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# CS 543 - Computer Graphics: 2D Viewing, Part 2

by

Robert W. Lindeman

[gogo@wpi.edu](mailto:gogo@wpi.edu)

(with help from Emmanuel Agu ;-)

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# Window-to-Viewport Mapping

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- Zooming in on a portion of object
- Tiling
  - W-to-V in loop
  - Multiple adjacent viewports
- Flipping drawings
- Stereo viewing
- Mapping different window and viewport aspect ratios ( $W / H$ )

# Tiling: Example 3.2.4 of Hill

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- Problem: want to tile dino.dat in 5x5 across screen

```
// set world window
gluOrtho2D( 0.0, 640.0, 0.0, 440.0 );

for( int i = 0; i < 5; i++ ) {
    for( int j = 0; j < 5; j++ ) {
        // .. now set viewport in a loop
        glViewport( i * 64, j * 44, 64, 44 );
        drawPolylineFile( "dino.dat" );
    }
}
```

# Zooming

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- Problem:
  - dino.dat is currently drawn in entire viewport
  - User wants to zoom into just the head
  - Specifies selection by clicking top-left and bottom-right corners
  
- Solution (pseudocode):
  - 1) Program accepts two mouse clicks as rectangle corners
  - 2) Calculate mapping A of current screen to all of dino.dat
  - 3) Use mapping A to refer screen rectangle to world
  - 4) Set window to smaller world rectangle
  - 5) Remaps small rectangle in world to screen viewport

# Unmatched Aspect Ratios

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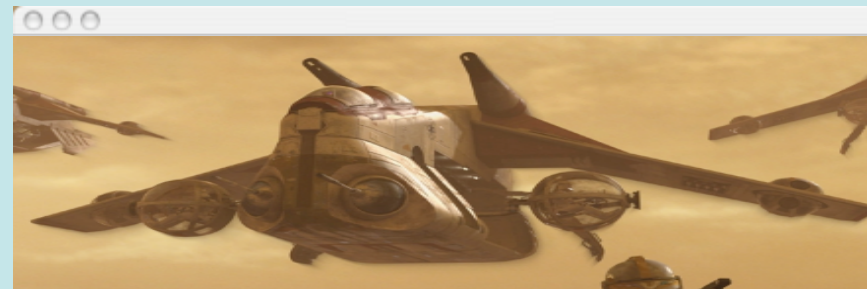
- Aspect ratio
  - $a = \text{Width/Height}$
  - $W.a = (W.r - W.l) / (W.t - W.b)$
  - $V.a = (V.r - V.l) / (V.t - V.b)$
  
- What if Window and Viewport have different *aspect ratios*?
  - $W.a \neq V.a$
  - Have you ever seen this problem before?

# Unmatched Aspect Ratios (cont.)

- Two possible cases
  - $W.a > V.a, W.a < V.a$
- With standard mapping



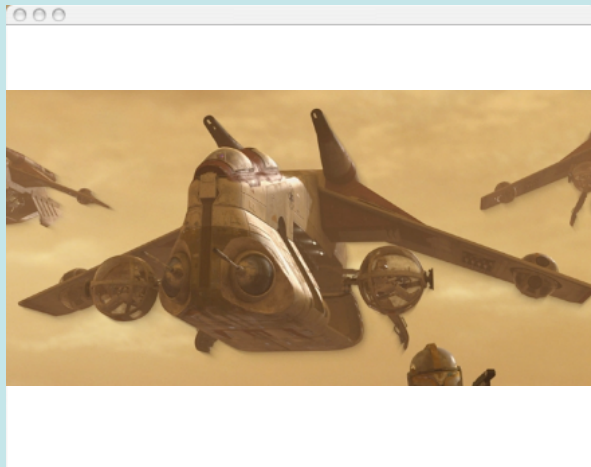
$W.a > V.a$



$W.a < V.a$

# Unmatched Aspect Ratios (cont).

- $W.a > V.a$ 
  - a) Match width, and leave top/bottom empty
  - b) Match height, center, then crop left/right



(a)

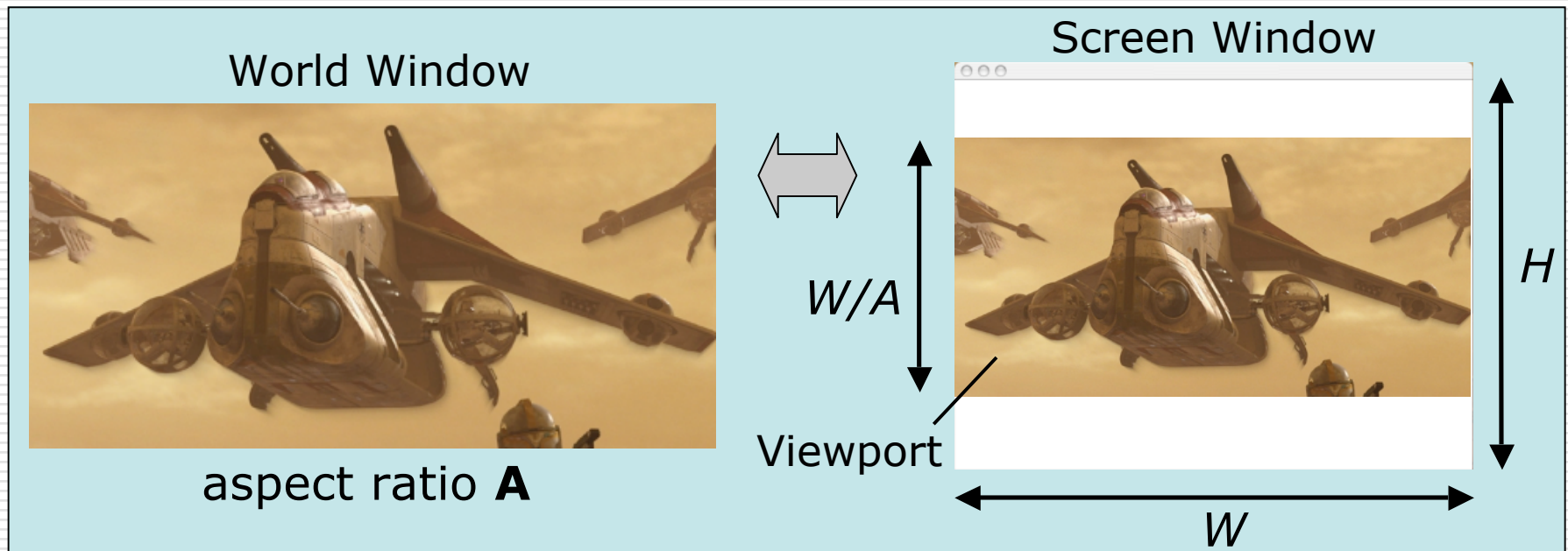


(b)

# Unmatched Aspect Ratios:

$$W.a > V.a$$

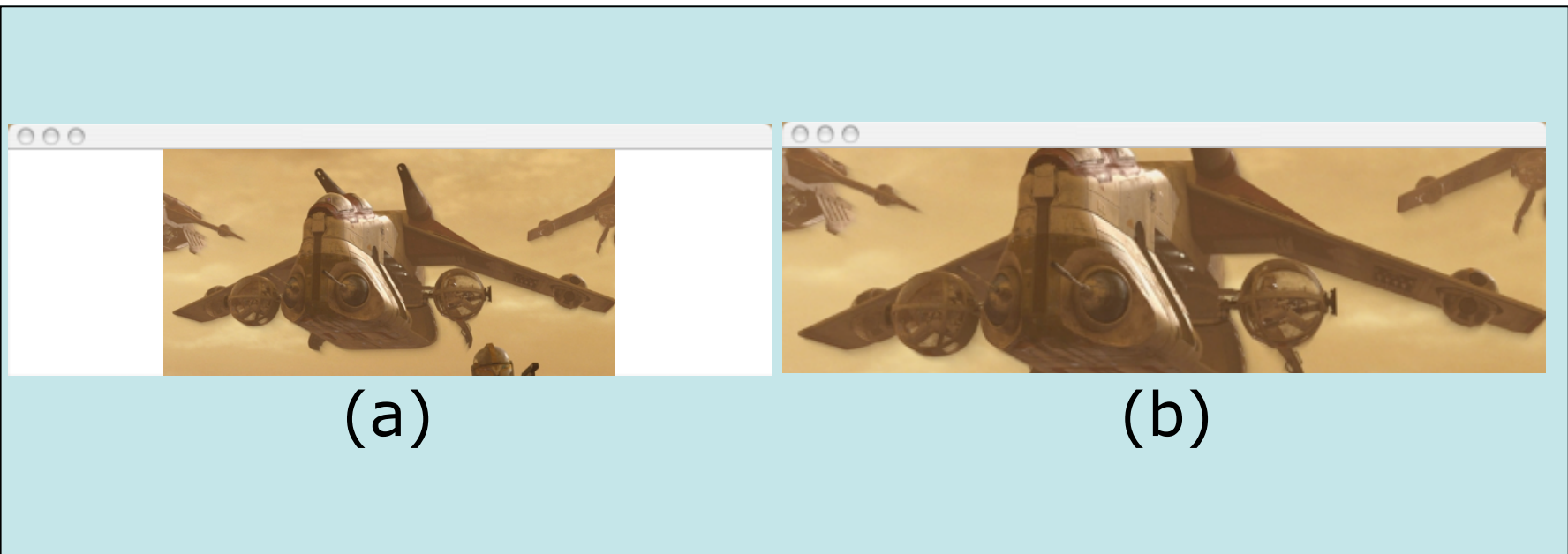
```
glOrtho( W.l, W.r, W.b, W.t );
A = ( W.r - W.l ) / ( W.t - W.b );
if( A > (W/H) ) {
    glViewport( 0, (H * 0.5) - ((W/A) * 0.5), W, W/A );
}
```





## Unmatched Aspect Ratios (cont).

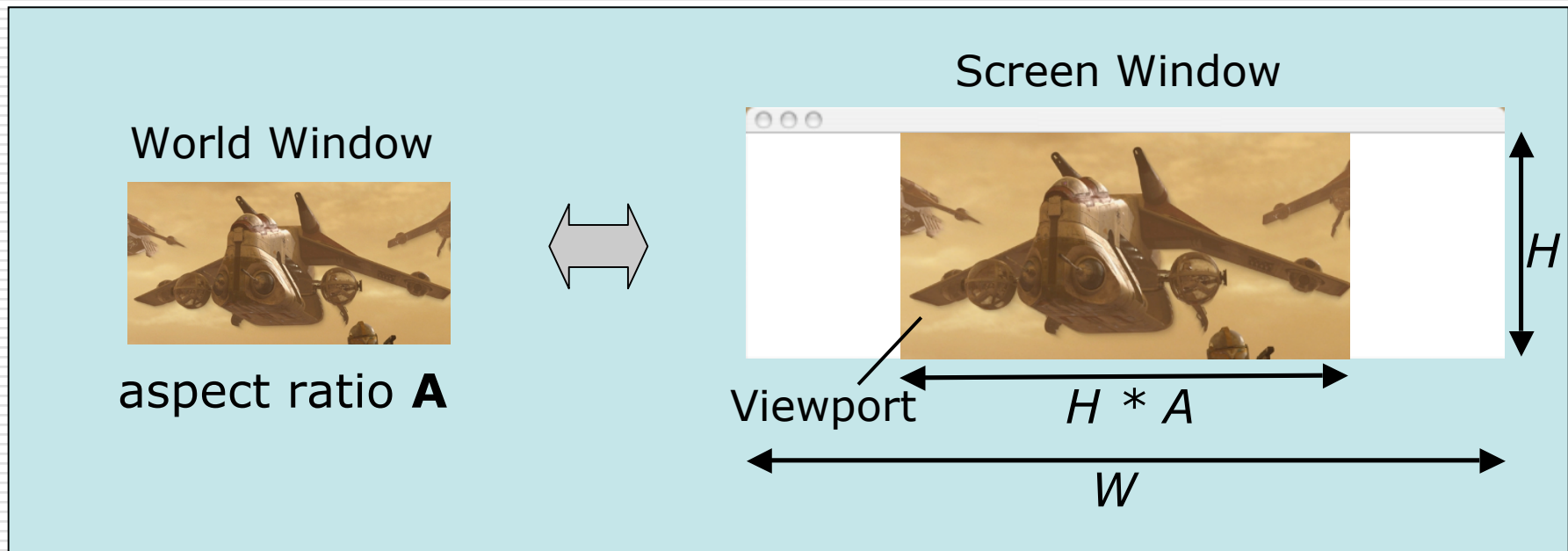
- $W.a < V.a$ 
  - a) Match height, and leave sides empty
  - b) Match width, center, then crop top/bottom



# Unmatched Aspect Ratios:

$$W.a < V.a$$

```
glOrtho( W.l, W.r, W.b, W.t );
A = ( W.r - W.l ) / ( W.t - W.b );
if( A < (W/H) ) {
    glViewport( (W * 0.5) - ((H*A) * 0.5), 0, H*A, H );
}
```



# Reshape: Maintain Aspect Ratio

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```
// glOrtho( l, r, b, t ); is done previously,  
// probably in your draw function  
  
void myReshape( double l, double r, double t, double b,  
               double W, double H ) {  
    A = (r-l) / (t-b);  
  
    if( A > (W/H) ) {  
        glViewport( 0, (H * 0.5) - ((W/A) * 0.5), W, W/A );  
    } else {  
        if( A < (W/H) ) {  
            glViewport( (W * 0.5) - ((H*A) * 0.5), 0, H*A, H );  
        } else {  
            glViewport( 0, 0, W, H ); // equal aspect ratios  
        }  
    }  
}
```

# Cohen-Sutherland Clipping

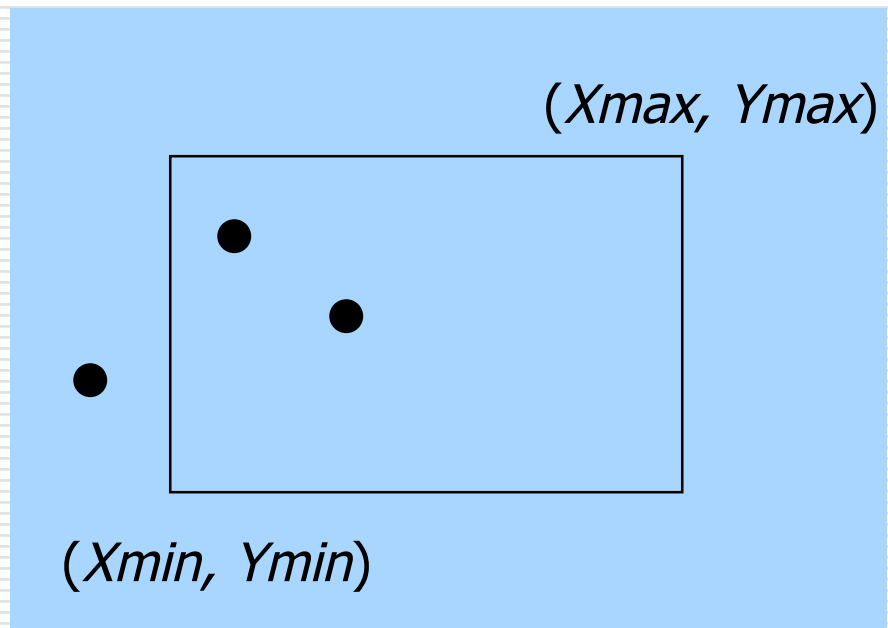
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- ❑ Frequently want to view only a portion of the picture
- ❑ For instance, in `dino.dat`, you can select to view/zoom in on only the dinosaur's head
- ❑ Clipping: eliminate portions not selected
- ❑ OpenGL automatically clips for you
- ❑ We want algorithm for clipping
- ❑ Classical algorithm: Cohen-Sutherland Clipping
- ❑ Picture could have 1,000s of segments
  - Efficiency is important

# Clipping Points

- Determine whether a point  $(x, y)$  is inside or outside of the world window

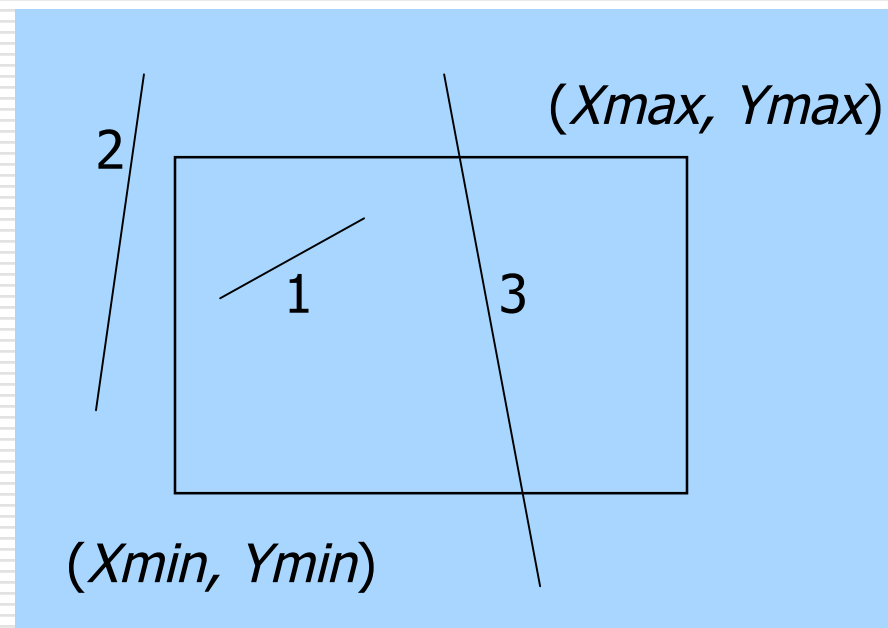
```
if( Xmin <= x <= Xmax ) and  
  ( Ymin <= y <= Ymax )  
then  
  the point  $(x, y)$  is inside  
else  
  the point is outside
```



# Clipping Lines: Three Cases

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- Case 1
  - All of line in
- Case 2
  - All of line out
- Case 3
  - Part in, part out



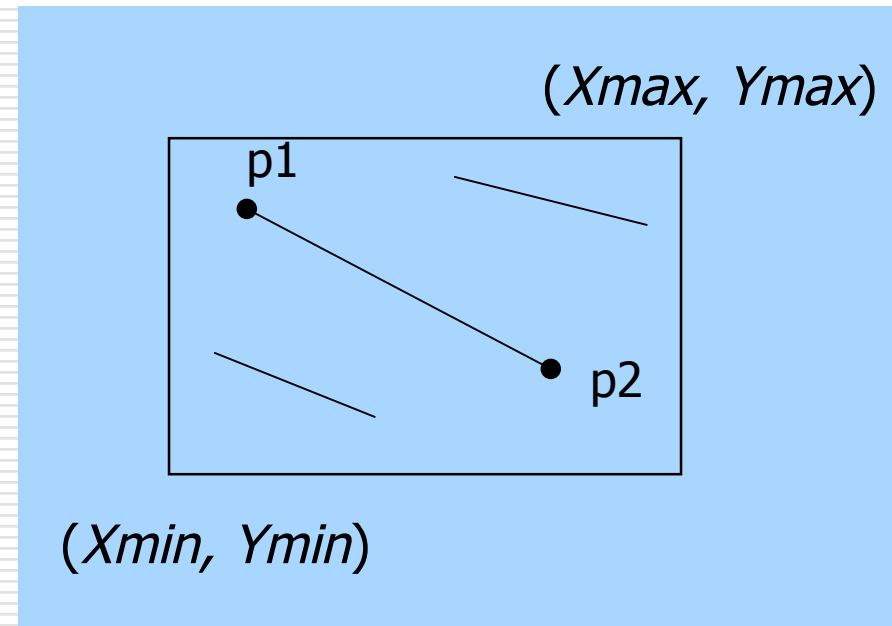
# Clipping Lines: Trivially Accept

## □ Case 1

- All of line inside
- Test line endpoints

## □ Method

- Simply compare  $x$ ,  $y$  values of endpoints to rectangle extents



```
if( Xmin <= p1.x <= Xmax ) and
  ( Xmin <= p2.x <= Xmax ) and
  ( Ymin <= p1.y <= Ymax ) and
  ( Ymin <= p2.y <= Ymax )
then
  draw line completely
```

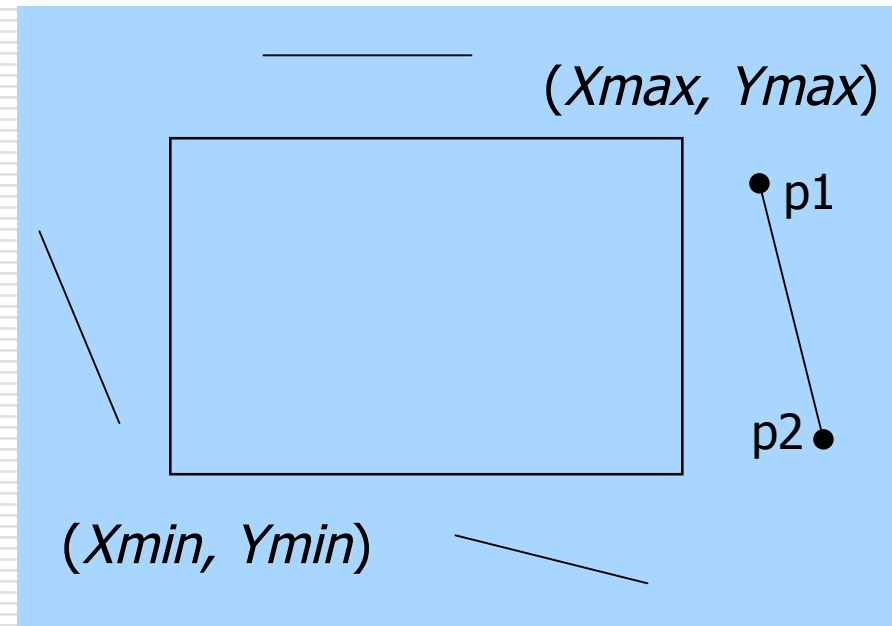
# Clipping Lines: Trivially Reject

## □ Case 2

- All of line outside
- Test line endpoints

## □ Method

- Simply compare  $x, y$  values of endpoints to rectangle extents



```

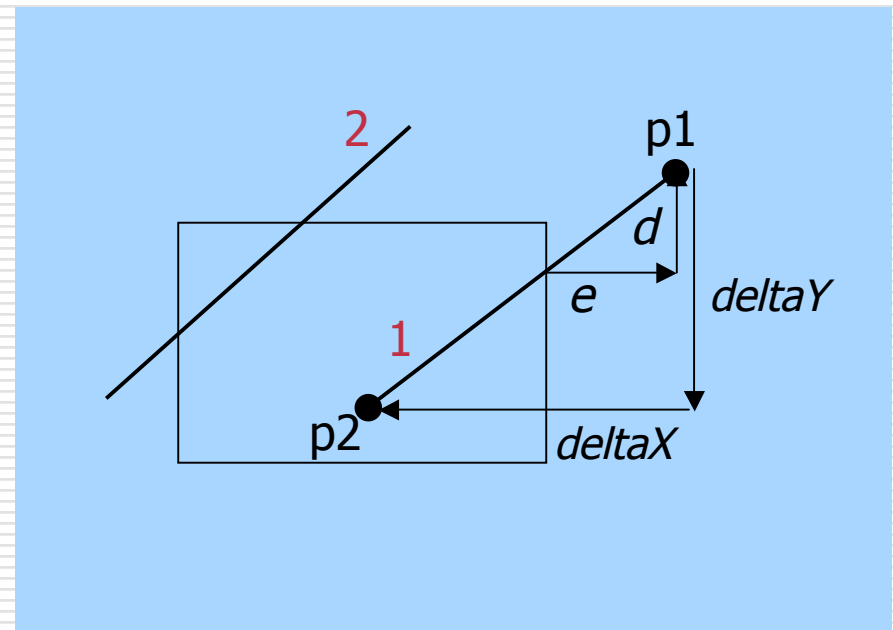
if( ( p1.x < Xmin ) and ( p2.x < Xmin ) ) or
   ( ( p1.x > Xmax ) and ( p2.x > Xmax ) ) or
   ( ( p1.y < Ymin ) and ( p2.y < Ymin ) ) or
   ( ( p1.y > Ymax ) and ( p2.y > Ymax ) ) or
then
  ignore line

```



# Clipping Lines: Non-Trivial Case

- Case 3
  - Part in, part out
- Two variations
  1. One point in, other out
  2. Both points out, but line cuts through
- Need to find inside segments
- Use similar triangles to figure out length of inside segments

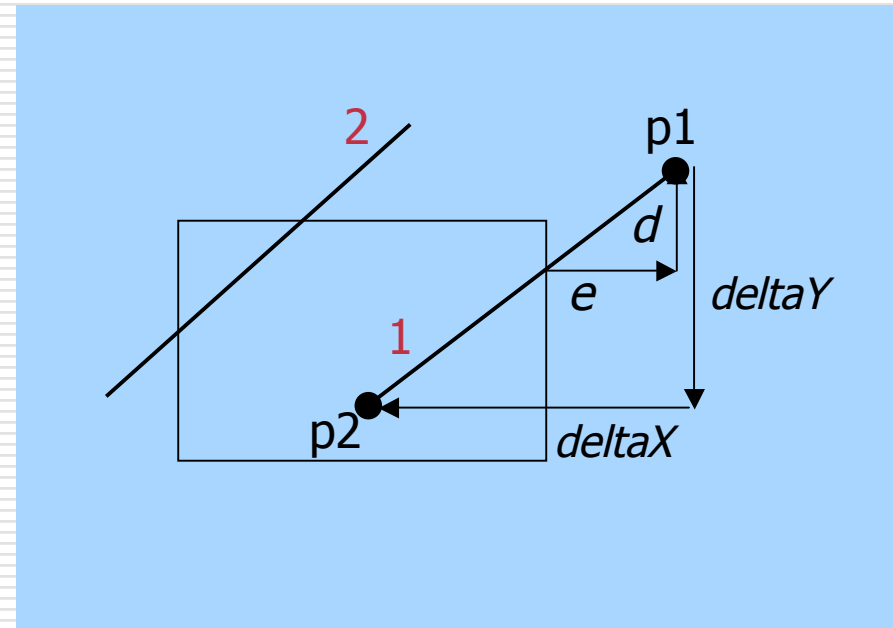


$$\frac{d}{\text{deltaY}} = \frac{e}{\text{deltaX}}$$

# Clipping Lines: Non-Trivial Case

□ If clipping window has  
 $(l, r, b, t) =$   
 $(30, 220, 50, 240)$ ,  
 what happens when  
 the following lines are  
 clipped?

- (a)  $p1 = (40, 140)$   
 $p2 = (100, 200)$
- (b)  $p1 = (20, 10)$   
 $p2 = (20, 200)$
- (c)  $p1 = (100, 180)$   
 $p2 = (200, 250)$



$$\frac{d}{\text{deltaY}} = \frac{e}{\text{deltaX}}$$

# Cohen-Sutherland Pseudocode

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```
int clipSegment( Point2 p1, Point2 p2, RealRect W ) {
    do {
        // If whole line survives
        if( trivial accept ) { return 1; }
        // If no portion survives
        if( trivial reject ) { return 0; }
        // now clip
        if( p1 is outside ) {
            // find surviving segment
            if( p1 < W.l )      clip at W.l
            else if( p1 > W.r ) clip to W.r
            else if( p1 < W.b ) clip to W.b
            else if( p1 > W.t ) clip to W.t
        }
    }
```

(continued on next slide)

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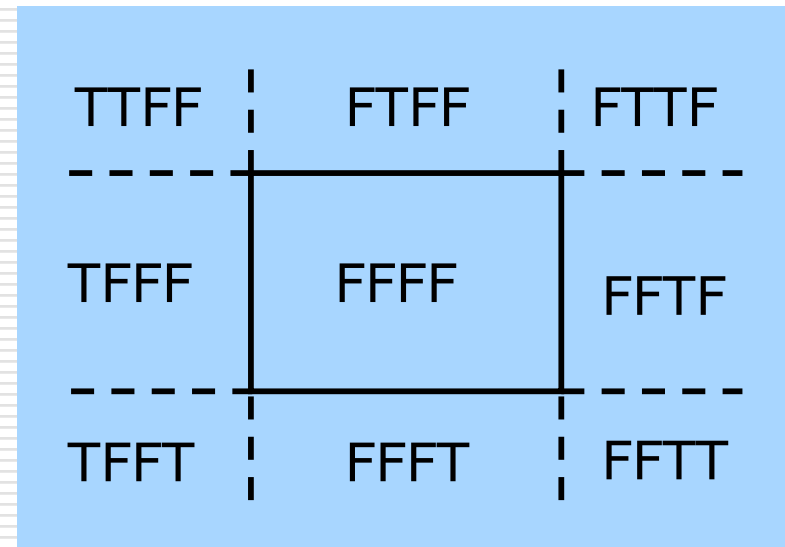
# Cohen-Sutherland Pseudocode (cont.)

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```
else { // p2 is outside
        // find surviving segment
        if( p2 < W.l )      clip at W.l
        else if( p2 > W.r ) clip to W.r
        else if( p2 < W.b ) clip to W.b
        else if( p2 > W.t ) clip to W.t
    }
} while( 1 );
}
```

# Cohen-Sutherland Implementation

- Need quick, efficient comparisons to get accepts, rejects, clips
- Can use C/C++ bit operations
- Break space into 4-bit words
  - Trivial accept: both points FFFF
  - Trivial reject: T in same position
  - Everything else: clip
- Systematically clips against four edges
- Important: read Hill 3.3



# References

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- Hill: 3.1 – 3.3, 3.8