Computer Graphics (CS 543) Lecture 6b: Viewing & Camera Control

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3D Viewing?

- Specify a view volume
- Objects inside view volume drawn to viewport (screen)
- Objects outside view volume clipped (not drawn)!







Different View Volume Shapes



Orthogonal view volume



Perspective view_volume

- Different view volume shape => different look
- Foreshortening? Near objects bigger
 - Perpective projection causes foreshortening
 - Orthogonal projection: no foreshortening



The World Frame

- Object positions initially defined in world frame
- World Frame origin at (0,0,0)
- Objects positioned, oriented (translate, scale, rotate transformations) applied to objects in world frame





Camera Frame



- More natural to describe object positions relative to camera (eye)
- Why?
 - Our view of the world
 - First person shooter games



Camera Frame

- Viewing: After user chooses camera (eye) position, represent objects in camera frame (origin at eye position)
- Viewing transformation: Converts object (x,y,z) positions in world frame to positions in camera frame





Default OpenGL Camera, View Volume

- Initially Camera at origin: object and camera frames same
- Points in negative z direction
- Default view volume is cube with sides of length 2







Moving the Camera Frame



- Object distances relative to camera determined by the modelview matrix
 - Transforms (scale, translate, rotate) go into modelview matrix
 - Camera transforms also go in modelview matrix (CTM)
 - Why? Combination of object + camera transforms = relative transform



Moving the Camera

- We can move camera using sequence of rotations and translations
- Example: side view
 - Rotate the camera
 - Move it away from origin
 - Model-view matrix C = TR

```
// Using mat.h
```

```
mat4 t = Translate (0.0, 0.0, -d);
mat4 ry = RotateY(90.0);
mat4 m = t*ry;
```





The LookAt Function



- gluLookAt deprecated!!
- Homegrown mat4 method LookAt() in mat.h
 - Functionality: sets camera position, transforms object distances to camera frame





The LookAt Function



LookAt(eye, at, up)





Nate Robbins LookAt Demo





0.00 , 0.00 , 0.00 , \sim - center

0.00 , 1.00 , 0.00); <- up

glLightfv(GL_LIGHT0, GL_POSITION, pos);

Click on the arguments and move the mouse to modify values.

What does LookAt do?

- Programmer defines eye, lookAt and Up
- LookAt method:
 - Forms new axes (u, v, n) at camera
 - Transform objects from world to eye camera frame





Camera with Arbitrary Orientation and Position



- v points vertically upward,
- **n** away from the view volume,
- **u** at right angles to both **n** and **v**.
- The camera looks toward -**n**.
- All vectors are normalized.





World coordinate

LookAt: Effect of Changing Eye Position or LookAt Point

- Programmer sets LookAt (eye, at, up)
- If eye, lookAt point changes => u,v,n changes







Viewing Transformation Steps

- 1. Form camera (u,v,n) frame
- 2. Transform objects from world frame (Compose matrix to transform coordinates)
- Next, let's form camera (u,v,n) frame



Constructing U,V,N Camera Frame

- Lookat arguments: LookAt (eye, at, up)
- Known: eye position, LookAt Point, up vector
- **Derive:** new origin and three basis (u,v,n) vectors





- New Origin: eye position (that was easy)
- 3 basis vectors:
 - one is the normal vector (**n**) of the viewing plane,
 - other two (**u** and **v**) span the viewing plane







• How about u and v?



 Derive u first
 u is a vector that is perp to the plane spanned by N and view up vector (V_up)

$$U = V_up \times n$$
$$u = U / |U|$$



How about v?









Step 2: World to Eye Transformation

- Next, use u, v, n to compose LookAt matrix
- Transformation matrix (M_{w2e}) ?
 - Matrix that transforms a point P in world frame to P' in eye frame

 $P' = M_{w^{2ex}} P$



1. Come up with transformation sequence that aligns eye frame with world frame

2. Apply this transform sequence to point ${\bf P}$ in reverse order





World to Eye Transformation

- 1. Rotate eye frame to "align" it with world frame
- 2. Translate (-ex, -ey, -ez) to align origin with eye



World to Eye Transformation

 Transformation order: apply the transformation to the object in reverse order - translation first, and then rotate



lookAt Implementation (from mat.h)



Eye space origin: (Eye.x , Eye.y,Eye.z)

Basis vectors:

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n = (eye - Lookat) / | eye - Lookat| u = (V_up x n) / | V_up x n | v = n x u ux uy uz -**e.u** vx vy vz -**e.v** nx ny nz -**e.n** 0 0 0 1

```
mat4 LookAt( const vec4& eye, const vec4& at, const vec4& up )
{
    vec4 n = normalize(eye - at);
    vec4 u = normalize(cross(up,n));
    vec4 v = normalize(cross(n,u));
    vec4 t = vec4(0.0, 0.0, 0.0, 1.0);
    mat4 c = mat4(u, v, n, t);
    return c * Translate( -eye );
```

Other Camera Controls



- The LookAt function is only for positioning camera
- Other ways to specify camera position/orientation/movement
 - Yaw, pitch, roll
 - Elevation, azimuth, twist
 - Direction angles

Flexible Camera Control

- Sometimes, we want camera to move
- Like controlling an airplane's orientation
- Adopt aviation terms:
 - Pitch: nose up-down
 - Roll: roll body of plane
 - Yaw: move nose side to side







Yaw, Pitch and Roll Applied to Camera



Flexible Camera Control

• Create a camera class





- class Camera private: Point3 eye; Vector3 u, v, n;.... etc
- Camera methods (functions) to specify slide, pitch, roll, yaw wrt u,v,n. E.g

cam.slide(1, 0, 2); // slide camera backward 2 and right 1
cam.roll(30); // roll camera 30 degrees
cam.yaw(40); // yaw camera 40 degrees
cam.pitch(20); // pitch camera 20 degrees





Question: Pitch rotates which axes?

Implementing Flexible Camera Control



Camera class: maintains current (u,v,n) and eye position

```
class Camera
private:
Point3 eye;
Vector3 u, v, n;.... etc
```

User inputs desired roll, pitch, yaw angle or slide

- 1. **Roll, pitch, yaw:** calculate modified vector (u', v', n')
- 2. Slide: Calculate new eye position
- 3. Update lookAt matrix, Load it into CTM

Example: Camera Slide

• Recall: the axes are unit vectors

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- User changes eye by delU, delV or delN
- eye = eye + changes (delU, delV, delN)
- Note: function below combines all slides into one
 E.g moving camera by *D* along its u axis = eye + Du

```
void camera::slide(float delU, float delV, float delN)
{
    eye.x += delU*u.x + delV*v.x + delN*n.x;
    eye.y += delU*u.y + delV*v.y + delN*n.y;
    eye.z += delU*u.z + delV*v.z + delN*n.z;
    setModelViewMatrix();
    Function to update new eye, u, v and n
```



Load Matrix into CTM



- Slide changes **eVec**,
- roll, pitch, yaw, change u, v, n
- Call setModelViewMatrix after slide, roll, pitch or yaw

Example: Camera Roll





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 $\mathbf{u}' = \cos(\alpha)\mathbf{u} + \sin(\alpha)\mathbf{v}$ $\mathbf{v}' = -\sin(\alpha)\mathbf{u} + \cos(\alpha)\mathbf{v}$

```
void Camera::roll(float angle)
{ // roll the camera through angle degrees
  float cs = cos(3.142/180 * angle);
  float sn = sin(3.142/180 * angle);
  Vector3 t = u; // remember old u
  u.set(cs*t.x - sn*v.x, cs*t.y - sn.v.y, cs*t.z - sn.v.z);
  v.set(sn*t.x + cs*v.x, sn*t.y + cs.v.y, sn*t.z + cs.v.z)
  setModelViewMatrix();
```

References

- Interactive Computer Graphics, Angel and Shreiner, Chapter 4
- Computer Graphics using OpenGL (3rd edition), Hill and Kelley