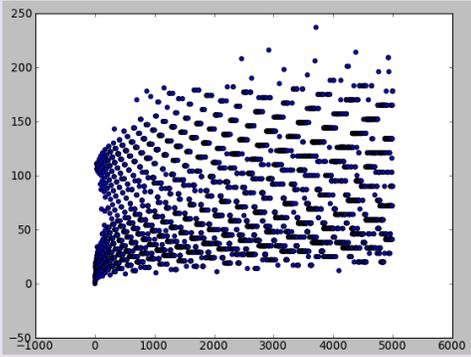


HW4: CS 110X C 2013

Note: This homework (and all remaining homework assignments) is a **partner homework** and must be completed by each partner pair. When you complete this assignment, you must not share your answers with any other student. Only one person from a partner pair needs to submit the assignment.

Q1	Working with Functions and While Loop
<div data-bbox="191 548 370 625" style="border: 1px solid gray; padding: 2px; margin-bottom: 5px;"> <i>Skills</i> </div> <div data-bbox="191 657 370 768" style="border: 1px solid gray; padding: 2px;"> <i>Lecture Dependency</i> Feb-1 </div>	<p data-bbox="394 520 1443 583">In a past homework assignment, you wrote code to compute newton's method 10 times for a given $f(x)$ and its <code>derivative(x)</code>.</p> <p data-bbox="394 625 1443 804">Now, write two helper functions $f(x)$ and <code>derivative(x)</code> using the structure as you saw in lab3 (and in class on February 1st). Write a <code>newtonMethod()</code> function that uses a <code>while</code> loop to compute a root given an initial guess. This <code>while</code> loop will terminate only when no more accuracy can be gained from the iteration. Review the provided code example to see how this would work.</p> <div data-bbox="418 835 1336 1171" style="border: 1px solid gray; padding: 5px; margin: 10px 0;"> <p style="background-color: #333; color: white; padding: 2px; margin: 0;">Sample Output</p> <pre style="margin: 0;">>>> newtonMethod() Enter initial guess for root 2 4.11795316565 3.37028590044 3.20769863535 3.20001689463 3.20000000008 3.2 The root 3.2 was found in 6 iterations</pre> </div> <p data-bbox="394 1213 1443 1287">Define “no more accuracy” as follows. Stop the <code>while</code> loop when two successive computations are within $1e-9$ of each other (i.e., <code>.000000001</code>).</p> <p data-bbox="394 1318 1443 1350">Use $f(x) = x^3 + 7.5x^2 - 18.94x - 48.96$ and $derivative(x) = 3x^2 + 15x - 18.94$</p> <p data-bbox="394 1392 1443 1465">Hint: Look at my solution working with sums of negative powers, provided with the template as a basis for this assignment.</p> <p data-bbox="394 1497 1443 1570">Also: Experiment with a variety of sample inputs to find the three roots of $f(x)$ and report them in your solution.</p> <p data-bbox="394 1602 1443 1633">Important: Report your roots by adding a variable like this:</p> <pre data-bbox="394 1675 849 1707">Q1_roots = [0.0, 0.0, 0.0]</pre> <p data-bbox="394 1749 1443 1780">Where you replace the 0.0 above with the values you determine.</p>

Q2	Demonstrate knowledge of functions that have parameters
<div data-bbox="191 468 370 541" style="border: 1px solid black; padding: 2px;"> Skills </div>	<p>The Collatz conjecture in mathematics is based on the following function <code>collatz(n)</code>. If n is an even number, then $\text{collatz}(n) = n/2$; if n is an odd number, then $\text{collatz}(n) = 3*n + 1$</p>
<div data-bbox="191 579 370 688" style="border: 1px solid black; padding: 2px;"> Lecture Dependency Feb-1 </div>	<p>One of the interesting observations about this function is that for any integer $n > 1$, you can generate a series $n_0, n_1, n_2, n_3, \dots$ as follows:</p>
	<div data-bbox="394 720 625 898" style="border: 1px solid black; padding: 2px;"> <pre>n0 = initial number n1 = collatz(n0) n2 = collatz(n1) n3 = collatz(n2) ...</pre> </div> <div data-bbox="394 930 1438 1077" style="border: 1px solid black; padding: 2px;"> <p>No one has been able to prove (or disprove) the simple claim that eventually you will reach 1 after a finite number of iterations. For example, if you start with 6, then after 8 iterations you will reach 1. Define a function <code>collatzIterations(n)</code> that uses a <code>while</code> loop to compute the number of iterations it takes to get from n to 1.</p> </div> <div data-bbox="394 1108 487 1434" style="border: 1px solid black; padding: 2px;"> <pre>n0 = 6 n1 = 3 n2 = 10 n3 = 5 n4 = 16 n5 = 8 n6 = 4 n7 = 2 n8 = 1</pre> </div> <div data-bbox="1097 579 1430 747" style="border: 1px solid black; padding: 2px;"> <p>Sample Output</p> <pre>>>> collatz(6) 3 >>> collatz(5) 16</pre> </div> <div data-bbox="906 1115 1377 1472" style="border: 1px solid black; padding: 2px;">  </div> <div data-bbox="394 1524 1390 1759" style="border: 1px solid black; padding: 2px;"> <p>Sample Output</p> <pre>>>> collatzIterations(6) 8 >>> collatzIterations(1287687156763264782) 443 >>> collatzIterations(1) 0</pre> </div>
	<p>Then write a function <code>plotCollatz()</code> that generates a scatter plot of $(n, \text{collatzIterations}(n))$ for integers in the range 1 through and including 5000. You should be able to produce a scatter plot graph like you see above.</p>

Q3	Demonstrate ability to read and write values to and from a file										
<div style="border: 1px solid gray; padding: 2px; margin-bottom: 5px;"><i>Skills</i></div> <div style="border: 1px solid gray; height: 15px; width: 100%;"></div>	<p>You are to write a Python function <code>sortit(input, output)</code> that reads in a number of words (one per line) stored in the file identified by <code>input</code>, and then writes to <code>output</code> these words, one per line, in sorted order.</p> <table border="1" style="width: 100%; border-collapse: collapse;"> <thead> <tr> <th style="background-color: #333; color: white;">InputFile.txt</th> <th style="background-color: #333; color: white;">OutputFile.txt</th> </tr> </thead> <tbody> <tr> <td>This</td> <td>A</td> </tr> <tr> <td>Is</td> <td>Is</td> </tr> <tr> <td>A</td> <td>Test</td> </tr> <tr> <td>Test</td> <td>This</td> </tr> </tbody> </table> <p>You can be assured that the designated input file will always exist. Look at the template for the structure of this function.</p> <p>To validate that your function works, you should write a <code>testSortIt()</code> method that calls <code>sortit()</code> with file names of your choosing. Note that the TA will evaluate using their own files.</p>	InputFile.txt	OutputFile.txt	This	A	Is	Is	A	Test	Test	This
InputFile.txt		OutputFile.txt									
This		A									
Is	Is										
A	Test										
Test	This										
<div style="border: 1px solid gray; padding: 2px; margin-bottom: 5px;"><i>Lecture Dependency</i></div> <div style="border: 1px solid gray; padding: 2px;">Feb-1</div>											

Q4	Test Interactive Functions
<div style="border: 1px solid gray; padding: 2px; margin-bottom: 5px;"><i>Skills</i></div> <div style="border: 1px solid gray; height: 15px; width: 100%;"></div>	<p>The Body Mass Index (BMI) is calculated as a person's weight (in pounds) times 720, divided by the square of the person's height (in inches). A BMI in the range 19-25, inclusive, is considered healthy. Write a function <code>BMIcheck(weight, height)</code> that calculates a person's BMI and prints a message telling whether they are above, within, or below the healthy range.</p>
<div style="border: 1px solid gray; padding: 2px; margin-bottom: 5px;"><i>Lecture Dependency</i></div> <div style="border: 1px solid gray; padding: 2px;">Feb-1</div>	

Q5	Test Interactive Functions
<div style="border: 1px solid gray; padding: 2px; margin-bottom: 5px;"><i>Skills</i></div> <div style="border: 1px solid gray; height: 15px; width: 100%;"></div>	<p>A speeding ticket fine policy is defined as following. The base ticket is \$50 plus \$5 for each mile per hour over the limit plus a penalty of \$200 for any speed over 90 miles per hour. Write a python function <code>speedCheck(speedLimit, actualSpeed)</code> that accepts a speed limit and a clocked speed and either prints a message indicating the speed was legal or prints the amount of the fine, if the speed was illegal.</p>
<div style="border: 1px solid gray; padding: 2px; margin-bottom: 5px;"><i>Lecture Dependency</i></div> <div style="border: 1px solid gray; padding: 2px;">Feb-1</div>	

How To Get Started On This Assignment

A template [HW4.py](#) file is provided to you with sample enrollment data.

To solve question you need to know how to determine if a number is odd. This is mentioned in the book (page 59) but you might not have noticed it because I have not yet demonstrated this in class. There is a Python operator, % (percent sign), that can be used to determine the remainder during integer division.

Here is a snippet to get you started:

```
print ("remainder when dividing 10 by 3:")
print (10 % 3)

print ("remainder when dividing 6 by 2:")
print (6 % 2)

if 5 % 2 == 1:
    print ("5 is an odd number.")
```

To see if a number is odd, check (using ==) whether the remainder of dividing that number by 2 is 1.

Submit your HW4.py file using the web-based turnin system. As we have mentioned in class, only one of the team members needs to submit the assignment. But just make sure that something gets submitted!