

Name \_\_\_\_\_

CS503 Homework #5

Worked with: \_\_\_\_\_

URL's consulted: \_\_\_\_\_

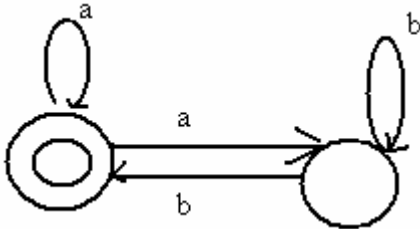
#1. Show that the following languages are or are not context-free

- a)  $\{w w^R w \mid w \in \{a,b\}^*\}$
- b)  $\{a^i b^{2i} c^j \mid i, j \geq 0\}$
- c)  $\{a^n b^n a^n \mid n \geq 0\}$
- d)  $\{x \in \{0,1\}^* \mid \#_0(x) = \#_1(x)\}$

#2. For each of the following languages, show it is either a) regular, b) context-free, but not regular, c) not context-free

- a)  $\{a^n b^m \mid n = 2m\}$
- b)  $\{a^n b^{2m} \mid n, m \geq 0\}$
- c)  $\{a^n b^m \mid n \neq m\}$

#3. a) Use the subset construction to convert the following nfa to a dfa



b) Give a regular expression for  $L(M)$

#4. Prove: CFL's are closed under union, concatenation and Kleene \*

#5. Prove: CFL's are not closed under intersection or complement