

# Security Goals and Protocol Transformations<sup>\*</sup>

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**Abstract.** Cryptographic protocol designers work incrementally. Having achieved some goals for confidentiality and authentication in a protocol  $\Pi_1$ , they transform it to a richer  $\Pi_2$  to achieve new goals.

But do the original goals still hold? More precisely, if a goal formula  $\Gamma$  holds whenever  $\Pi_1$  runs against an adversary, does a translation of  $\Gamma$  hold whenever  $\Pi_2$  runs against it?

We prove that a transformation preserves goal formulas if a labeled transition system for analyzing  $\Pi_1$  simulates a portion of an LTS for analyzing  $\Pi_2$ , while preserving progress in that portion.

Thus, we examine the process of analyzing a protocol  $\Pi$ . We use LTSS that describe *our* activity when *analyzing*  $\Pi$ , not that of the principals *executing*  $\Pi$ . Each analysis step considers—for an observed message reception—what earlier transmissions would explain it. The LTS then contains a transition from a fragmentary execution containing the reception to a richer one containing an explaining transmission. The strand space protocol analysis tool CPSA generates some of the LTSS used.

## 1 Introduction

Protocol design is an art of reuse. A few basic patterns for achieving authentication and confidentiality—despite actively malicious parties—are frequently adapted to new contexts. Designers combine these patterns, piggy-backing values on top of them, to solve many problems. The transformations modify message structure; add new transmissions or receptions on a given role; and add entirely new roles. Constructing protocols may be difficult, particularly for interactions involving more than two participants: Some data values may be shared among subsets of the participants, while remaining hidden from the other participants. Designers use existing protocols as heuristics for parts of the protocol, welding the parts cleverly together, so that the transformed protocol preserves the goals achieved by the components, while achieving additional goals.

Our goal here is not to make this cleverness unnecessary, but to explain it semantically. Thm. 2 justifies inferring that a transformed protocol satisfies some security goals, when the source protocol did. Although a logical result about models of protocol behavior and the formulas they satisfy, it is a corollary of a logic-free theorem (Thm. 1). The latter concerns only fragments of protocol executions (called *skeletons*), the information-preserving maps (*homomorphisms*) between them, and some labeled transition systems. These LTSS formalize the

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activity of protocol analysis. Reifying the protocol analysis activity into LTSS, and explaining relations between protocols using them, are new in this paper.

Although these results help us avoid verifying the transformed protocol directly, they also have a deeper value. They suggest design principles for incremental construction of protocols. We expect future work to lead to *syntactic* conditions that imply that a transformation preserves security goals. Protocol design, now a hit-or-miss activity requiring experience and ingenuity, could become a more predictable and possibly tool-supported process.

**Structure of this paper.** Section 2 introduces two protocols, with two transformations between them, motivating a definition of transformation (Def. 2). Section 3 analyzes these protocols, illustrating how a transformation can preserve the activity of protocol analysis. Section 4 axiomatizes these analysis activities, representing them as labeled transition systems. A simulation-plus-progress relation on LTSS ensures that a transformation does not create counterexamples to security goals (Section 5). Section 6 defines classical first order languages  $\mathcal{L}(II)$ , and defines security goal translations. We lift Thm. 1 to satisfaction of goals (Thm. 2) in Section 7, and comment on related and future work.

**Strand Spaces.** We work within the strand space theory [18]. A **strand** is the sequence of message transmissions and message receptions executed by a single principal in a single protocol session. Transmission and reception events jointly are **nodes**. We will write strands, either horizontally or vertically, as sequences of bullets connected by double arrows:  $\bullet \Rightarrow \bullet$ . (See [18, Sec. 2.4].)

A **protocol**  $II$  consists of a finite set of strands, called the **roles** of the protocol, possibly annotated with some trust assumptions that we will not need here. We give each  $II$  a “listener” role, consisting of a single node receiving a message  $t$ , which can witness for the disclosure of  $t$ . An **instance** of a role  $\rho \in II$  results from choosing values from some reasonable algebra  $\mathfrak{M}$  of messages for  $\rho$ ’s parameters. We formalize this choice by applying a substitution  $\alpha$  to  $\rho$ , where a substitution  $\alpha$  means a homomorphism from  $\mathfrak{M}$  to itself. The strand  $\alpha(\rho)$  is the sequence of transmissions and receptions in which each message in  $\rho$  is instantiated according to  $\alpha$ . That is, each parameter  $x$  appearing in  $\rho$  is replaced by  $\alpha(x)$ . Each strand  $\alpha(\rho)$  is a **regular** behavior of some principal in  $II$ , i.e. a local session in which the principal complies with  $II$ . (See [18, Sec. 2.5].)

A fragmentary execution, called a **skeleton**, consists of a number of regular strands of  $II$ , or their initial segments. A skeleton  $\mathbb{A}$  consists of its regular nodes, equipped with (i) a partial ordering  $\preceq_{\mathbb{A}}$ , akin to the Lamport causal ordering [22]; (ii) some assumptions  $\text{unique}(\mathbb{A})$  about freshly chosen values; and (iii) some assumptions  $\text{non}(\mathbb{A})$  about uncompromised long term keys. (See [18, Def. 3.1].)

A skeleton  $\mathbb{A}$  is **realized** if, whenever  $n$  is a reception node in  $\mathbb{A}$ , an adversary can obtain or construct its message  $t$ , without violating the assumptions  $\text{unique}(\mathbb{A})$  and  $\text{non}(\mathbb{A})$ . No value assumed freshly chosen should equal a guessed or independently chosen value. No long term key assumed uncompromised should be used by the adversary. (See [18, Defs. 3.2–4].) A realized skeleton is a full execution. When node  $n$  receives  $t$ , then the adversary obtains  $t$ , or can derive it using transmissions prior to  $n$  in the partial ordering  $\preceq_{\mathbb{A}}$ .

Any skeleton  $\mathbb{A}$  represents a set of realized skeletons  $\mathbb{B}$ . These are the executions in which at least the transmissions and receptions in  $\mathbb{A}$  have occurred, possibly made more specific by a substitution  $\alpha$ , and node ordering extends  $\preceq_{\mathbb{A}}$ . Moreover, the assumptions  $\alpha(\text{unique}(\mathbb{A}))$  and  $\alpha(\text{non}(\mathbb{A}))$ —i.e. the images of  $\text{unique}(\mathbb{A})$  and  $\text{non}(\mathbb{A})$  under  $\alpha$ —must be satisfied.

**Definition 1.** The concatenation of two messages  $t_0$  and  $t_1$  is  $t_0 \hat{\ } t_1$ , and the (asymmetric) encryption of  $t$  using the public encryption key of  $B$  is  $\{\!\{t\}\!\}_{\text{pk}(B)}$ .

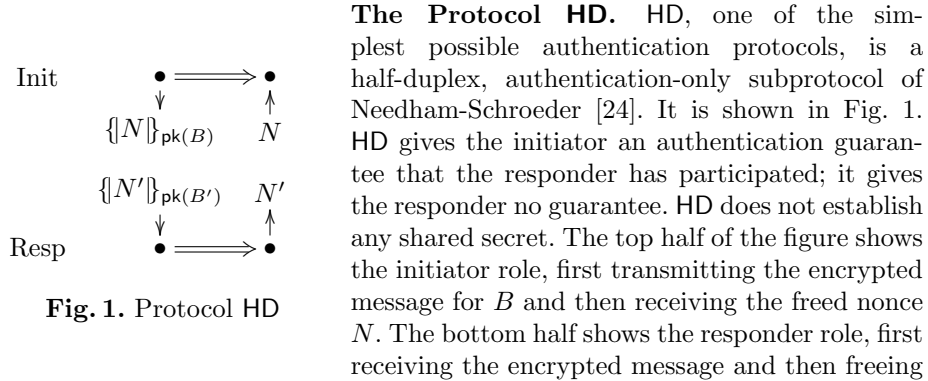
The  $i^{\text{th}}$  node along a strand  $s$ , starting from 1, is  $s \downarrow i$ .

We write  $t_0 \sqsubseteq t_1$  to mean that message  $t_0$  is an **ingredient** in  $t_1$ , i.e. that  $t_0$  is a subterm of  $t_1$  considering plaintexts but not the keys used to prepare encryptions. That is,  $\sqsubseteq$  is the smallest reflexive transitive relation such that  $t_0 \sqsubseteq \{\!\{t_0\}\!\}_K$ ;  $t_0 \sqsubseteq t_0 \hat{\ } t_1$ , and  $t_1 \sqsubseteq t_0 \hat{\ } t_1$ . The key  $K$  used in an encryption  $\{\!\{t_0\}\!\}_K$  is not an ingredient of it, however, unless it was an ingredient of  $t_0$  (contrary to good practice). For instance,  $N_b \sqsubseteq \{\!\{N_b \hat{\ } B\}\!\}_{\text{pk}(A)}$ , but  $\text{pk}(A) \not\sqsubseteq \{\!\{N_b \hat{\ } B\}\!\}_{\text{pk}(A)}$ .

A message  $t_0$  **originates at** a node  $n$  iff  $n$  is a transmission node,  $t_0 \sqsubseteq \text{msg}(n)$ , and for all  $m$  such that  $m \Rightarrow^+ n$ ,  $t_0 \not\sqsubseteq \text{msg}(m)$ . Thus,  $t_0$  originates at  $n$  when it was transmitted as an ingredient, but was neither transmitted nor received earlier on the same strand.

If  $\rho \in \Pi$  is a role of protocol  $\Pi$ , then  $\text{instances}(\rho)$  is the set of instances of  $\rho$ , i.e. the set  $\{\alpha(\rho) : \alpha \text{ is a substitution}\}$ . The (larger) set of strands that agree with a member of  $\text{instances}(\rho)$  on the first  $i$  nodes is defined:  $\text{instances}(\rho|_i) = \{s : \exists r \in \text{instances}(\rho). \forall j \leq i. s \downarrow j = r \downarrow j\}$ . So  $\text{instances}(\rho|_i)$  contains a strand if it is indistinguishable from a run of  $\rho$  while only  $i$  events have occurred. If  $r \in \text{instances}(\rho)$  agrees with  $s$  up to  $i$ , then  $r$  is an **instances**( $\rho|_i$ )-**witness for**  $s$ .

## 2 Some Protocol Transformations



**Fig. 1.** Protocol HD

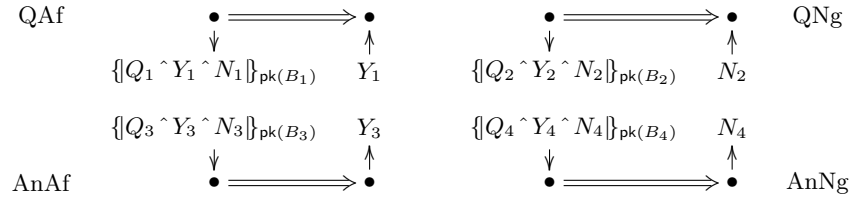
The Protocol HD. HD, one of the simplest possible authentication protocols, is a half-duplex, authentication-only subprotocol of Needham-Schroeder [24]. It is shown in Fig. 1. HD gives the initiator an authentication guarantee that the responder has participated; it gives the responder no guarantee. HD does not establish any shared secret. The top half of the figure shows the initiator role, first transmitting the encrypted message for  $B$  and then receiving the freed nonce  $N$ . The bottom half shows the responder role, first receiving the encrypted message and then freeing and transmitting  $N'$ . A regular strand of HD is any instance of either one of these roles, using any values for the parameters  $N, B, N', B'$ . We do not show the listener role in this or other protocol diagrams, since it is always present, and simply passively receives a message  $t$ .

A skeleton  $\mathbb{A}$  over HD contains any number of these regular strands, and selects sets of freshness and non-compromise assumptions  $\text{unique}(\mathbb{A})$  and  $\text{non}(\mathbb{A})$ .

$\mathbb{A}$  is realized if an adversary can synthesize the message received on each reception node, using messages transmitted earlier relative to  $\preceq_{\mathbb{A}}$ , without violating the assumptions  $\text{unique}(\mathbb{A})$  and  $\text{non}(\mathbb{A})$ .

**The Yes-or-No Protocol.** The Yes-or-No Protocol YN allows a Questioner to ask a question, to which the Answerer gives a private, authenticated reply; YN is constructed by two transformations of HD. In YN, the question and answer should each remain secret. Indeed, the protocol should prevent even an adversary who has guessed the question from determining what answer was given. The Questioner authenticates the Answerer as supplying an answer. The Questioner chooses two random nonces, and encrypts them, together with the question. The Answerer releases the first of the two nonces to indicate a *yes*, and the second to indicate a *no*. No adversary learns anything, since whichever nonce was released, the questioner was equally likely to have used it in the other position.

The protocol has four roles (Fig. 2). One describes the behavior of a Ques-



**Fig. 2.** The Yes-or-No Protocol YN

tioner receiving an affirmative answer. The second describes the behavior of a Questioner receiving a negative answer. The remaining two describe the behavior of an Answerer providing an affirmative and respectively negative answer.

We can view either half of this diagram as a transformation of the protocol HD. We first rename the nonces  $N, N'$  of HD to the affirmative nonces  $Y_1, Y_3$ , to view the left half in this way. We would rename  $N, N'$  to the negative nonces  $N_2, N_4$  for the right half. Before formalizing the transformations, we formalize these renamings as substitutions (homomorphisms) on the message algebra  $\mathfrak{M}$ . The renamings, yielding respectively the protocols  $\alpha_1(\text{HD})$  and  $\alpha_2(\text{HD})$ , are:

$$\begin{aligned} \alpha_1 &= [N \mapsto Y_1, N' \mapsto Y_3, B \mapsto B_1, B' \mapsto B_3] \quad \text{and} \\ \alpha_2 &= [N \mapsto N_2, N' \mapsto N_4, B \mapsto B_2, B' \mapsto B_4] \end{aligned}$$

We could alternatively incorporate substitutions such as  $\alpha_1, \alpha_2$  into the transformations themselves, but at the cost of complicating the already subtle Def. 2.

**Protocol Transformations.** By a *protocol transformation* from a source protocol  $\Pi_1$  to a target protocol  $\Pi_2$ , we mean a map from nodes on roles of  $\Pi_1$  to nodes on roles of  $\Pi_2$ . The images of nodes of a single role  $\rho_1 \in \Pi_1$  all lie along a single role  $\rho_2 \in \Pi_2$ , so we formalize this with two components: one which selects

the correct  $\rho_2$ , and another which is a function  $g$  that maps the index of a node on  $\rho_1$  to the index of its image along  $\rho_2$ . Thus:

$F_1: \alpha_1(\text{HD}) \rightarrow \text{YN}$  sends Init to the Questioner’s Affirmative role QAf. The first node of Init—the transmission node—is associated with the first node of QAf, and the second nodes are associated.  $F_1$  sends Resp to the Answerer’s Affirmative role AnAf, preserving node indices.

So  $F_1(\text{Init}) = (\text{QAf}, \text{ld})$  and  $F_1(\text{Resp}) = (\text{AnAf}, \text{ld})$ .

$F_2: \alpha_2(\text{HD}) \rightarrow \text{YN}$  acts similarly, with negative target roles. It sends Init to the Questioner’s Negative role QNg. It sends Resp to the Answerer’s Negative role AnNg. In both,  $F_2$  preserves node indices, so  $F_2(\text{Init}) = (\text{QNg}, \text{ld})$ , and  $F_2(\text{Resp}) = (\text{AnNg}, \text{ld})$ .

These node index functions  $g$  are the identity  $\text{ld}$ , but other transformations use non-identity  $gs$ . For instance, if one principal in YN sent a message before the messages shown, which the other received before the messages shown, then we would alter  $F_1, F_2$  to use  $\lambda i. i + 1$  to increment each node index.

Our examples have several properties. The node index mapping functions are order-preserving, and the transformations also preserve the direction of the nodes (transmission vs. reception). The transmission node  $n$  of the HD initiator originates the value  $N$  and this value—as renamed by  $\alpha_1$ —also originates on  $F_1(n)$  (see Def. 1). The reception node  $m$  of the HD responder receives  $N \sqsubseteq \text{msg}(m)$ , and we also have  $\alpha_1(N) \sqsubseteq \text{msg}(F_1(m))$ . Thus,  $F_1$  preserves the originated values and the ingredients of nodes. Similarly,  $F_2$  preserves these properties of  $\alpha_2(N)$ .

These properties, with one other, define a protocol transformation. This last property is vacuously true of  $F_1, F_2$ . It concerns branching, as for instance, in a transformation  $F: \text{YN} \rightarrow \Pi$ , QAf and QNg branch after a first node in common. It says that the result in the target  $\Pi$  should not commit to either branch until the source behaviors have committed by diverging from each other.

**Definition 2 (Transformation).** *Suppose  $F$  maps each role  $\rho_1 \in \Pi_1$  to a pair  $\rho_2, g$ , where  $\rho_2 \in \Pi_2$  and  $g: \mathbb{N}^+ \rightarrow \mathbb{N}^+$ .  $F$  is a protocol transformation iff:*

1.  $g$  is order-preserving and  $g(\text{length}(\rho_1)) \leq \text{length}(\rho_2)$ ;
2.  $\rho_1 \downarrow i$  is a transmission (or resp. reception) node iff  $\rho_2 \downarrow g(i)$  is;
3. Whenever  $x \sqsubseteq \text{msg}(\rho_1 \downarrow i)$ , there exists a  $j \leq g(i)$  such that  $x \sqsubseteq \text{msg}(\rho_2 \downarrow j)$ ;
4. Whenever  $x$  originates on  $\rho_1 \downarrow i$ , for some  $j \leq g(i)$ ,  $x$  originates on  $\rho_2 \downarrow j$ ;
5. Suppose that  $\rho_1$  and  $\sigma_1 \in \Pi_1$  have a common instance up to  $i$ , i.e.  $\alpha(\rho_1) \in \text{instances}(\sigma_1|_i)$ . Let  $F(\sigma_1) = \sigma_2, h$ . Then we have  $g(j) = h(j)$  for all  $j \leq i$ . Moreover,  $\alpha(\rho_2) \in \text{instances}(\sigma_2|_{h(i)})$ .

### 3 Security Analysis of HD and YN

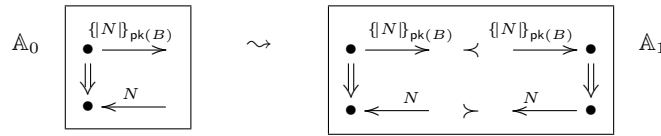
Security analysis aims to find what must have happened—or must not have happened—if a certain situation has arisen. In the case of HD, the relevant analysis considers what must have happened, when there has been a local session

of the initiator role. If its nonce  $N$  was freshly chosen, and  $B$ 's private decryption key was uncompromised, what can we be sure has happened?

CPSA [26] is a software tool to answer such questions. It starts with an object representing the situation—namely a skeleton  $\mathbb{A}$  (cf. p. 3)—and generates enriched skeletons to represent all the complete executions compatible with the starting point  $\mathbb{A}$ . In each step it takes, CPSA locates an *unsolved test*, some reception node that cannot be explained by adversary activity, given the regular (non-adversarial) activity currently present in the skeleton. For each alternate piece of regular activity that could help explain the current skeleton, CPSA constructs an enriched skeleton; the search branches to explore those enrichments. When every reception node is explained, and the skeleton is realized, CPSA has found a leaf in the search (“a shape”).

CPSA implements a labeled transition system. The nodes are skeletons. There is a transition  $\mathbb{A} \xrightarrow{\ell} \mathbb{B}_i$  if  $\mathbb{B}_i$  is one of the alternate enrichments that explains a test  $\ell$  unsolved in  $\mathbb{A}$ . All of the  $\mathbb{B}_i$  that provide alternate solutions to  $\ell$  are successors of  $\mathbb{A}$  with the same label  $\ell$ . A label  $\ell$  indicates some unexplained behavior in  $\mathbb{A}$  that prevents it from being realized; each  $\mathbb{B}_i$  offers a different potential way to fix  $\ell$ . Given a protocol  $\Pi$ , security analysis for authentication and confidentiality goals involving the situation  $\mathbb{A}_0$  consists of exploring the portion of the LTS for  $\Pi$  accessible from  $\mathbb{A}_0$ .

**Analyzing HD.** In HD, the relevant starting skeleton is  $\mathbb{A}_0$ , shown on the left in Fig. 3, where the assumptions—that  $N$  was freshly chosen and  $B$ 's decryp-



**Fig. 3.** Goal met by HD, with  $\text{unique} = \{N\}$ ,  $\text{non} = \{\text{pk}(B)^{-1}\}$

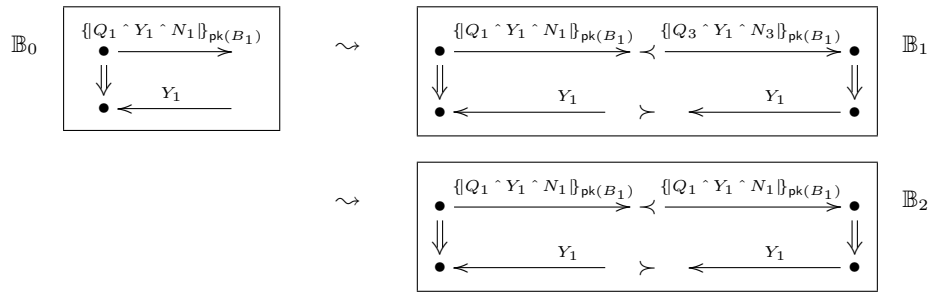
tion key is uncompromised—are shown in the caption. CPSA identifies the lower reception node as unexplained, given the assumptions: how did  $N$  escape from the encryption  $\{\{N\}\}_{\text{pk}(B)}$ ? It can be solved in only one way, namely, a responder strand can extract  $N$  and retransmit it as shown. The result of this step,  $\mathbb{A}_1$ , is now realized, i.e. fully explained.

Since every realized skeleton that enriches  $\mathbb{A}_0$  must solve this test, it must be an enrichment of  $\mathbb{A}_1$ . In every situation in which an initiator has acted as in  $\mathbb{A}_0$ , a responder has had a corresponding local session. This is  $A$ 's authentication guarantee, telling  $A$  that  $B$  has participated in the session.

**Transforming our Analysis under  $F_1, F_2$ .** Each transformation  $F: \Pi_1 \mapsto \Pi_2$  determines a map that lifts any skeleton  $\mathbb{A}$  of the protocol  $\Pi_1$  to a corresponding skeleton  $F(\mathbb{A})$  of  $\Pi_2$ . In particular, suppose  $\mathbb{A}$  contains the first  $j$  nodes

of a strand  $s$ , and  $s$  is an instance of a role  $\rho_1 \in \Pi_1$ . Thus, for some substitution  $\beta$ ,  $s = \beta(\rho_1)$ . When  $F(\rho_1) = (\rho_2, g)$ , then  $F(\mathbb{A})$  should contain the first  $g(j)$  nodes of a strand  $F(s)$ . It should be an instance of  $\rho_2 \in \Pi_2$ . Specifically  $F(s) = \beta'(\rho_2)$ , where  $\beta'$  agrees with  $\beta$  on all the parameters appearing in the first  $j$  nodes of  $\rho_1$ . The remaining parameters of  $\rho_2$  are assigned new values, chosen to be distinct from any of the other values selected for  $F(\mathbb{A})$ . Since  $\beta'$  depends on all of  $\mathbb{A}$ , it would be more accurate to write  $F_{\mathbb{A}}(s)$  rather than  $F(s)$ , although we will not do so.

If we apply first  $\alpha_1$  and then  $F_1$  mechanically to Fig. 3, we obtain the upper



**Fig. 4.** A goal met by YN, with  $\text{unique} = \{Y_1\}$ ,  $\text{non} = \{pk(B_1)^{-1}\}$

two skeletons in Fig. 4. In  $\mathbb{B}_0$ , the lower node, which is the image of the unsolved test node of  $\mathbb{A}_0$ , is itself an unsolved test node. Moreover, the new strand in  $\mathbb{B}_1$  is the image of the one solution in HD. However,  $\mathbb{B}_1$  is not realized. There is only one way to complete the search for a realized skeleton, namely to identify corresponding parameters in the questioner and answerer strands of  $\mathbb{B}_1$ , setting  $Q_3 = Q_1$  and  $N_3 = N_1$ . The result is  $\mathbb{B}_2$ .

CPSA generates  $\mathbb{B}_2$  from  $\mathbb{B}_0$  in one step, which factors through  $\mathbb{B}_1$ : To realize  $\mathbb{B}_0$ , one must add the information present in  $\mathbb{B}_1$ , and also the additional information that  $Q_3 = Q_1$  and  $N_3 = N_1$ . In any YN scenario in which  $\mathbb{B}_0$  has occurred, the information in  $\mathbb{B}_1$  also holds. Thus, the security analysis of HD has given us sound conclusions about YN. We now formalize this relation.

## 4 What is Protocol Analysis?

In our examples, we started with skeletons  $\mathbb{A}_0, \mathbb{B}_0$ . They were not large enough to be realized, i.e. to be executions that could really happen without any extra regular behavior. We then enriched them to the realized skeletons  $\mathbb{A}_1, \mathbb{B}_2$ .

**Homomorphisms.** These enrichments are examples of *homomorphisms* among skeletons [18, Def. 3.6]. A *homomorphism*  $H: \mathbb{A} \rightarrow \mathbb{B}$  between skeletons of  $\Pi$  transforms messages in a structure-respecting way, mapping transmission nodes

to transmission nodes and reception nodes to reception nodes. A homomorphism must preserve the ordering relations of the source, and it must preserve its freshness and non-compromise assumptions. It is an *information-preserving map*.

Homomorphisms determine a preorder, not a partial order, since  $\mathbb{A} \xrightarrow{H} \mathbb{B} \xrightarrow{J} \mathbb{A}$  does not imply that  $J \circ H$  is an isomorphism. However, if  $H, J$  map distinct nodes of their sources injectively to distinct nodes of their targets, then  $J \circ H$  is an isomorphism (under reasonable assumptions about the algebra of messages). Thus, these *node-injective* homomorphisms  $H: \mathbb{A} \rightarrow_{ni} \mathbb{B}$  determine a partial order  $\leq_{ni}$  on skeletons to within isomorphism.

**Lemma 1 ([18, Lemma 3.11]).**  $\leq_{ni}$  is a well-founded partial order. Indeed, for every  $\mathbb{B}$ , there are only finitely many non-isomorphic  $\mathbb{A}$  such that  $\mathbb{A} \leq_{ni} \mathbb{B}$ .

**Protocol analysis: A search through  $\rightarrow$ .** Protocol analysis is a search through part of the preorder  $\rightarrow$ . Skeletons  $\mathbb{A}_0$  determine starting points for the search; protocol analysis then seeks realized skeletons  $\mathbb{C}$  such that  $\mathbb{A} \rightarrow \mathbb{C}$ . CPSA computes a set of representative realized skeletons we call *shapes*. Within the set of all realized  $\mathbb{B}$  such that  $\mathbb{A} \rightarrow \mathbb{B}$ , the shapes are the *minimal* ones in the node-injective ordering  $\leq_{ni}$  [13]. CPSA’s test-and-solution steps form a labeled transition system, where  $\mathbb{A}_0 \xrightarrow{\ell} \mathbb{A}_1$  means that  $\mathbb{A}_0$  has an unsolved test described by the label  $\ell$ , and  $\mathbb{A}_1$  contains one solution to this test. Figs. 3 and 4 give examples of test-and-solution steps. The LTS  $\rightsquigarrow$  is a subrelation of  $\rightarrow$ .

Indeed, most of the search process works in the partial order  $\leq_{ni}$ . Although CPSA’s implementation is somewhat different, its search could be separated into two phases. After an initial non-node-injective step, all of its test-solving could take place in the node-injective ordering (see [18, Thm. 6.5]).

**Core Idea of this Paper.** If  $F: \Pi_1 \mapsto \Pi_2$ , the portion of the LTS for  $\Pi_1$  accessible from  $\mathbb{A}_0$  may *simulate* the portion of the LTS for  $\Pi_2$  accessible from the  $\Pi_2$  skeleton  $F(\mathbb{A}_0)$ . Since the labels on the two transition systems may differ, in finding the successful simulation, we freely choose a *relabeling function*  $\Delta$  mapping  $\Pi_1$  labels to  $\Pi_2$  labels. A simulation using  $\Delta$  *progresses* iff, whenever a  $\Pi_1$  skeleton  $\mathbb{A}$  can take some  $\ell$ -transition, the  $\Pi_2$  skeleton  $F(\mathbb{A})$  can take some  $\Delta(\ell)$  transition. If for some  $\Delta$ , we have a simulation that progresses, then  $F$  preserves all security goals concerning the starting situation  $\mathbb{A}_0$ .

We axiomatize the crucial properties of test-and-solution LTSS, rather than defining one as a function of  $\Pi$ . This has two advantages. First, we can establish goal preservation using finite, often very small, LTSS. Second, particularly for  $\Pi_2$ , we can use a finer LTS (as in Fig. 4) or a coarser one than CPSA would generate.

**Definition 3.** Let  $S$  be a set of skeletons, and  $\text{dead} \in \Lambda$ . A ternary relation  $\cdot \rightsquigarrow \cdot \subseteq S \times \Lambda \times S$  is a test-and-solution lts or TLTS for  $S, \Lambda$  iff:

1. If  $\mathbb{A} \in S$ , then: there exists a  $\mathbb{B}$  such that  $\mathbb{A} \rightsquigarrow \mathbb{B}$  iff  $\mathbb{A}$  is not realized;
2. If  $\mathbb{A} \xrightarrow{\ell} \mathbb{B}$ , then:
  - (a) If  $\ell = \text{dead}$ , then  $\mathbb{A} = \mathbb{B}$  and there is no realized  $\mathbb{C}$  such that  $\mathbb{A} \rightarrow \mathbb{C}$ ;
  - (b) If  $\ell \neq \text{dead}$ , then  $\mathbb{A} \leq_{ni} \mathbb{B}$  and  $\mathbb{B} \not\leq_{ni} \mathbb{A}$ ;



- (c) For every homomorphism  $J: \mathbb{A} \rightarrow \mathbb{C}$  from  $\mathbb{A}$  to a realized  $\mathbb{C}$ , there exists some  $\mathbb{B}'$  such that  $\mathbb{A} \xrightarrow{\ell} \mathbb{B}'$ , and  $J = K \circ H$ , where  $\mathbb{A} \xrightarrow{H} \mathbb{B}' \xrightarrow{K} \mathbb{C}$ .

Let  $S(\rightsquigarrow) = \{\mathbb{A}: \exists \mathbb{B}. \mathbb{A} \rightsquigarrow \mathbb{B}\} \cup \{\mathbb{B}: \exists \mathbb{A}. \mathbb{A} \rightsquigarrow \mathbb{B}\}$ .

Our TLTSs have the finite image property, i.e.  $\{\mathbb{B}: \mathbb{A} \xrightarrow{\ell} \mathbb{B}\}$  is finite for all  $\mathbb{A}, \ell$ . The non-dead labels in our applications are triples  $c, E, n_1$ , where  $c$  is a value received in a new, unexplained form in the node  $n_1$ . “Unexplained” because in  $n_1$   $c$  is not contained within a set of encryptions  $E$ . We call  $E$  an “escape set,” since  $c$  has escaped from the protection of the encryptions  $E$  before reaching  $n_1$ .

In Fig. 3,  $c$  is the nonce  $N$ .  $E$  is the singleton set  $\{\{N\}_{\text{pk}(B)}\}$ , which is the one form in which  $N$  has been seen. The node  $n_1$  is the lower (reception) node of  $\mathbb{A}_0$ , in which  $N$  is suddenly received outside of its encrypted form in  $E$ .

For both steps in Fig. 4,  $c$  is the nonce  $Y_1$ , and  $E$  is the singleton set  $\{\{Q_1 \wedge Y_1 \wedge N_1\}_{\text{pk}(B_1)}\}$ , which is the one form in which  $N_b$  has been seen prior to the test nodes  $n_1$ . In the first step, the test node  $n_1$  is the lower (reception) node of  $\mathbb{B}_0$ , in which  $Y_1$  is suddenly received outside of its encrypted form in  $E$ . In the second step, the test node  $n_1$  is the upper right (reception) node in  $\mathbb{B}_1$ , in which  $Y_1$  is received packaged with the (possibly distinct) values  $Q_3, N_3$ . The protocol provides no way to perform this repackaging if  $Q_3 \neq Q_1$  or  $N_3 \neq N_1$ , so the only possible explanation is to equate them. Non-singleton  $E$ s arise naturally in protocols that use a nonce repeatedly, for successive authentication steps.

**Lemma 2.** *Suppose that  $\cdot \rightsquigarrow \cdot$  is a TLTS, and  $\mathbb{A} \in S(\rightsquigarrow)$ . If  $\mathbb{A} \rightarrow_{ni} \mathbb{C}$  where  $\mathbb{C}$  is realized, then there exists a realized  $\mathbb{B}$  such that  $\mathbb{A} \rightsquigarrow * \mathbb{B}$  and  $\mathbb{B} \rightarrow_{ni} \mathbb{C}$ .*

This lemma is an instance of Thm. 1, and can be proved by specializing its proof.

**Homomorphisms and Transformations.** Homomorphisms are preserved by protocol transformations (Def. 2). Writing  $\text{Skel}(\Pi_i)$  for the set of skeletons over  $\Pi_i$ ,  $F: \Pi_1 \rightarrow \Pi_2$  determines an *image* operation  $\text{Skel}(\Pi_1) \rightarrow \text{Skel}(\Pi_2)$ . The *image* operation supplies new values for  $\Pi_2$  role parameters that do not appear in their  $\Pi_1$  preimages, using some convention. We write  $F(\mathbb{A})$  for  $\mathbb{A}$ ’s image.

**Lemma 3 ([17]).** *Suppose that  $F: \Pi_1 \rightarrow \Pi_2$  is a protocol transformation.*

1. *If  $H: \mathbb{A} \rightarrow \mathbb{B}$ , for  $\mathbb{A}, \mathbb{B} \in \text{Skel}(\Pi_1)$ , there is a unique  $F(H): F(\mathbb{A}) \rightarrow F(\mathbb{B})$  that commutes with the image operation.*
2. *If  $G: F(\mathbb{A}) \rightarrow F(\mathbb{B})$  is any homomorphism between skeletons of this form, then  $G = F(H)$  for some  $H: \mathbb{A} \rightarrow \mathbb{B}$ .*
3. *If  $\mathbb{D} \in \text{Skel}(\Pi_2)$ , then  $\{\mathbb{A}: F(\mathbb{A}) \leq_{ni} \mathbb{D}\}$  has a  $\leq_{ni}$ -maximum in  $\text{Skel}(\Pi_1)$ .*

## 5 The Preservation Theorem

Preserving protocol goals is about TLTSs for the two protocols. Assume a relabeling function  $\Delta: \Lambda(\Pi_1) \rightarrow \Lambda(\Pi_2)$ . The  $\text{Skel}(\Pi_1)$  argument determines what parameters in  $\mathbb{A}$  to avoid, when choosing new role parameters.

- Definition 4.** 1.  $F, \Delta$  preserve progress for  $\rightsquigarrow_1$  and  $\rightsquigarrow_2$  iff: (a)  $\ell = \text{dead}$  iff  $\Delta(\ell) = \text{dead}$ , and (b) for every  $\ell \in \Lambda$ ,  $\mathbb{A} \rightsquigarrow_1^\ell$  implies  $F(\mathbb{A}) \rightsquigarrow_2^{\Delta(\ell)}$ .
2. Lts  $\rightsquigarrow_1$  simulates  $\rightsquigarrow_2$  under  $F, \Delta$  iff: whenever  $F(\mathbb{A}) \rightsquigarrow_2^{\ell'} \mathbb{B}'$  and  $\ell' = \Delta(\ell)$ , then there exists a  $\mathbb{B}$  s.t.  $\mathbb{B}' = F(\mathbb{B})$  and  $\mathbb{A} \rightsquigarrow_1^\ell \mathbb{B}$ .

If  $F, \Delta$  preserve progress,  $\mathbb{A} \in S(\rightsquigarrow_1)$  implies  $F(\mathbb{A}) \in S(\rightsquigarrow_2)$ . There may be many  $\ell' \in \Lambda(\Pi_2)$  outside  $\text{ran}(\Delta)$ , for instance the second step in Fig. 4. In  $F_1, F_2$ ,  $\Delta$  is determined directly from  $F_i$ ; in other cases,  $\Delta(\ell)$  can use a larger escape set  $E$  than the naïve choice suggested by  $F$ .

**Theorem 1** Let  $F: \Pi_1 \rightarrow \Pi_2$ , and  $\Delta: \Lambda(\Pi_1) \rightarrow \Lambda(\Pi_2)$ . Let  $\rightsquigarrow_1$  and  $\rightsquigarrow_2$  be TLTSS with  $\mathbb{A} \in S(\rightsquigarrow_1) \subseteq \text{Skel}(\Pi_1)$  and  $S(\rightsquigarrow_2) \subseteq \text{Skel}(\Pi_2)$ . Suppose that:

1.  $F, \Delta$  preserve progress for  $\rightsquigarrow_1$  and  $\rightsquigarrow_2$ ;
2.  $\rightsquigarrow_1$  simulates  $\rightsquigarrow_2$  under  $F, \Delta$ .

For every  $\Pi_2$ -realized  $\mathbb{C}$ , if  $H: F(\mathbb{A}) \rightarrow_{ni} \mathbb{C}$ , there is a  $\Pi_1$ -realized  $\mathbb{B}$  such that  $\mathbb{A} \rightsquigarrow_1 * \mathbb{B}$ , and the accompanying diagram commutes.

$$\begin{array}{ccc}
 & & H \\
 & \curvearrowright & \\
 F(\mathbb{A}) & \xrightarrow{K} & F(\mathbb{B}) \xrightarrow{J} \mathbb{C} \\
 \vdots & & \vdots \\
 \mathbb{A} & \rightsquigarrow & \mathbb{B}
 \end{array}$$

*Proof.* We use induction on the set  $\{\mathbb{D}: F(\mathbb{A}) \leq_{ni} \mathbb{D} \leq_{ni} \mathbb{C}\}$ , since by Lemma 1, there are only finitely many non-isomorphic  $\mathbb{D} \leq_{ni} \mathbb{C}$ , and thus only finitely many s.t.  $F(\mathbb{A}) \leq_{ni} \mathbb{D} \leq_{ni} \mathbb{C}$ .

**$\mathbb{A}$  dead:** If  $\mathbb{A} \rightsquigarrow_1^{\text{dead}}$ , then by progress,  $F(\mathbb{A}) \rightsquigarrow_2^{\text{dead}}$  contrary to Def. 3, Clause 2a.

**$\mathbb{A}$  realized:** If  $\mathbb{A}$  is realized, it is the desired  $\mathbb{B}$ , with  $K = \text{Id}_{F(\mathbb{A})}$  and  $J = H$ .

**Otherwise,** for some  $\ell \neq \text{dead}$ ,  $\mathbb{A} \rightsquigarrow_1^\ell$ . By progress,  $F(\mathbb{A}) \rightsquigarrow_2^{\Delta(\ell)}$ . By Def. 3, Cl. 2c,  $H$  factors through some member of  $\{\mathbb{E}: F(\mathbb{A}) \rightsquigarrow_2^{\Delta(\ell)} \mathbb{E}\}$ , say  $\mathbb{E}_0$ . By simulation,  $\mathbb{E}_0 = F(\mathbb{A}')$  for some  $\mathbb{A}'$  with  $\mathbb{A} \rightsquigarrow_1^\ell \mathbb{A}'$ . By Defn. 3, Cl. 2b,  $F(\mathbb{A}) \leq_{ni} F(\mathbb{A}')$  but  $F(\mathbb{A}') \not\leq_{ni} F(\mathbb{A})$ .

Hence, the following proper inclusion eliminates an isomorphism class:

$$\{\mathbb{D}: F(\mathbb{A}') \leq_{ni} \mathbb{D} \leq_{ni} \mathbb{C}\} \subsetneq \{\mathbb{D}: F(\mathbb{A}) \leq_{ni} \mathbb{D} \leq_{ni} \mathbb{C}\};$$

i.e. the cardinality (modulo isomorphism) is reduced. Thus, we can apply the induction hypothesis to  $\mathbb{A}'$  in place of  $\mathbb{A}$ .  $\square$

Lemma 2 is the special case of Thm. 1 in which  $F, \Delta$  are the identity functions.

Although Thm. 1 is not about logical formulas, it has a corollary about security goal formulas for  $\Pi_1$ . If the  $\Pi_2$ -realized  $\mathbb{C}$  is a *counterexample* to a  $\Pi_1$  goal formula, then the  $\Pi_1$ -realized  $\mathbb{B}$  will also be a counterexample to that goal.

## 6 The Language $\mathcal{L}(\Pi)$ of a Protocol $\Pi$

$\mathcal{L}(\Pi)$  is a classical first order language with equality [16].<sup>1</sup> A formula

$$\forall \bar{x}. (\phi \supset \exists \bar{y}. \psi_1 \vee \dots \vee \psi_j) \tag{1}$$

<sup>1</sup> Although the syntax is simplified from [16],  $\mathcal{L}(\Pi)$ 's expressiveness is unchanged.

is a *security goal* if (i)  $\phi$  and each  $\psi_i$  is a conjunction of atomic formulas, (ii)  $\bar{x}$  and  $\bar{y}$  are disjoint lists of variables, and (iii) all variables free in any  $\psi_i$  but not in  $\phi$  is free in  $\bar{y}$ . Null and unary disjunctions ( $j = 0$  or  $j = 1$ ) are permitted, where the null disjunction  $\perp$  is the constantly false formula.

Since  $\mathcal{L}(II)$  says nothing about the structure of  $II$ 's messages, it can express goals that are preserved when message structure is transformed. It describes nodes by their role, their index along the role, and the role's parameters.

$\mathcal{L}(II)$  contains function symbols  $\text{pk}(a)$ ,  $\text{sk}(a)$ , and  $\text{inv}(a)$ , for  $a$ 's public encryption key;  $a$ 's private signature key; and the inverse member of a key pair.

**Example 1:  $\mathcal{L}(\text{HD})$ .**  $\mathcal{L}(\text{HD})$  shares some vocabulary with the other  $\mathcal{L}(II)$ :

$$\text{Prec}(m, n) \quad \text{Unq}(v) \quad \text{UnqAt}(n, v) \quad \text{Non}(v)$$

expressing node precedence; unique origination of  $v$ ; unique origination of  $v$  at the node  $n$ ; and non-origination of  $v$ . Its protocol-specific relations are:

$$\begin{array}{ccccc} \text{AtPos1}(s, n) & \text{AtPos2}(s, n) & \text{Init}(s) & \text{Resp}(s) & \text{Lsn}(s) \\ \text{Peer}(s, b) & \text{Self}(s, b) & \text{Nonce}(s, v) & \text{Hear}(s, v) & \end{array}$$

The predicates  $\text{AtPos1}$  and  $\text{AtPos2}$  say that a node  $n$  lies at the first or second position (resp.) on strand  $s$ .  $\text{Init}$  and  $\text{Resp}$  say that a strand  $s$  is an initiator or responder strand (resp.).  $\text{Lsn}(s)$  says that  $s$  is a listener strand, a purely receptive strand that can witness that a value is disclosed.  $\text{Peer}$  says that  $s$ 's name parameter is  $b$ , if  $s$  is an initiator strand. This name refers to  $s$ 's intended partner.  $\text{Self}$  says that  $s$ 's name parameter is  $b$ , if  $s$  is a responder strand. This name refers to the active party in this strand, the owner of the decryption key. We use  $\text{Nonce}$  to say that  $v$  is the nonce in either type of strand  $s$ .  $\text{Hear}$  says that  $s$  has received the value  $v$ , if  $s$  is a listener strand. The skeleton  $\mathbb{A}_0$  of Fig. 3 satisfies the formula  $\Phi_0 =$

$$\begin{aligned} & \text{Init}(s) \wedge \text{AtPos1}(s, n) \wedge \text{AtPos2}(s, m) \wedge \text{Peer}(s, b) \\ & \wedge \text{Nonce}(s, v) \wedge \text{Non}(\text{inv}(\text{pk}(b))) \wedge \text{UnqAt}(n, v), \end{aligned}$$

when we assign  $s$  to the initiator strand shown; assign  $n$  and  $m$  to its first and second nodes resp.; assign  $b$  to the name  $B$ ; and assign  $v$  to nonce  $N$ . If  $\Phi_1 =$

$$\begin{aligned} & \text{Resp}(s') \wedge \text{AtPos1}(s', n') \wedge \text{AtPos2}(s', m') \wedge \text{Self}(s', b) \\ & \wedge \text{Nonce}(s', v) \wedge \text{Prec}(n, n') \wedge \text{Prec}(m', m), \end{aligned}$$

then  $\mathbb{A}_1$  satisfies  $\Phi_0 \wedge \Phi_1$ , when we (additionally) assign  $s'$  to the responder strand shown, and  $n', m'$  to its first and second nodes resp. The variables  $b, v$  are *not* primed in  $\Phi_1$ , expressing the agreement of the initiator and responder strands on these parameters. So  $\Phi_0 \supset \Phi_1$  is an authentication goal.

Although HD does not achieve any confidentiality goal, we would express it with a null conclusion, and with the  $\text{Lsn}$  and  $\text{Hear}$  predicates in the hypothesis. Letting  $\perp$  be the vacuously false null disjunction:

$$\begin{aligned} & (\text{Init}(s) \wedge \text{AtPos1}(s, n) \wedge \text{Peer}(s, b) \\ & \text{Nonce}(s, v) \wedge \text{Non}(\text{inv}(\text{pk}(b))) \wedge \text{UnqAt}(n, v) \\ & \text{Lsn}(s') \wedge \text{AtPos1}(s', n') \wedge \text{Hear}(n', b)) \supset \perp \end{aligned}$$

would express the secrecy of  $b$ .

**$\mathcal{L}(\Pi)$  in General.** In the previous paragraphs, we created an intuitive relation between a particular protocol  $\Pi$  and the predicates of its language. To do the same thing more generally, we will use a table  $\tau$ .

The table  $\tau$  should associate a distinct one place predicate with each role. For HD,  $\tau$  mapped the initiator role to the **Init** predicate and the responder role to **Resp**. These are the *role predicates*. We also have  $\tau$  associate each pair of a role and parameter of that role to a two place predicate. For HD,  $\tau$  mapped the initiator role and the parameter  $N$  to the predicate **Nonce**; it also maps the responder role and  $N'$  to **Nonce**. These are the *parameter predicates*. We require (i) role predicates and parameter predicates are disjoint, and (ii)  $\tau$  maps different parameters of the same role to different parameter predicates. For precision, we could write  $\mathcal{L}_\tau(\Pi)$  for the language determined by a particular choice of  $\tau$ , but the choice of  $\tau$  makes no semantically relevant difference in security goals.

We add  $k$  position predicates **AtPos1**( $s, n$ ),  $\dots$ , **AtPosk**( $s, n$ ), where  $k$  is the length of the longest role in  $\Pi$ .  $\mathcal{L}(\Pi)$  contains these position predicates, the shared predicates **Prec**, **Unq**, **UnqAt**, **Non**, and the predicates in the range of  $\tau$ .

**Classical Semantics of  $\mathcal{L}(\Pi)$ .** Fix a message algebra  $\mathfrak{M}$ . Each skeleton  $\mathbb{A}$  for  $\Pi$  determines a model for  $\mathcal{L}(\Pi)$  where the domain contains the messages in  $\mathfrak{M}$  together with the strands and nodes of  $\mathbb{A}$ . Given an assignment  $\eta$  mapping free variables to values in the domain, the value  $\eta(v)$  of any term  $v$ , involving variables and functions symbols such as **pk**, etc., is determined by  $\eta$  and  $\mathfrak{M}$ . The satisfaction conditions for the predicates are:

$$\begin{aligned}
\mathbb{A} \models_\eta \mathbf{Prec}(n, n') & \quad \text{iff } \eta(n) \prec_{\mathbb{A}} \eta(n'); \\
\mathbb{A} \models_\eta \mathbf{Non}(v) & \quad \text{iff } \eta(v) \in \mathbf{non}_{\mathbb{A}}; \\
\mathbb{A} \models_\eta \mathbf{Uniq}(v) & \quad \text{iff } \eta(v) \in \mathbf{unique}_{\mathbb{A}}; \\
\mathbb{A} \models_\eta \mathbf{UniqAt}(n, a) & \quad \text{iff } \eta(v) \in \mathbf{unique}_{\mathbb{A}} \text{ and } \eta(v) \text{ originates at } \eta(n) \text{ in } \mathbb{A}; \\
\mathbb{A} \models_\eta \mathbf{AtPosk}(s, n) & \quad \text{iff } \eta(n) \in \mathbf{nodes}_{\mathbb{A}} \text{ and } \eta(n) = \eta(s) \downarrow k; \\
\mathbb{A} \models_\eta \mathbf{RolePred}(s) & \quad \text{iff for some } j > 0, \mathbf{nodes}_{\mathbb{A}} \text{ contains exactly } j \text{ nodes of } \eta(s), \\
& \quad \text{and } \eta(s) \in \mathbf{instances}(\rho|_j), \text{ where } \tau(\rho) \text{ is } \mathbf{RolePred}; \\
\mathbb{A} \models_\eta \mathbf{ParamPred}(s, v) & \quad \text{iff for some } j > 0, \mathbf{nodes}_{\mathbb{A}} \text{ contains exactly } j \text{ nodes of} \\
& \quad \eta(s), \text{ and } \eta(s) \in \mathbf{instances}(\rho|_j), \text{ and for every } \mathbf{instances}(\rho|_j)\text{-witness } \alpha(\rho) \text{ for} \\
& \quad \eta(s) \text{ has } \alpha(a) = \eta(v), \text{ where } \tau(\rho, a) \text{ is } \mathbf{ParamPred}.
\end{aligned}$$

The definition ensures that  $\mathbb{A} \models_\eta \phi[s]$  is never sensitive to the part of  $\eta(s)$  outside  $\mathbb{A}$ . As in Def. 2, Clause 5,  $\mathcal{L}(\Pi)$  is insensitive to not-yet-executed branch points.

This definition also justifies our claims about  $\Phi_0$  and  $\Phi_0 \wedge \Phi_1$  above.  $\Phi_0$  is satisfied in both  $\mathbb{A}_0$  and  $\mathbb{A}_1$ . Indeed, because  $\Phi_0$  is a conjunction of atoms, it will be satisfied in *every* homomorphic image of  $\mathbb{A}_0$ . Specifically, if  $H: \mathbb{A}_0 \rightarrow \mathbb{C}$ , then composing  $H$  with the variable assignment  $\eta$ , we have  $\mathbb{C} \models_{H \circ \eta} \Phi_0$ . Moreover, this is exact: If  $\mathbb{C} \models_\theta \Phi_0$ , then for some  $H: \mathbb{A}_0 \rightarrow \mathbb{C}$ ,  $\theta = H \circ \eta$ .

**Definition 5.**  $\mathbb{A}, \eta$  is a  $\Phi$ -characteristic pair iff (i)  $\mathbb{A} \models_\eta \Phi$  and (ii), for all  $\mathbb{B}, \theta$ , if  $\mathbb{B} \models_\theta \Phi$  implies  $\exists! H. H: \mathbb{A} \rightarrow \mathbb{B}$  and for all  $x \in \mathbf{fv}(\Phi)$ ,  $\theta(x) = (H \circ \eta)(x)$ .

$\mathbb{A}$  is a  $\Phi$ -characteristic skeleton iff some  $\mathbb{A}, \eta$  is a  $\Phi$ -characteristic pair.

We write  $\mathbb{A}, \eta = \text{cp}(\Phi)$  for the characteristic pair and  $\mathbb{A} = \text{cs}(\Phi)$  for the characteristic skeleton, when they exist, since they are unique to within isomorphism.  $\mathbb{A}_0$  is the characteristic skeleton of  $\Phi_0$ , i.e.  $\mathbb{A}_0 = \text{cs}(\Phi_0)$ , and  $\mathbb{A}_1 = \text{cs}(\Phi_0 \wedge \Phi_1)$ . In Fig. 3, since every  $H: \mathbb{A}_0 \rightarrow \mathbb{C}$  to a realized skeleton factors through  $\mathbb{A}_0 \rightsquigarrow \mathbb{A}_1$ , we have demonstrated the goal  $\Gamma_1 =$

$$\forall s, n, m, b, v. (\Phi_0 \supset \exists s', n', m'. \Phi_1). \quad (2)$$

**Role-Specific Formulas.** A variable  $s$  appearing in a role predicate in  $\phi$ , or as the first argument to a position predicate or a role parameter predicate, is called a *strand variable* in  $\phi$ . A variable  $n$  appearing as the second argument to a role position predicate, or either argument to an order predicate, or the first argument to an **UnqAt** predicate, is called a *node variable*.

A conjunction of atoms  $\phi$  is *role specific* if strand and node variables are disjoint; every strand variable appears in exactly one role predicate; and every node variable appears in exactly one position predicate.  $\Phi_0$  and  $\Phi_0 \wedge \Phi_1$  are role specific, but  $\Phi_1$  alone is not. Node variables  $m, n$  occur in no position predicate in  $\Phi_1$ . By associativity and commutativity, a role specific  $\phi$  can be rewritten so every leftmost subformula is role specific. That is,  $\phi$  is equivalent to  $\phi_0 \wedge \psi_1$  where  $\phi_0$  is role specific, and if  $\phi_0$  is a conjunction  $\phi_1 \wedge \psi_1$ , then  $\phi_1$  satisfies the same property recursively. This holds because the role predicate for  $s$  can precede position and parameter predicates for it, and the position predicate for  $n$  can precede **Pred** and **UnqAt** predicates for it. As in [16, Thm. 5.2]:

**Lemma 4.** *If  $\phi$  is role specific, the characteristic skeleton  $\text{cs}(\phi)$  is defined.*

If  $\Gamma$  is a goal formula as in Eqn. (1), then we say that  $\Gamma$  is role specific if  $\phi$  is, and each of the conjunctions  $\phi \wedge \psi_i$  is, where  $1 \leq i \leq j$ .

**Example 2:  $\mathcal{L}(\text{YN})$ .** The language  $\mathcal{L}(\text{YN})$ , like  $\mathcal{L}(\text{HD})$ , has the position predicates **AtPos1**( $s, n$ ) and **AtPos2**( $s, n$ ). It has five role predicates, namely **QAf**( $s$ ), **QNg**( $s$ ), **AnAf**( $s$ ), **AnNg**( $s$ ), and **Lsn**( $s$ ). Again expressing an intended peer via **Peer**( $s, b$ ), and an actual identity via **Self**( $s, b$ ), we have five parameter predicates:

$$\text{Quest}(s, q), \text{YesVal}(s, v), \text{NoVal}(s, v), \text{Peer}(s, b), \text{Self}(s, b).$$

**Protocol Transformations and Language Translations.** Each  $F: \Pi_1 \rightarrow \Pi_2$  determines a translation  $\text{Tr}_F(\cdot)$  between role specific goal formulas of  $\mathcal{L}(\Pi_1)$  and  $\mathcal{L}(\Pi_2)$ . We translate conjunctions by translating each conjunct. Let  $F(\rho_1) = (\rho_2, g)$ . The order and assumption predicates are translated verbatim. For the remaining predicates, we use the tables  $\tau_1$  and  $\tau_2$ .

**RolePred1**( $s$ ): If **RolePred1** is  $\tau_1(\rho_1)$ , translate it to  $\tau_2(\rho_2)$ .

**PosPredi**( $s, n$ ): Because the formula is role specific, there is a single conjunct **RolePred1**( $s$ ) with the same  $s$ . If **RolePred1** is  $\tau_1(\rho_1)$ , then letting the index  $j = g(i)$ , the result is **PosPredj**( $s, n$ ).

**ParamName1**( $s, t$ ): Again, there is a single conjunct **RolePred1**( $s$ ) with this  $s$ , by role specificity. Let **RolePred1** be  $\tau_1(\rho_1)$ , and **ParamName1** be  $\tau_1(\rho_1, a)$ . Select the predicate **ParamName2** to be  $\tau_2(\rho_2, a)$ . If either (i)  $a$  does not appear in  $\rho_2$ , or (ii) for all parameters  $a$  of  $\rho_1$ , **ParamName1** is not  $\tau_1(\rho_1, a)$ , then the result is vacuously true:  $s = s \wedge t = t$ .

If  $\phi \wedge \psi_i$  is role specific,  $Tr_F^\phi(\psi)$  translates  $\psi_i$  the same way, using conjuncts of  $\phi$  to provide the specification of the roles. We have ensured that  $\text{fv}(Tr_F(\phi)) = \text{fv}(\phi)$  and  $\text{fv}(Tr_F^\phi(\psi)) = \text{fv}(\psi)$ . So, let  $Tr_F(\forall \bar{x}. (\phi \supset \exists \bar{y}. \psi_1 \vee \dots \vee \psi_k))$  be

$$\forall \bar{x}. (Tr_F(\phi) \supset \exists \bar{y}. Tr_F^\phi(\psi_1) \vee \dots \vee Tr_F^\phi(\psi_k)). \quad (3)$$

For the goal formula  $\Gamma_1$  describing Fig. 3,  $Tr_{F_1}(\Gamma_1)$  is:

$$\begin{aligned} \forall s, n, m, b, v. & (\text{QAf}(s) \wedge \text{AtPos1}(s, n) \wedge \text{AtPos2}(s, m) \wedge \text{Peer}(s, b) \\ & \wedge \text{Non}(\text{inv}(\text{pk}(b))) \wedge \text{YesVal}(s, v) \wedge \text{UnqAt}(n, v) \\ \supset \exists s', n', m'. & \text{AnAf}(s') \wedge \text{AtPos1}(s', n') \wedge \text{AtPos2}(s', m') \wedge \text{Self}(s', b) \\ & \wedge \text{YesVal}(s', v) \wedge \text{Prec}(n, n') \wedge \text{Prec}(m', m)). \end{aligned}$$

If  $\eta$  is an variable assignment taking values in  $\mathbb{A}$ , define  $\bar{\eta}$  to be the corresponding assignment taking values in  $F(\mathbb{A})$ . In particular,  $\bar{\eta}$  agrees with  $\eta$  for variables whose value is a message. For variables whose value is a strand or node, we have  $\bar{\eta}(v) = F(\eta(v))$ , so that  $\bar{\eta}$  is the composition of  $\eta$  with the “image” map from  $\mathbb{A}$  to  $F(\mathbb{A})$ .

- Lemma 5.** 1. If  $\mathbb{A} \models_\eta \phi$ , then  $F(\mathbb{A}) \models_{\bar{\eta}} Tr_F(\phi)$ .  
2. If  $\mathbb{A} \models_\eta \phi \wedge \psi$ , then  $F(\mathbb{A}) \models_{\bar{\eta}} Tr_F^\phi(\psi)$ .  
3. If  $\mathbb{B} \models_\theta Tr_F(\phi)$  and  $\text{cp}(\phi) = \mathbb{A}, \eta$ , then there exists a  $J$  such that  $J: F(\text{cs}(\phi)) \rightarrow \mathbb{B}$ , and  $\theta$  agrees with  $J \circ \bar{\eta}$  on  $\text{fv}(\phi)$ .  
4. If  $\phi$  is role specific, then  $\text{cs}(Tr_F(\phi))$  exists, and  $F(\text{cs}(\phi)) = \text{cs}(Tr_F(\phi))$ .

*Proof.* **1.** We left-associate conjunctions, so that when  $\phi$  is  $\phi_1 \wedge \phi_2$ ,  $\phi_2$  is atomic. We also assume that  $\phi$  is written in the order defined before Lemma 4, so every leftmost subformula of  $\phi$  is also role specific. We use structural induction on  $\phi$ . *Base case:* If  $\phi$  is the trivially true conjunction with 0 conjuncts, then  $Tr_F(\phi)$  is also the null conjunction, which is true in every structure.

*Induction step:* Let  $\phi$  be  $\phi_1 \wedge \phi_2$ , where the claim holds for  $\phi_1$ , and  $\phi_2$  is atomic. When  $\phi_2$  uses **Prec**, **Unq**, **UnqAt**, **Non**, or  $=$ , the claim follows from the definitions.

If  $\phi_2$  is a role predicate **RoleName**( $s$ ),  $\eta(s)$  is a strand with at least one node in  $\mathbb{A}$ , and all of its nodes in  $\mathbb{A}$  agree with an initial segment of an instance of the associated role  $\rho_1$ . Thus, its  $F$ -image in  $F(\mathbb{A})$  has at least  $g(1)$  nodes in  $\mathbb{A}$  and all of its nodes in  $\mathbb{A}$  agree with an initial segment of an instance of the corresponding role  $\rho_2$ . Hence  $F(\mathbb{A}) \models_{\bar{\eta}} Tr_F(\phi_2)$ . Position predicates are similar.

Let  $\phi_2$  be a parameter predicate **ParamName**( $s, t$ ). Since  $\phi$  is role specific, there is just one **RoleName**( $s$ ) with the same  $s$  in  $\phi_1$ , and  $\mathbb{A} \models_\eta \text{RoleName}(s)$ . Thus,  $Tr_F(\phi_2)$  is the  $F$ -corresponding parameter name predicate, and the  $F$ -image of  $\eta(s)$  has the same parameter  $\eta(t)$ . Hence,  $F(\mathbb{A}) \models_{\bar{\eta}} Tr_F(\phi_2)$ .

2.  $Tr_F(\phi \wedge \psi)$  entails  $Tr_F^\phi(\psi)$ , and Clause 1 implies  $F(\mathbb{A}) \models_{\bar{\eta}} Tr_F(\phi \wedge \psi)$ .

3. By Lemma 4,  $cs(\phi)$  exists. By the properties of  $cs$  [16], each strand with nodes in  $\mathbb{A}$  is  $\eta(s)$  for some distinct  $s$  in a role predicate in  $\phi$ . If  $\mathbb{A}$  contains  $i$  nodes of  $\eta(s)$ , then there is a node position predicate for  $i$ ,  $s$ , and some  $n$ . Moreover, each parameter to the associated role  $\rho$  takes an atom or indeterminate as its value in  $\eta(s)$ , not a concatenation or encryption.

We will construct a  $J: F(cs(\phi)) \rightarrow \mathbb{B}$ .  $J = [\phi, \alpha]$  is defined:  $\phi(\bar{\eta}(s)) = \theta(s)$ . If  $a$  is a parameter to  $\bar{\eta}(s)$ , then  $\alpha(a)$  is the corresponding parameter to  $\bar{\theta}(s)$ . By the universality of  $cs(\phi)$  and of  $F(\mathbb{A})$ ,  $J = [\phi, \alpha]$  is a homomorphism.

4. By the syntax,  $Tr_F(\phi)$  is role specific, so Lemma 4 implies  $cs(Tr_F(\phi))$  exists. By the previous clause,  $J: F(cs(\phi)) \rightarrow cs(Tr_F(\phi))$ .

By clause 1,  $F(cs(\phi)) \models_{\bar{\eta}} Tr_F(\phi)$ . Thus, Def. 5 entails that  $K: cs(Tr_F(\phi)) \rightarrow F(cs(\phi))$ . Hence, by the uniqueness in Def. 5,  $J \circ K = \text{Id}$ . Hence,  $F(cs(\phi))$  and  $cs(Tr_F(\phi))$  are isomorphic.  $\square$

## 7 Preserving Security Goal Formulas

$\Pi$  achieves a goal formula  $\Gamma$  iff, for all realized  $\Pi$ -skeletons  $\mathbb{C}$ ,  $\mathbb{C} \models \Gamma$ .

**Theorem 2** Let  $F: \Pi_1 \rightarrow \Pi_2$ , and let  $\phi$  be goal specific with  $\mathbb{A} = cs(\phi)$ .

Suppose  $\Pi_1$  achieves the goal  $\Gamma = \forall \bar{x}. (\phi \supset \exists \bar{y}. \psi_1 \vee \dots \vee \psi_j)$ , and assume there exists a  $\Delta$  and TLTSS  $\rightsquigarrow_1$  and  $\rightsquigarrow_2$  as in Thm. 1, i.e.  $\mathbb{A} \in S(\rightsquigarrow_1)$  and

1.  $F, \Delta$  preserve progress for  $\rightsquigarrow_1$  and  $\rightsquigarrow_2$ ;
2.  $\rightsquigarrow_1$  simulates  $\rightsquigarrow_2$  under  $F, \Delta$ .

Then  $\Pi_2$  achieves  $Tr_F(\Gamma)$ .

*Proof.*  $Tr_F(\Gamma)$  is  $\forall \bar{x}. (Tr_F(\phi) \supset \exists \bar{y}. Tr_F^\phi(\psi_1) \vee \dots \vee Tr_F^\phi(\psi_j))$ . Suppose that  $\mathbb{C}$  is any  $\Pi_2$ -realized skeleton and  $\theta$  is a variable assignment.

If  $\mathbb{C} \not\models_{\theta} Tr_F(\phi)$ , then  $\mathbb{C} \models_{\theta} Tr_F(\phi) \supset Tr_F^\phi(\psi_1) \vee \dots \vee Tr_F^\phi(\psi_j)$ .

So suppose  $\mathbb{C} \models_{\theta} Tr_F(\phi)$ . By Lemma 5, Clause 4,  $cp(Tr_F(\phi)) = F(\mathbb{A}), \bar{\eta}$ . By Def. 5, there exists  $H: F(\mathbb{A}) \rightarrow \mathbb{C}$ , and  $\theta \upharpoonright \bar{x} = (H \circ \bar{\eta}) \upharpoonright \bar{x}$ .

*Case 1.* Suppose that  $H$  is node-injective. By Thm. 1, there is a  $\Pi_1$ -realized  $\mathbb{B}$  such that  $\mathbb{A} \rightsquigarrow_1 * \mathbb{B}$  and, for some  $J, K$ ,  $F(\mathbb{A}) \xrightarrow{K}_{ni} F(\mathbb{B}) \xrightarrow{J}_{ni} \mathbb{C}$ . By Lemma 3, Clause 2,  $K = F(L)$  for some  $L: \mathbb{A} \rightarrow \mathbb{B}$ . Thus,  $\mathbb{B} \models_{L \circ \bar{\eta}} \phi$ .

Since, by assumption,  $\Pi_1$  achieves  $\Gamma$ , it follows that  $\mathbb{B} \models_{\zeta} \psi_i$ , for some  $\psi_i$  and some  $\zeta$  s.t.  $\zeta \upharpoonright \bar{x} = (L \circ \bar{\eta}) \upharpoonright \bar{x}$ . By Lemma 5, Clause 2, we can lift this to  $F(\mathbb{B})$ , so that  $F(\mathbb{B}) \models_{\bar{\zeta}} Tr_F^\phi(\psi_i)$ . Quantifying existentially,  $F(\mathbb{B}) \models_{F(L) \circ \bar{\zeta}} \exists \bar{y}. Tr_F^\phi(\psi_i)$ .

Applying  $J$  and using  $K = F(L)$ , we have  $\mathbb{C} \models_{J \circ (K \circ \bar{\zeta})} \exists \bar{y}. Tr_F^\phi(\psi_i)$ . Since  $J \circ K = H$  and  $\theta \upharpoonright \bar{x} = (H \circ \bar{\zeta}) \upharpoonright \bar{x}$ , we have  $\mathbb{C} \models_{\theta} \exists \bar{y}. Tr_F^\phi(\psi_i)$ .

*Case 2.*  $H$  is not node-injective. By [18, Thm. 6.5], there is a  $K_0: F(\mathbb{A}) \rightarrow \mathbb{D}$  that is universal among homomorphisms equating the nodes that  $H$  equates, and for some node-injective  $H_0$ ,  $H = H_0 \circ K_0$ . Apply Case 1 to  $H_0$  and  $\mathbb{D}$ .  $\square$

**Related Work** The safe protocol transformation problem is not new. As an idea for protocol design, it goes back at least to Bird et al. [5]. In a key special case, “protocol composition,” it dates from the 1990s [21, e.g.]. In the protocol composition case, roles of  $\Pi_1$  also appear unchanged as roles of  $\Pi_2$ . Since  $\Pi_2$  may also have additional roles not in the image of  $\Pi_1$ , composition is thus effectively the case in which  $\Pi_1 \subseteq \Pi_2$ . While there has been an extensive literature devoted to this special case, the more general type of transformation discussed here has seen very little progress. Our view is that the effects of a syntactic change in message structure on protocol behavior are very hard to predict (given an active adversary model). This has made it hard to reason about the full notion of transformation, as opposed to the special case of composition. We have introduced the TLTS as a representation of the protocol analysis problem to tame this complexity.

Focusing then on protocol composition, it has been very successfully treated in a *cryptographic* model. A strong form of composition is reactive simulatability [25, 3] or universal composability [7]; weaker forms may still be cryptographically justified [12].

In the *symbolic* model, we previously provided a widely applicable and practically useful criterion [19, 14]. Cortier et al.’s criterion is in some ways broader but in other ways narrower than ours [8]; cf. [1]. Our [15] covers the union of [19, 8, 1]. From one point of view, the contribution of the present paper is to generalize [15] beyond the composition case.

The Protocol Composition Logic PCL considers refinements that preserve security goals [11, Thms. 4.4, 4.8]. A specific proof of a goal formula relies on particular invariants. If a protocol refinement introduces no actions falsifying these invariants, it preserves the security goal. Although PCL was designed to support richer forms of transformation, the existing results are essentially confined to the composition case. [11]’s “parallel” and “sequential” composition amounts to  $\Pi_1 \subseteq \Pi_2$ . Datta et al.’s “protocol refinement using templates” [10] suggested many of our examples.

By contrast with Distributed Temporal Logic [6],  $\mathcal{L}(\Pi)$  is intended to be less expressive about the forms of messages. We wanted to focus only on what is retained under transformation, which concerns the role parameters rather than the forms of the messages. Nevertheless, our logic, unlike DTL, being a quantified logic, satisfaction is undecidable.

Lowe and Auty [23] refine protocols to concrete messages starting from formulas in a Hoare-like logic that represent the effect of messages. Maffei et al. [2] express the effects of messages by abstract tags, and provide constraints on instantiating the tags by concrete messages.

“Protocol compilers” transform their input automatically. Some start with a crypto-free protocol, and transform it into a protocol meeting security goals [9, 4]. Others transform a protocol secure in a weak adversary model into protocols satisfying those goals with multi-session, active adversary [20].

**Future work.** We leave a major gap: What syntactic property of  $F: \Pi_1 \rightarrow \Pi_2$  ensures that  $F$  preserves security goals? A clue comes from the “disjoint



encryption” property [19, 15], cf. [23, 8]. Consider a map  $E$  from all encrypted units used by  $\Pi_1$  to a subset of the encrypted units of  $\Pi_2$ .  $\Pi_2$  should create an encryption  $\alpha(E(e))$  on node  $n$  only if  $n = F(n_0)$  and  $n_0$  creates  $\alpha(e)$  in  $\Pi_1$ . Likewise,  $\Pi_2$  should remove an ingredient from  $\alpha(E(e))$  only on a node  $n = F(n_0)$  where  $n_0$  removes an ingredient from  $\alpha(e)$  in  $\Pi_1$ .

Tool support is also required. CPSA generates some TLTS transition relations. We then construct others, and the simulations, by hand. A variant of CPSA that would explore two protocols in tandem would be of great interest.

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