

**Homework #3**  
**Due Tuesday 4/11**  
**(at the beginning of class)**

This homework is the sole work of: \_\_\_\_\_ whose conference section is at: \_\_\_\_\_  
\_\_\_\_\_ whose conference section is at: \_\_\_\_\_

Sources (People, URL's, Books etc.) consulted:

Source \_\_\_\_\_ for Problem # \_\_\_\_\_

Source \_\_\_\_\_ for Problem # \_\_\_\_\_

Source \_\_\_\_\_ for Problem # \_\_\_\_\_

Date: \_\_\_\_\_

#1. (5 Points) Section 3.4, #48 a,b. Find these values of Ackerman's Function

a)  $A(1,0)$

d)  $A(2,2)$

Ackerman's function,  $A(m,n)$  is defined:

$$\begin{aligned} A(m,n) &= 2n && \text{if } m = 0 \\ &= 0 && \text{if } m \geq 1 \text{ and } n = 0 \\ &= 2 && \text{if } m \geq 1 \text{ and } n = 1 \\ &= A(m-1, A(m,n-1)) && \text{if } m \geq 1 \text{ and } n \geq 2 \end{aligned}$$

#2. (5 Points) Section 4.1, #32. How many functions are there from the set  $\{1, 2, 3, \dots, n\}$  (when  $n$  is a positive integer) to the set  $\{0,1\}$ .

#3. A computer password consists of from 1 to 3 letters chosen from the 26 letters in the alphabet (repetitions allowed). How many passwords are possible?

**#4. Show that if  $f$  is a function from  $S \rightarrow T$  where  $S$  and  $T$  are finite sets with  $|S| > |T|$ , then there are elements  $s_1$  and  $s_2$  with**

$$f(s_1) = f(s_2)$$

**i.e.,  $f$  is not 1-1**

**#5. Section 4.2, #18 Suppose there are 9 students in a discrete math class (can't be WPI!).**

- a) Show that the class must have at least 5 male students or at least 5 female students.**
  
- b) Show that the class must have at least 3 male students or at least 7 female students**

**#6.**

**Let  $S = \{1, 2, 3, 4, 5\}$**

- a) How many 3-permutations of  $S$  are there? List 5 of them.**
  
- b) How many 3-combinations of  $S$  are there? List 5 of them.**

**#7. How many ways can 3 of the letters in the word ALGORITHM be selected and written in a row?**

**#8. How many 8-bit binary strings have exactly three 1's?**