



CS 543 - Computer Graphics: Ray Tracing Detail, Part 4

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(with help from Emmanuel Agu ;-)



Reflection and Transparency

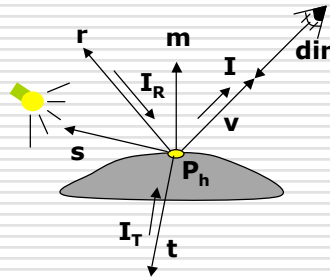
- Ray tracing also handles reflections and refraction of light well
- We can easily render realistic scenes with
 - mirrors
 - martini glasses
- So, far, we have considered **Local components** (ambient, diffuse, specular)
- Local components are contributions from light sources which are visible from hit point
- To render reflection, and refraction we need to add reflection and refraction components of light

$$I = I_{amb} + I_{diff} + I_{spec} + I_{refl} + I_{tran}$$

Reflection and Transparency

- First three components are local

$$I = I_{amb} + I_{diff} + I_{spec} + I_{refl} + I_{tran}$$



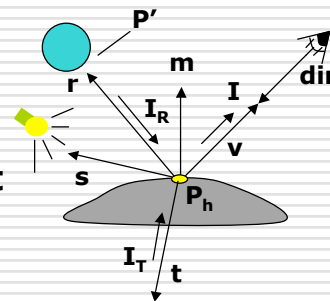
- Reflected component, I_R , is along mirror direction from eye $-\mathbf{r}$

Reflection and Transparency

- \mathbf{r} is given as (see eqn 4.22) as

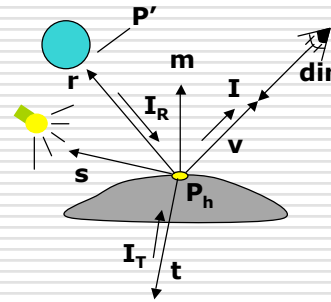
$$\mathbf{r} = \mathbf{dir} - 2(\mathbf{dir} \cdot \mathbf{m})\mathbf{m}$$

- Transmitted component I_T is along transmitted direction \mathbf{t}
- Portion of light coming in from direction \mathbf{t} is bent along \mathbf{dir}
- I_R and I_T each have their own five components (ambient, diffuse, etc)
- In some sense, point P' along reflected direction \mathbf{r} serves as a light source to point P_h



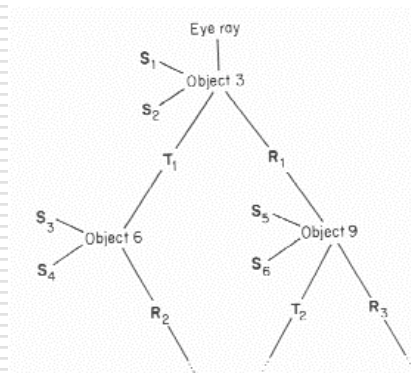
Reflection and Transparency

- To determine reflected component
 - Spawn reflected ray along direction \mathbf{r}
 - Determine closest object hit
- To determine transmitted component
 - Cast transmitted ray along direction \mathbf{t}
 - Determine closest object hit
- So, at each hit point, local, reflected and refracted components merge to form total contributions



Reflection and Transparency: WPI Ray Tree

- Local, reflected, transmitted and shadow rays form a tree



Reflection and Transparency

- ❑ Tree structure suggests recursion at successive hit points
- ❑ Recurse forever? No!!
- ❑ At each point, only fraction of impinging reflected or refracted ray is lost
- ❑ Who determines fraction? Designer... sets transparency or reflectivity in SDL file.
- ❑ E.g., reflectivity 0.8 means only 80% of impinging ray is reflected
- ❑ Thus, need to check reflected contribution by saying
if(reflectivity > 0.6)...
- ❑ Also check if(transparency > threshold)
- ❑ Basically, do not want to work hard for tiny contributions.
 - Drop (terminate shade) if contribution is too small.

Refraction and Transparency

- ❑ May also need to determine how many times you want to bounce (even if threshold is still high)
- ❑ For example, in room with many mirrors, do you want to bounce forever (your system may cry!!)
- ❑ Set **recurseLevel** (yup!! same as in shadows) to say how many bounces using (variable **maxRecursionLevel**)
- ❑ recurseLevel of 4 or 5 is usually enough to create realistic pictures
- ❑ Ray from eye to first hit point has recurseLevel of 0
- ❑ All rays from first hit point have recurseLevel = 1
- ❑ Need to modify shade function to handle recursion

Recursive shade () skeleton

```
Color3 Scene::shade( Ray& ) {
    Get the first hit, and build hitInfo h
    Shape* myObj = ( Shape* )h.hitObject; // ptr to hit obj
    Color3 color.set( the emissive component );
    color.add( ambient contribution );
    get normalized normal vector m at hit point
    for( each light source )
        add the diffuse and specular components
        // now add the reflected and transmitted components

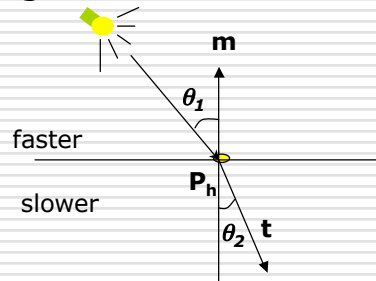
    if( r.recurseLevel == maxRecursionLevel )
        return color; // don't recurse further
}
```

Recursive shade () skeleton

```
if( hit object is shiny enough ) { // add reflected light
    get reflection direction
    build reflected ray, refl
    refl.recurseLevel = r.recurseLevel + 1;
    color.add( shininess * shade( refl ) );
}
if( hit object is transparent enough ) {
    get transmitted direction
    build transmitted ray, trans
    trans.recurseLevel = r.recurseLevel + 1;
    color.add( transparency * shade( trans ) );
}
return color;
}
```

Finding Transmitted Direction

- ❑ So far, found reflected ray direction as mirror direction from eye
- ❑ Transmitted direction obeys **Snell's law**
- ❑ Snell's law: relationship holds in the following diagram



$$\frac{\sin(\theta_2)}{c_2} = \frac{\sin(\theta_1)}{c_1}$$

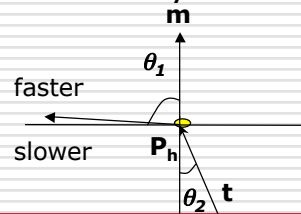
c_1, c_2 are speeds of light in medium 1 and 2

Finding Transmitted Direction

- ❑ If ray goes from faster to slower medium, ray is bent **towards** normal
- ❑ If ray goes from slower to faster medium, ray is bent **away** from normal
- ❑ c_1/c_2 is important
 - Usually measured for medium-to-vacuum. E.g., water to vacuum
- ❑ Some measured relative c_1/c_2 are:
 - Air: 99.97%
 - Glass: 52.2% to 59%
 - Water: 75.19%
 - Sapphire: 56.50%
 - Diamond: 41.33%

Critical Angle

- There exists transmitted angle at which ray in faster medium (e.g., air) is bent along object surface
- That angle (θ_2 in figure below) is known as the **critical angle**
- Increasing transmission angle beyond critical angle has “no effect”... transmitted ray still below object surface
- Physical significance:
 - Underwater in pond, can see world through small cone of angles

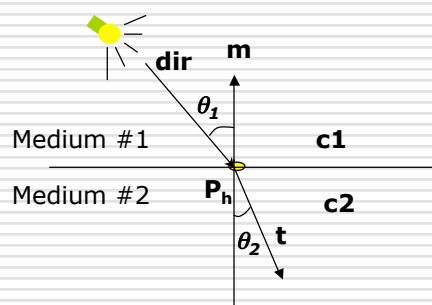


Transmission Angle

- Vector for transmission angle can be found as

$$\mathbf{t} = \frac{c_2}{c_1} \mathbf{dir} + \left(\frac{c_2}{c_1} (\mathbf{m} \cdot \mathbf{dir}) - \cos(\theta_2) \right) \mathbf{m}$$

where



$$\cos(\theta_2) = \sqrt{1 - \left(\frac{c_2}{c_1} \right)^2 (1 - (\mathbf{m} \cdot \mathbf{dir})^2)}$$

For Project 4

- May read up hit (intersection) functions for shapes, add to your ray tracer
 - Cube
 - Cylinder
 - Mesh, ... etc

References

- Hill, chapter 12