Computer Graphics (CS 543)  
Lecture 11c: 2D Clipping

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OpenGL Stages

- After projection, several stages before objects drawn to screen
- These stages are **NOT** programmable

Vertex shader: programmable

In hardware: **NOT** programmable
Hardware Stage: Primitive Assembly

- Up till now: Transformations and projections applied to vertices individually
- **Primitive assembly**: After transforms, projections, individual vertices grouped back into primitives
- **E.g. v6, v7 and v8** grouped back into triangle
Hardware Stage: Clipping

- After primitive assembly, subsequent operations are per-primitive
- **Clipping**: Remove primitives (lines, polygons, text, curves) outside view frustum (canonical view volume)
Rasterization

- Determine which pixels that primitives (shapes) map to
  - Fragment generation
  - Rasterization or scan conversion
Hidden Surface Removal

- Some tasks deferred until fragment processing
Clipping

- 2D and 3D clipping algorithms
  - 2D against clipping window
  - 3D against clipping volume
- 2D clipping
  - Lines (e.g. dino.dat)
  - Polygons
  - Curves
  - Text
Clipping 2D Line Segments

- **Brute force approach**: compute intersections with all sides of clipping window
  - Inefficient: one division per intersection
2D Clipping

- **Better Idea:** eliminate as many cases as possible without computing intersections
- Cohen-Sutherland Clipping algorithm

Goal: Develop simple tests to eliminate lines like CD or AB (no intersection)
Clipping Points


Determine whether a point \((x,y)\) is inside or outside of the world window?

If \((x_{\text{min}} \leq x \leq x_{\text{max}})\) and \((y_{\text{min}} \leq y \leq y_{\text{max}})\)

then the point \((x,y)\) is inside
else the point is outside
3 cases:

- **Case 1:** All of line in
- **Case 2:** All of line out
- **Case 3:** Part in, part out
Clipping Lines: Trivial Accept

Case 1: All of line in Test line endpoints:

\[ \text{Xmin} \leq P1.x, P2.x \leq \text{Xmax} \quad \text{and} \quad \text{Ymin} \leq P1.y, P2.y \leq \text{Ymax} \]

Note: simply comparing x,y values of endpoints to x,y values of rectangle

Result: trivially accept.
Draw line in completely
Clipping Lines: Trivial Reject

Case 2: All of line out
Test line endpoints:

- $p1.x, p2.x <= X_{min}$ OR
- $p1.x, p2.x >= X_{max}$ OR
- $p1.y, p2.y <= y_{min}$ OR
- $p1.y, p2.y >= y_{max}$

Note: simply comparing $x,y$ values of endpoints to $x,y$ values of rectangle

Result: trivially reject.
Don’t draw line in
Clipping Lines: Non-Trivial Cases

**Case 3:** Part in, part out

Two variations:
- One point in, other out
- Both points out, but part of line cuts through viewport

Need to find inside segments

Use similar triangles to figure out length of inside segments

\[
\frac{d}{dely} = \frac{e}{delx}
\]
If chopping window has (left, right, bottom, top) = (30, 220, 50, 240), what happens when the following lines are chopped?

(a) p1 = (40, 140), p2 = (100, 200)

(b) p1 = (20, 10), p2 = (20, 200)

(c) p1 = (100, 180), p2 = (200, 250)

\[
\frac{d}{dely} = \frac{e}{delx}
\]
Cohen-Sutherland pseudocode (Hill)

```cpp
int clipSegment(Point2& p1, Point2& p2, RealRect W) {
    do{
        if(trivial accept) return 1; // whole line survives
        if(trivial reject) return 0; // no portion survives
        // now chop
        if(p1 is outside)
            // find surviving segment
            {
                if(p1 is to the left) chop against left edge
                else if(p1 is to the right) chop against right edge
                else if(p1 is below) chop against the bottom edge
                else if(p1 is above) chop against the top edge
            }
    }
```
Cohen-Sutherland pseudocode (Hill)

else // p2 is outside
    // find surviving segment
    {
        if(p2 is to the left) chop against left edge
        else if(p2 is to right) chop against right edge
        else if(p2 is below) chop against the bottom edge
        else if(p2 is above) chop against the top edge
    }
}while(1);
References