

CS2223
HW#1 SOLUTIONS

1. (a) MAKENULL(S), INSERT(a,S), MEMBER?(a,S)

(b,c) One possibility is to store the elements of S in the first k positions of array $\text{int } S[n]$ in the order in which they arrive (unsorted)

$$\text{MAKENULL}(S) - \Theta(1)$$

$$\text{INSERT}(a,S) - \Theta(1)$$

$$\text{MEMBER?}(a,S) - \Theta(k) \quad \text{where } |S|=k$$

If the array S were sorted, then the analysis would be

$$\text{MAKENULL}(S) - \Theta(1)$$

$$\text{INSERT}(a,S) - \Theta(k) \quad \text{where } |S|=k$$

$$\text{MEMBER?}(a,S) - \Theta(\lg n)$$

2. (a) $1 \text{ sec} = c * n^2 = c * 1000^2$. Thus, $c=10^{-6}$. We solve for

$$s \text{ sec} = c * n^2 = 10^{-6} * 10000^2 = 10^{-6} * 10^8 = 100 \text{ sec}$$

(b) $1 \text{ sec} = c * n * \log n = c * 1000 * \ln 1000 = c * 1000 * \log_{10} 1000 / \log_{10} e = c * 3000 / \log_{10} e$

Thus, $c = \log_{10} e / 3000$. We solve for

$$s \text{ sec} = c * 10000 * \ln 10000 = 10000 * \ln 10000 * \log_{10} e / 3000 =$$

$$\log_{10} 1000 = 10000 * \frac{\log_{10} 10000}{\log_{10} e} * \frac{\log_{10} e}{3000} = 13 \frac{1}{3} \text{ seconds.}$$