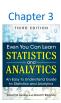
#### **IMGD 2905**

# **Descriptive Statistics**



#### **Summarizing Data**

- · With lots of playtesting, there will be a lot of data
  - This is a good thing!
- But raw data is just a pile of numbers
  - Rarely of interest
  - Or even sensible
- Q: How to summarize all this information?



# **Summarizing Data**

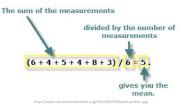
- · With lots of playtesting, there will be a lot of data
  - This is a good thing!
- But raw data is just a pile of numbers
  - Rarely of interest
  - Or even sensible
- · Q: How to summarize all this information?



Measures of central tendency

Χ

## Measure of Central Tendency: Mean



- Also called the "arithmetic mean" or "average"
- In Excel, =AVERAGE(range) =AVERAGEIF() - averages if numbers meet certain condition



#### Measure of Central Tendency: Median

· Sort values low to high and take middle value

• In Excel, =MEDIAN(range)



#### Measure of Central Tendency: Mode

- Number which occurs most frequently
- · Not too useful in many
- → Best use for categorical
  - e.g., most popular position in FIFA 18
- In Excel, =MODE()





# Depiction: Mean, Median, Mode requency (c)

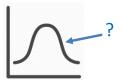
Which to Use, Mean, Median, Mode?

#### Which to Use, Mean, Median, Mode

- · Mean many statistical tests with sample
  - Estimator of population mean
- Uses all data
- · Median is useful for skewed data
  - e.g., income data (US Census) or housing prices (Zillo)
  - e.g., Overwatch team (6 players): 5 people level 5, 1 person level 275
    - Mean is 50 not so useful since no one at this level
    - Median is 5 more representative
  - Does not use all data. "Resistant" to extremes (e.g., 275)
  - But what if were exam scores? Hard to "bring up" grade
- Mode is useful primarily for categorical data only
  - Most played League champion, most popular maze, ...

### Other Measures of Position

- May not always want center
  - e.g., want to know best League Champions
- What other positions may be desired?



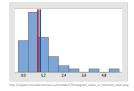
#### Other Measures of Position

- Maximum / Minimum
  - Not discussed more
- Trimmed Mean
- Quartiles
- Percentiles

#### **Trimmed Mean**

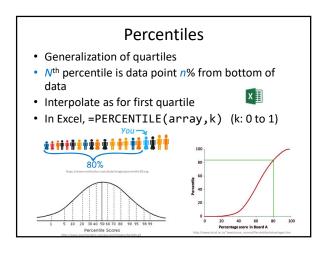
- Take "trimming" off top and bottom (typically 5% or 10%)
  - Reduces effects of extreme values, like median
- In Excel, =TRIMMEAN(array, percent)

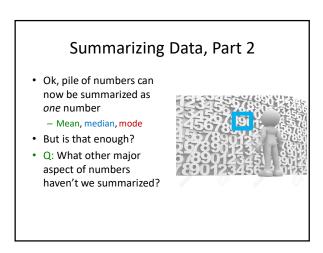


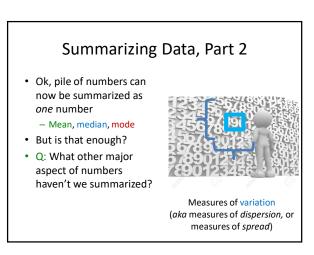


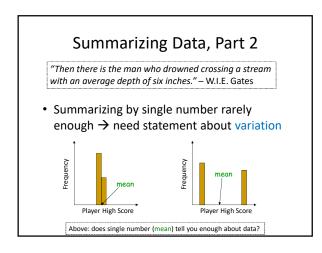
Blue - original mean Red – trimmed mean

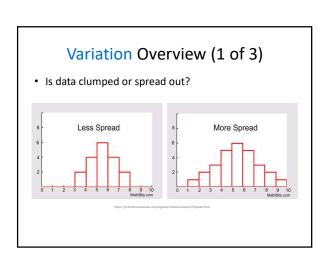
# Quartiles • Sort values • First quartile (Q1) is 25% from bottom • Third quartile (Q3) is 75% from bottom • (What is second quartile?) • In Excel, =QUARTILE(array,n)





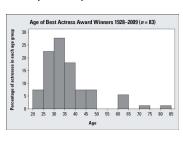






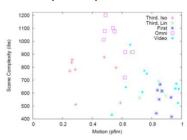
# Variation Overview (2 of 3)

• Is data clumped or spread out?

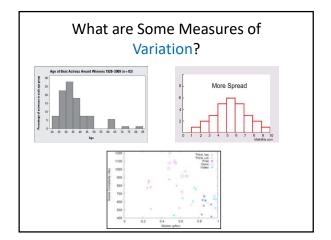


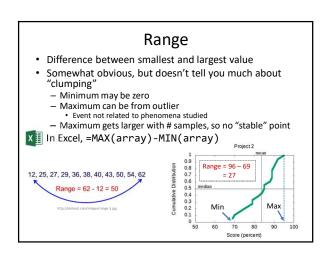
# Variation Overview (3 of 3)

• Is data clumped or spread out?



"Motion and Scene Complexity for Streaming Video Games"





#### Variance

- Compute mean of sample
- Compute how far each value in sample is from mean
  - Some can be less than mean, some greater
  - → So <u>square</u> this difference (why square?)
- Divide by number of sample values 1
  - The "-1" corrects "bias" when trying to estimate population variance using sample variance

Sample Variance = 
$$s^2 = \frac{\sum_{k=0}^{\text{"sum up all"}} \sum_{k=0}^{\text{"mean"}} \sum_{k=0}^{\text{"mean"}} \frac{\sum_{k=0}^{\text{"mean"}} \sum_{k=0}^{\text{"mean"}} \sum_{k=0}^{\text{"mean"}} \frac{\sum_{k=0}^{\text{"mean"}} \sum_{k=0}^{\text{"mean"}} \sum_{k=0}^$$

# Variance Example

- Sample kills in League of Legends match
  - 12, 20, 16, 18, 19
  - What is sample variance?
- First, mean = 85 / 5 = 17

<u>Kills</u>	<u>X – mean</u>	(X – mean) <sup>2</sup>	
12	-5	25	
20	3	9	
16	-1	1	
18	1	1	
19	2	4	
$s^2 = (2$	25 + 9 + 1 + 1 + 4) / (	(5-1) = 40 / 4 = 10	kills squared
			larger" means

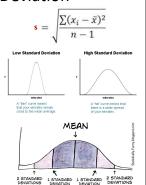
In Excel, =VAR(array)



"Larger" means "more spread" ... but units odd

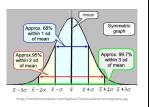
#### Standard Deviation

- Square-root of variance
- Usually, use standard deviation instead of variance
  - Why? → Same units as data (e.g., "kills" in previous example)
- Can compare standard deviation to mean (coefficient of variation, next)
- But first:
  - Mendenhall's Empirical Rule
  - Z-score



# Mendenhall's Empirical Rule

- About 68% data within one standard deviation of mean
  - interval between mean-s and mean+s contains about 68% of data
- About 95% within 2 standard deviations of mean
- Almost all data within 3 standard deviations of mean



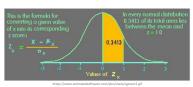
(Rules assume normal distribution)

#### **Z-Score**

· Measure of how "far" from center (mean) single data point is

 $z = \frac{X - \overline{X}}{}$ 

 Not measure of dispersion for whole data set



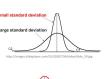
Example Mean Std dev 119 650 Z-score for X? (650 - 469)/119 1.52

# Coefficient of Variation (CV)

- Size of standard deviation relative
  - e.g., large sd & large mean, not so spread
  - but large sd & small mean, more spread
- Standard deviation divided by mean
- Can do this since same units!
- CV is "unit-less", so measure of spread independent of quantity
- E.g. seconds, clicks, spaces







Shown as percent (multiply by 100)

 $CV = \frac{s}{\overline{x}} \times 100$ 

Different Means
Different Standard Deviations

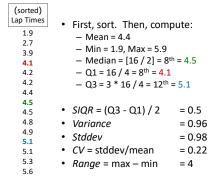
# Semi-Interquartile Range

•  $\frac{1}{2}$  distance between Q3 (75th percentile) and Q1 (25th percentile)

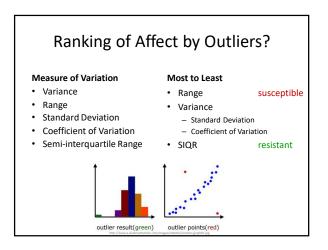


Guideline: use semi-interquantile (SIQR) for index of dispersion whenever using median as index of central tendency

# Index of Variation Example



# Ranking of Affect by Outliers? **Measure of Variation** Most to Least Variance Range Standard Deviation · Coefficient of Variation Semi-interquartile Range



# **Index of Variation Summary**

· Ranking of affect by outliers

Range

Variance

· Standard deviation Coefficient of variation

Semi-interquartile range

Sometimes called "boxplot"

resistant

susceptible

· Note, all only applied to quantitative data!

- For categorical data, can't quantify spread since no 'distance' between
- Instead, give number of categories for given percentile of samples
  - e.g., "90% of samples are in 3 categories"

# **Depicting Variation in Charts**

 Histogram (done)

· Cumulative distribution

(done)

Box-and-Whiskers

(new)

Error Bars

(new)

#### **Box-and-Whiskers Chart** Maximum Value Q3 (75th percentile) Median · Way of showing variation Highlight middle 50% (interquartile range, IQR) Lines go to smallest non-outlier "Whiskers" Points indicate outliers Middle line shows median Sometimes with mean Outlier? → Data value "way out there", "far" from the rest Formally, 1.5+ IQRs away from quartile Available in Excel 2016

