) Prove that the union of two disjoint countably infinite sets is countably infinite.
- b*) Prove that the union of two disjoint countable sets is countable.

2. (10 points) A total function $f : \mathbb{N} \rightarrow \mathbb{N}$ is *monotone increasing* if $f(n) < f(n+1)$ for all $n \in \mathbb{N}$. Is the set $\{f : \mathbb{N} \rightarrow \mathbb{N} \mid f \text{ is monotone increasing and total}\}$ countable? Justify your answer.