

# Computer Graphics (CS 4731)

## Lecture 17: Lighting, Shading and Materials (Part 2)

Prof Emmanuel Agu

*Computer Science Dept.  
Worcester Polytechnic Institute (WPI)*





# Modified Phong Model

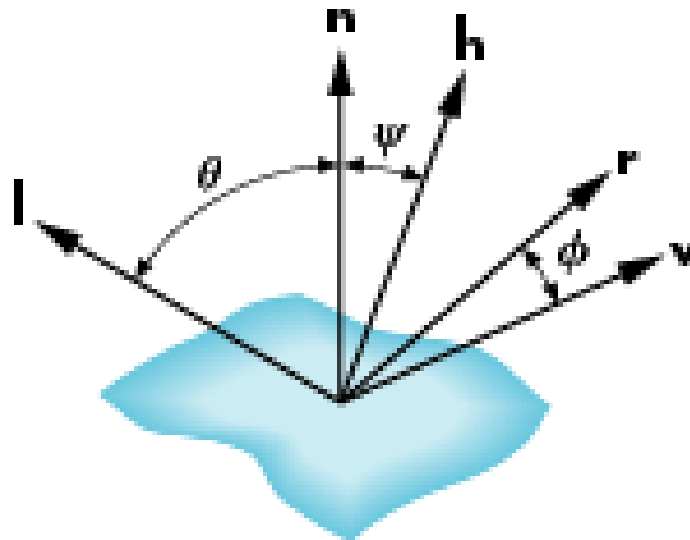
$$I = k_d I_d \mathbf{l} \cdot \mathbf{n} + k_s I_s (\mathbf{v} \cdot \mathbf{r})^\alpha + k_a I_a$$

$$I = k_d I_d \mathbf{l} \cdot \mathbf{n} + k_s I_s (\mathbf{n} \cdot \mathbf{h})^\beta + k_a I_a$$

Used in  
OpenGL

- Blinn proposed using **halfway vector**, more efficient
- **h** is normalized vector halfway between **l** and **v**

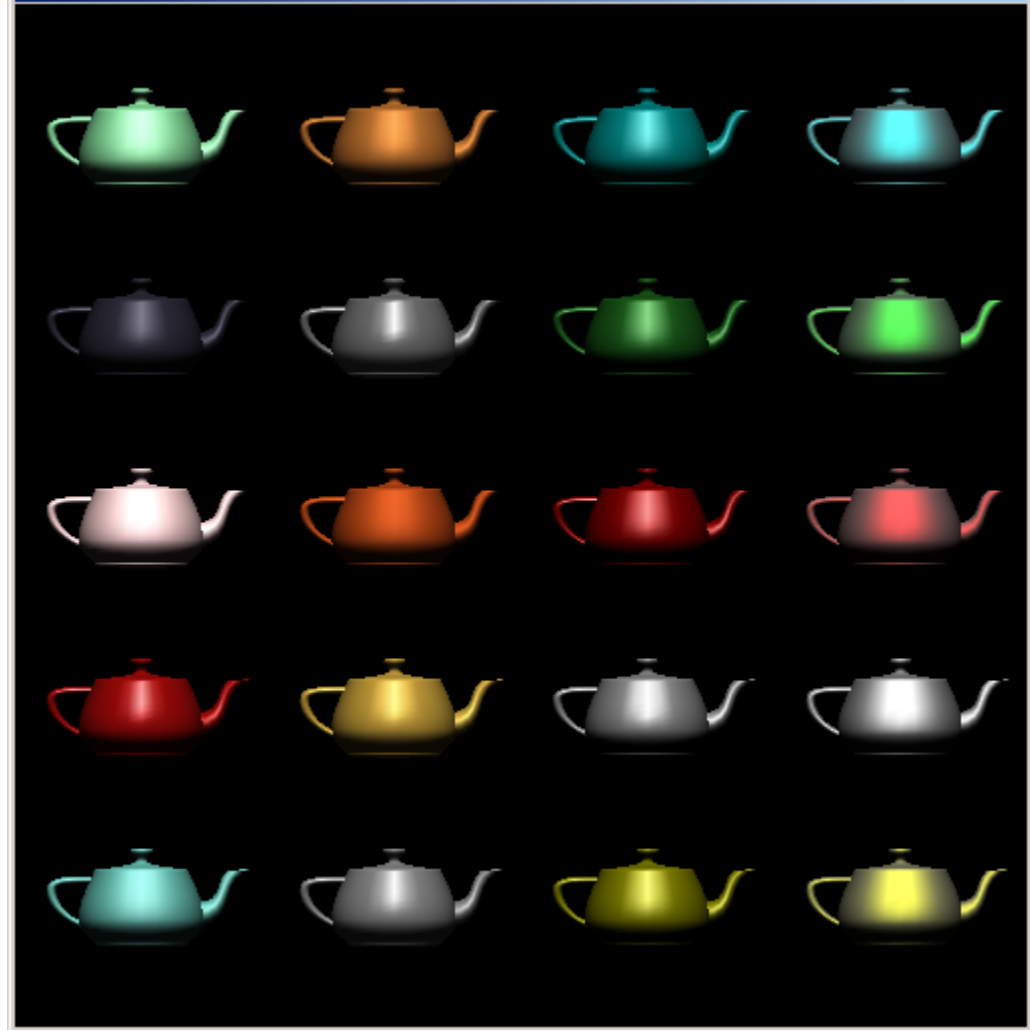
$$\mathbf{h} = (\mathbf{l} + \mathbf{v}) / |\mathbf{l} + \mathbf{v}|$$



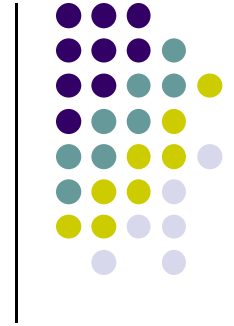


# Example

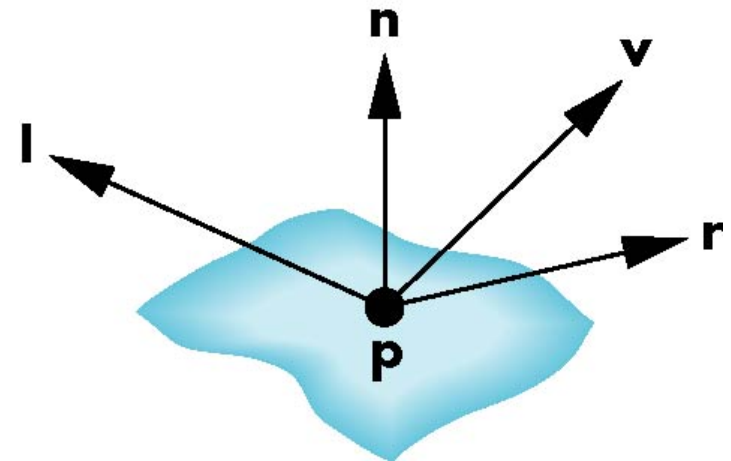
Modified  
Phong model gives  
Similar results as  
original Phong



# Computation of Vectors



- To calculate lighting at vertex P  
Need  **$\mathbf{l}$** ,  **$\mathbf{n}$** ,  **$\mathbf{r}$**  and  **$\mathbf{v}$**  vectors at vertex P
- User specifies:
  - Light position
  - Viewer (camera) position
  - Vertex (mesh position)
- **$\mathbf{l}$** : Light position – vertex position
- **$\mathbf{v}$** : Viewer position – vertex position
- Normalize all vectors!





# Specifying a Point Light Source

- For each light source component, set RGBA and position
- alpha = transparency

```
vec4 diffuse0 =vec4(1.0, 0.0, 0.0, 1.0);
vec4 ambient0 = vec4(1.0, 0.0, 0.0, 1.0);
vec4 specular0 = vec4(1.0, 0.0, 0.0, 1.0);
vec4 light0_pos =vec4(1.0, 2.0, 3,0, 1.0);
```

Red            Green            Blue            Alpha

x            y            z            w



# Distance and Direction

```
vec4 light0_pos =vec4(1.0, 2.0, 3,0, 1.0);
```

x            y            z            w

Four red arrows point from the labels x, y, z, and w below to the corresponding values in the vector: 1.0, 2.0, 3,0, and 1.0.

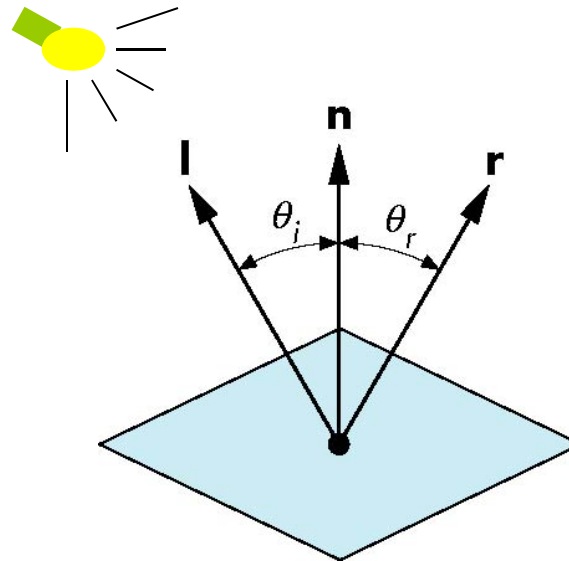
- Position is in homogeneous coordinates
  - If  $w = 1.0$ , we are specifying a finite  $(x,y,z)$  location
  - If  $w = 0.0$ , light at infinity  
( $x/w = \text{infinity}$  if  $w = 0$ )



## Recall: Mirror Direction Vector $\mathbf{r}$

- Can compute  $\mathbf{r}$  from  $\mathbf{l}$  and  $\mathbf{n}$
- $\mathbf{l}$ ,  $\mathbf{n}$  and  $\mathbf{r}$  are co-planar
- What about determining vertex normal  $\mathbf{n}$ ?

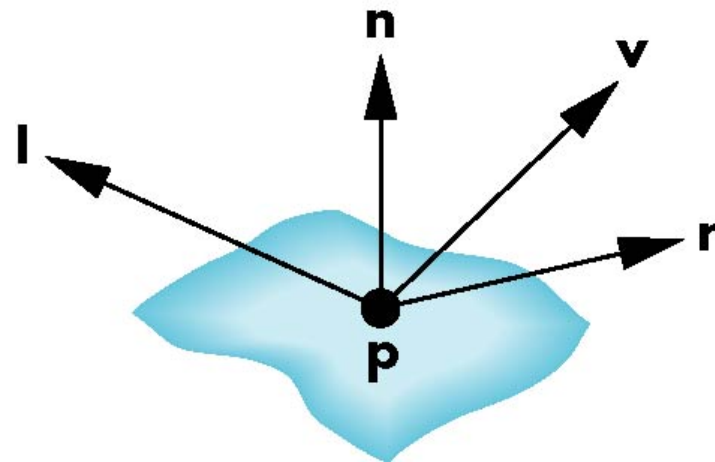
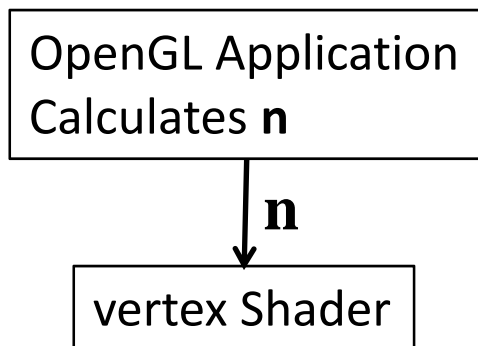
$$\mathbf{r} = 2 (\mathbf{l} \cdot \mathbf{n}) \mathbf{n} - \mathbf{l}$$





# Finding Normal, $\mathbf{n}$

- Normal calculation in application, passed to vertex shader





# Recall: Newell Method for Normal Vectors



- Formulae: Normal  $N = (m_x, m_y, m_z)$

$$m_x = \sum_{i=0}^{N-1} (y_i - y_{next(i)}) (z_i + z_{next(i)})$$

$$m_y = \sum_{i=0}^{N-1} (z_i - z_{next(i)}) (x_i + x_{next(i)})$$

$$m_z = \sum_{i=0}^{N-1} (x_i - x_{next(i)}) (y_i + y_{next(i)})$$

# OpenGL shading



- Need
  - Normals
  - material properties
  - Lights
- State-based shading functions (glNormal, glMaterial, glLight) have been deprecated
- 2 options:
  - Compute lighting in application
  - or send attributes to shaders



# Material Properties

- Need to specify material properties of scene objects
- Material properties also has ambient, diffuse, specular
- Material properties specified as RGBA + reflectivities
- w component gives opacity (transparency)
- **Default?** all surfaces are opaque

```
vec4 ambient = vec4(0.2, 0.2, 0.2, 1.0);
vec4 diffuse = vec4(1.0, 0.8, 0.0, 1.0);
vec4 specular = vec4(1.0, 1.0, 1.0, 1.0);
GLfloat shine = 100.0
```

Red      Green      Blue      Opacity

Material  
Shininess

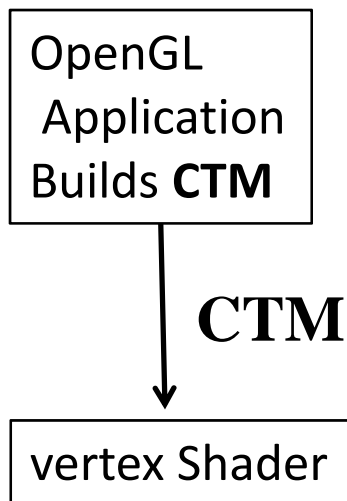


## Recall: CTM Matrix passed into Shader

- **Recall:** CTM matrix concatenated in application

mat4 **ctm** = ctm \* LookAt(vec4 eye, vec4 at, vec4 up);

- CTM matrix passed in contains object transform + Camera
- Connected to matrix **ModelView** in shader



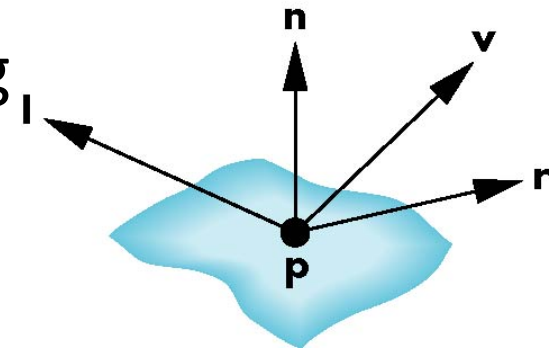
```
in vec4 vPosition;
Uniform mat4 ModelView ; ← CTM passed in

main( )
{
    // Transform vertex position into eye coordinates
    vec3 pos = (ModelView * vPosition).xyz;
    .....
}
```



# Computation of Vectors

- CTM transforms vertex position into eye coordinates
  - Eye coordinates? Object, light distances measured from eye
- Normalize all vectors! (magnitude = 1)
- GLSL has a **normalize** function
- **Note:** vector lengths affected by scaling



```
// Transform vertex position into eye coordinates
```

```
vec3 pos = (ModelView * vPosition).xyz;
```

```
vec3 L = normalize( LightPosition.xyz - pos ); // light vector
```

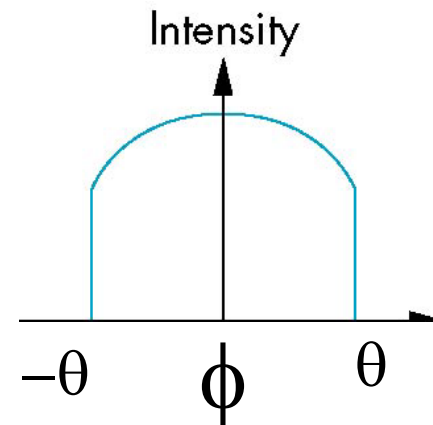
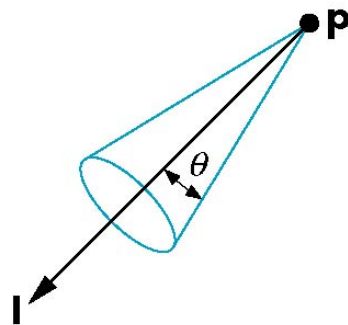
```
vec3 E = normalize( -pos ); // view vector
```

```
vec3 H = normalize( L + E ); // Halfway vector
```



# Spotlights

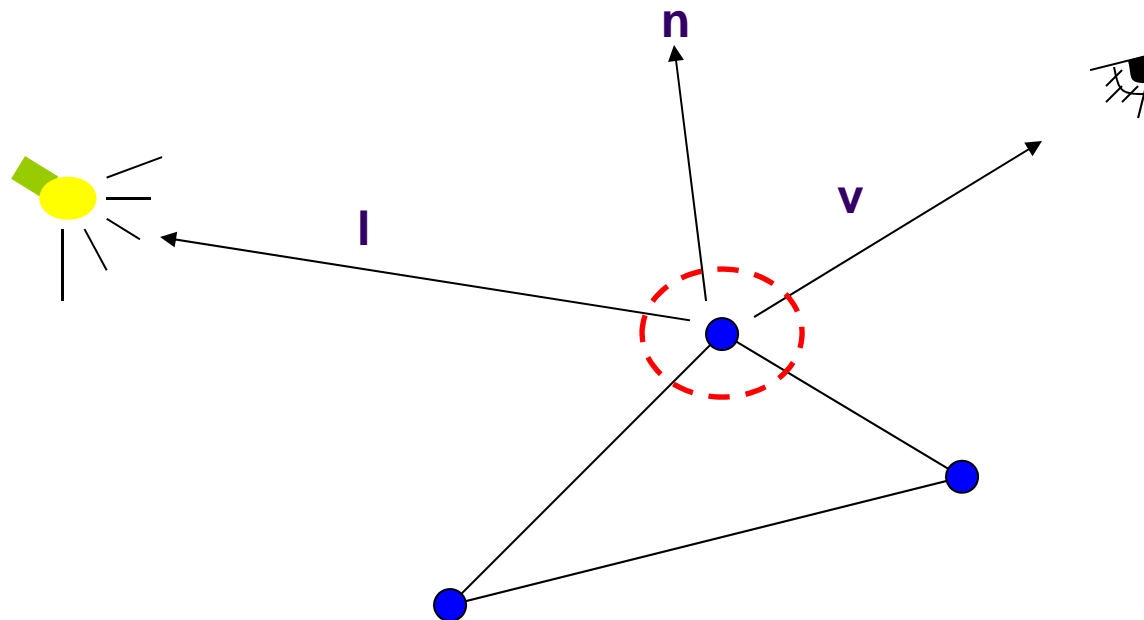
- Derive from point source
  - **Direction I** (of lobe center)
  - **Cutoff:** No light outside  $\theta$
  - **Attenuation:** Proportional to  $\cos^\alpha \phi$





## Recall: Lighting Calculated Per Vertex

- Phong model (ambient+diffuse+specular) calculated at each vertex to determine vertex color
- Per vertex calculation? Usually done in vertex shader





# Per-Vertex Lighting Shaders I

**// vertex shader**

```
in vec4 vPosition;  
in vec3 vNormal;  
out vec4 color; //vertex shade
```

Ambient, diffuse, specular  
(light \* reflectivity) specified by user

```
// light and material properties  
uniform vec4 AmbientProduct, DiffuseProduct, SpecularProduct;  
uniform mat4 ModelView;  
uniform mat4 Projection;  
uniform vec4 LightPosition;  
uniform float Shininess;
```

$k_a I_a$

$k_d I_d$

$k_s I_s$

exponent of specular term





# Per-Vertex Lighting Shaders II

```
void main( )
{
    // Transform vertex position into eye coordinates
    vec3 pos = (ModelView * vPosition).xyz;

    vec3 L = normalize( LightPosition.xyz - pos );
    vec3 E = normalize( -pos );
    vec3 H = normalize( L + E ); // halfway Vector

    // Transform vertex normal into eye coordinates
    vec3 N = normalize( ModelView*vec4(vNormal, 0.0) ).xyz;
```

# Per-Vertex Lighting Shaders III



// Compute terms in the illumination equation

vec4 ambient = AmbientProduct; ←  $k_a I_a$

float cos\_theta = max( dot(L, N), 0.0 );

vec4 diffuse = cos\_theta \* DiffuseProduct; ←  $k_d I_d \mathbf{l} \cdot \mathbf{n}$

float cos\_phi = pow( max(dot(N, H), 0.0), Shininess );

vec4 specular = cos\_phi \* SpecularProduct; ←  $k_s I_s (\mathbf{n} \cdot \mathbf{h})^\beta$

if( dot(L, N) < 0.0 ) specular = vec4(0.0, 0.0, 0.0, 1.0);

gl\_Position = Projection \* ModelView \* vPosition;

color = ambient + diffuse + specular;

color.a = 1.0;

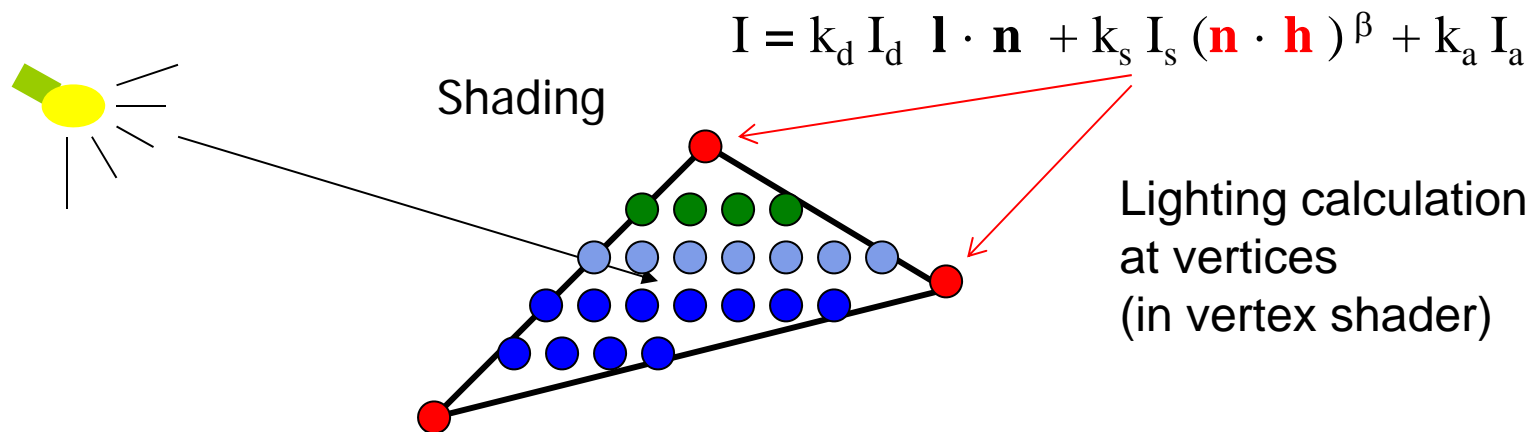
}

$$I = k_d I_d \mathbf{l} \cdot \mathbf{n} + k_s I_s (\mathbf{n} \cdot \mathbf{h})^\beta + k_a I_a$$



# Shading?

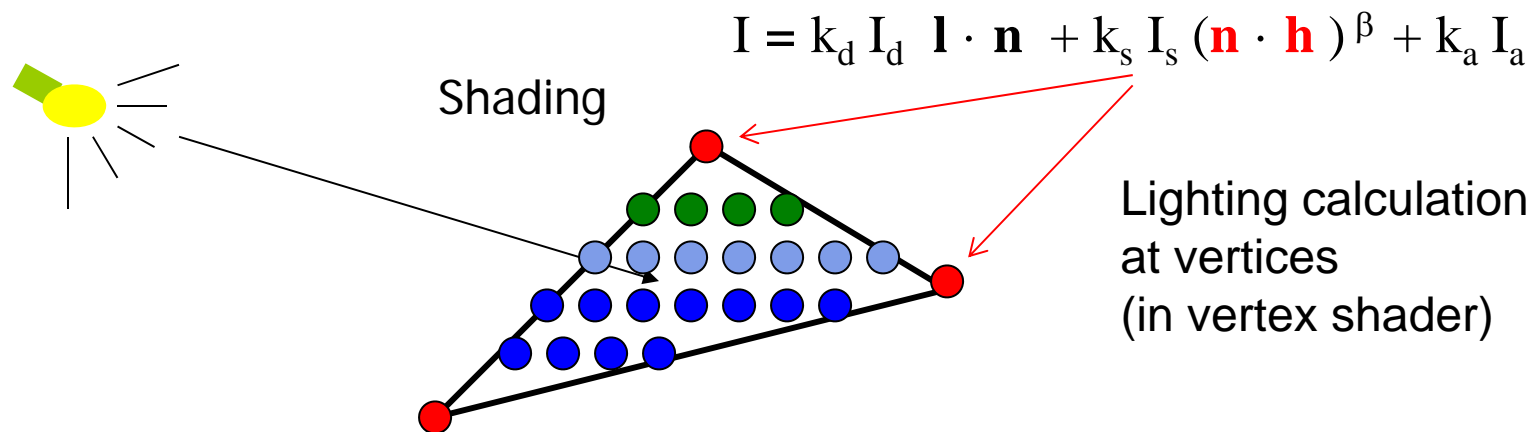
- After triangle is rasterized/drawn
  - Per-vertex lighting calculation means we know color of pixels coinciding with vertices (**red dots**)
- Shading determines color of interior surface pixels





# Shading?

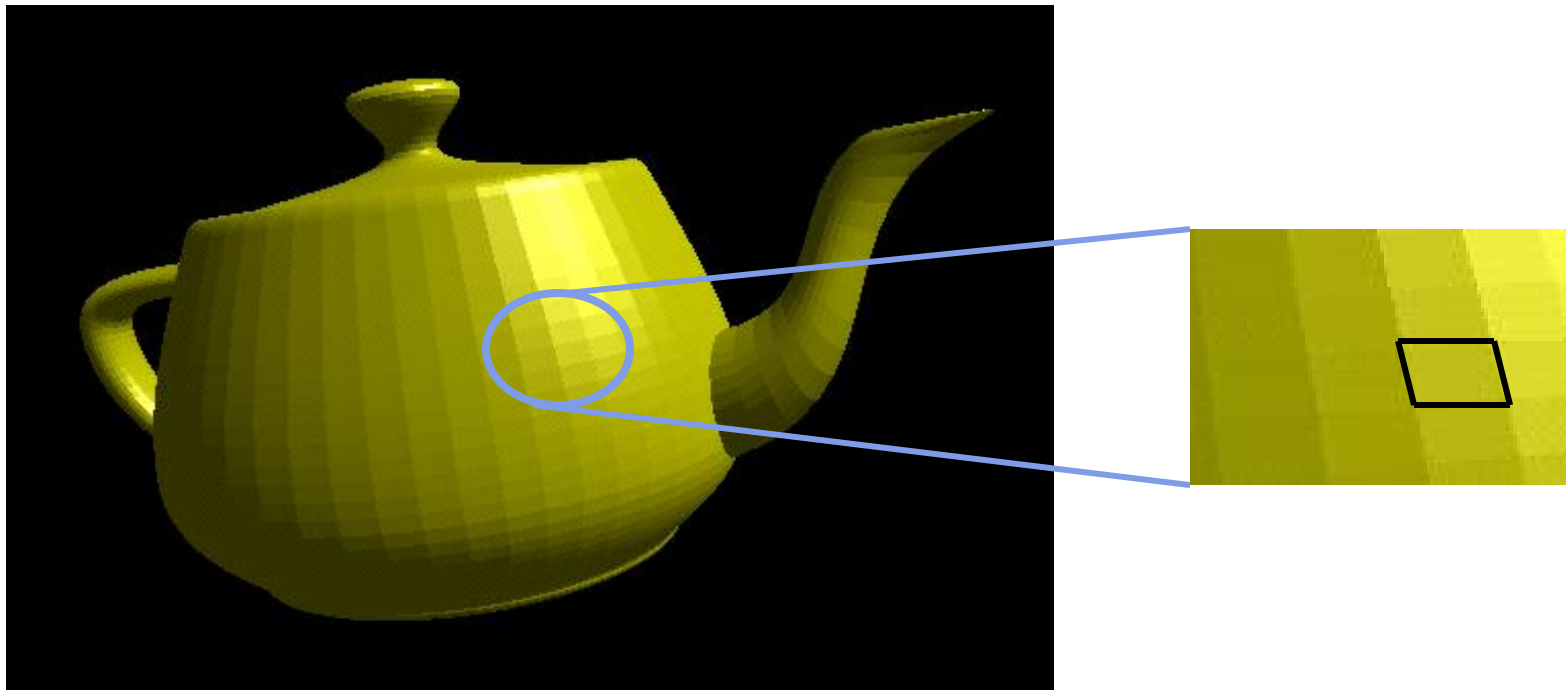
- Two types of shading
  - Assume linear change => interpolate (**Smooth shading**)
  - No interpolation (**Flat shading**)





# Flat Shading

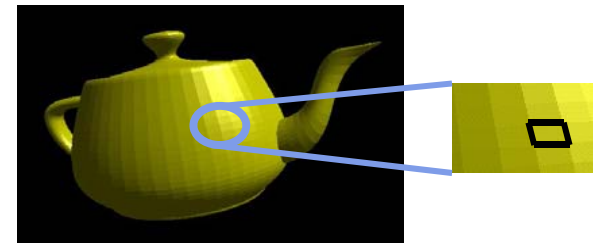
- compute lighting once for each face, assign color to whole face





# Flat shading

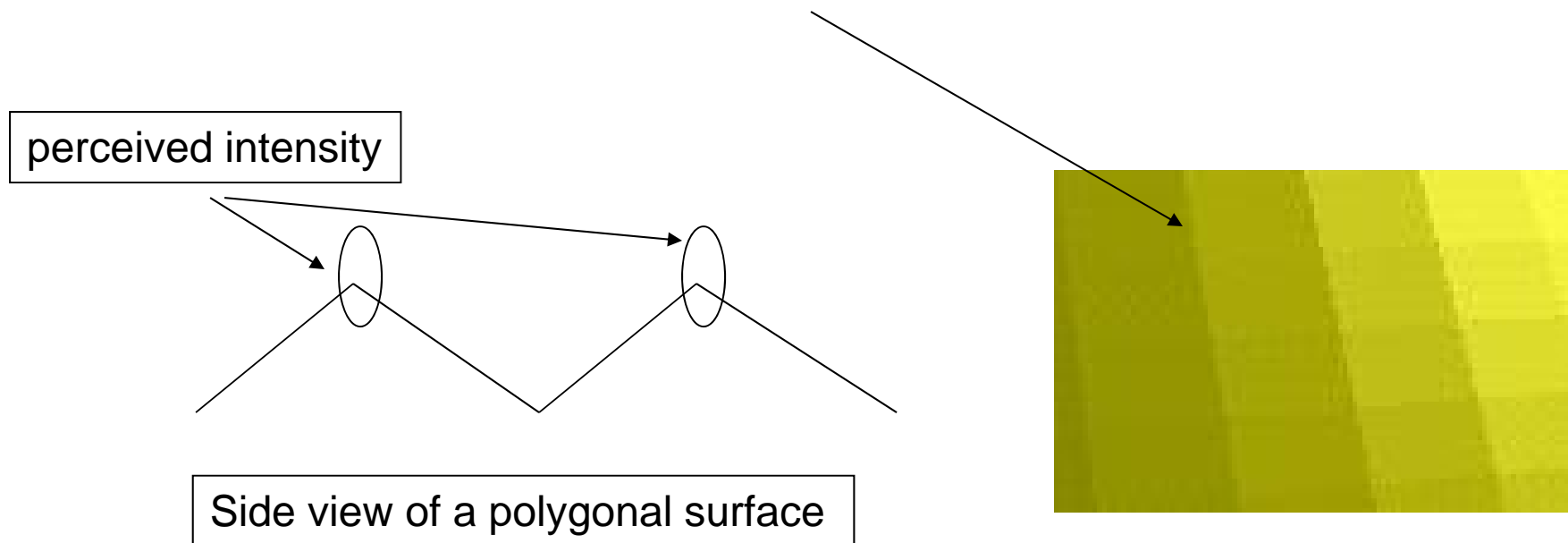
- Only use face normal for all vertices in face and material property to compute color for face
- Benefit: **Fast!**
- Used when:
  - Polygon is small enough
  - Light source is far away (why?)
  - Eye is very far away (why?)
- Previous OpenGL command: `glShadeModel(GL_FLAT)`  
**deprecated!**





# Mach Band Effect

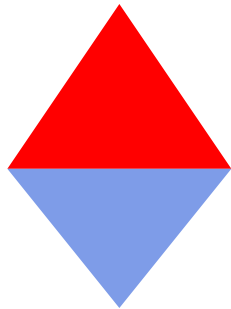
- Flat shading suffers from “mach band effect”
- Mach band effect – human eyes accentuate the discontinuity at the boundary



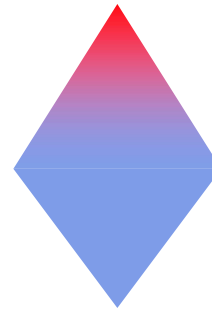
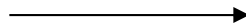


# Smooth shading

- Fix mach band effect – remove edge discontinuity
- Compute lighting for more points on each face
- 2 popular methods:
  - Gouraud shading
  - Phong shading



**Flat shading**



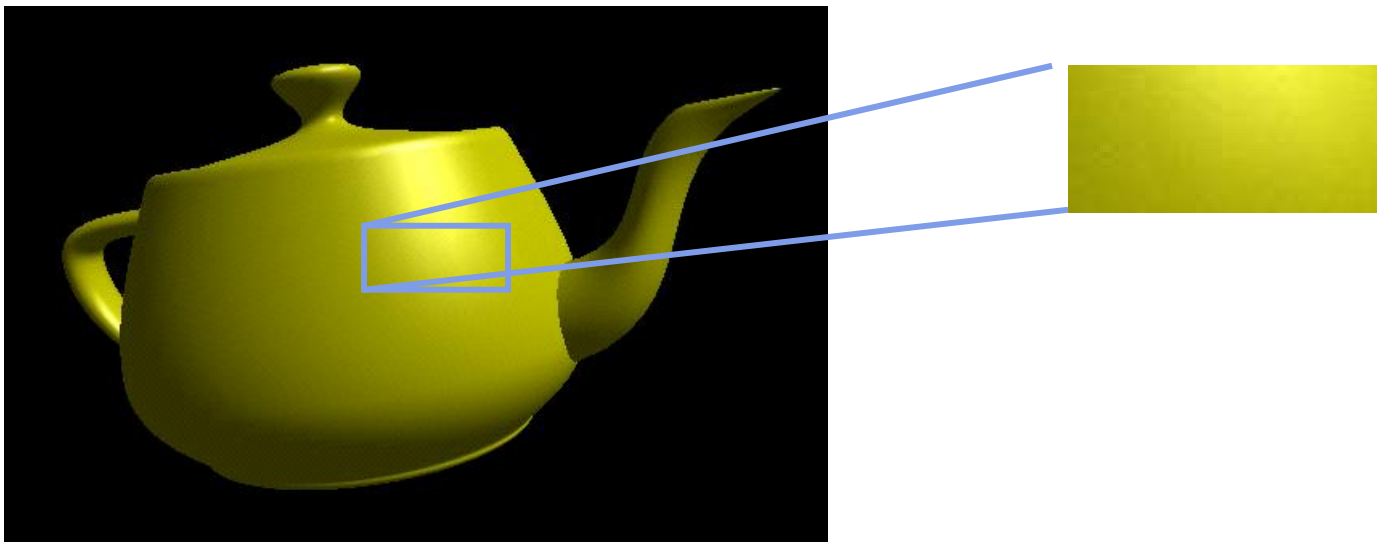
**Smooth shading**





# Gouraud Shading

- Lighting calculated for each polygon vertex
- Colors are interpolated for interior pixels
- Interpolation? Assume linear change from one vertex color to another
- Gouraud shading (interpolation) is OpenGL default





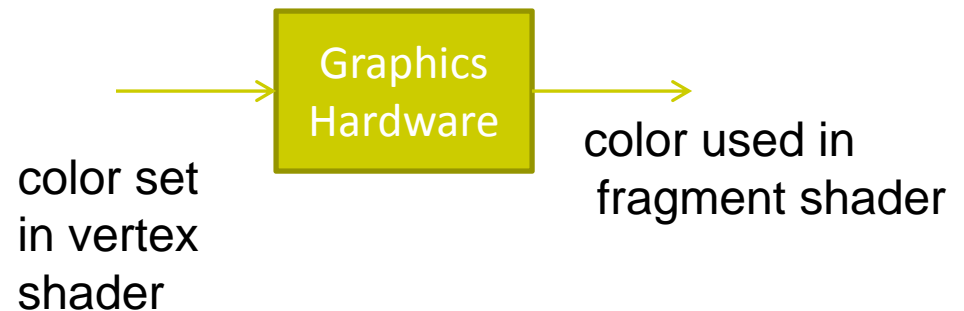
# Per-Vertex Lighting Shaders IV

```
// in vertex shader, we declared color as out, set it
```

```
.....  
color = ambient + diffuse + specular;  
color.a = 1.0;  
}
```

```
// in fragment shader (  
in vec4 color;
```

```
void main()  
{  
    gl_FragColor = color;  
}
```





# Flat Shading Implementation

- Default is **smooth shading**
- Colors set in vertex shader interpolated
- **Flat shading?** Prevent color interpolation
- In vertex shader, add keyword **flat** to output **color**

```
flat out vec4 color; //vertex shade
```

```
.....
```

```
color = ambient + diffuse + specular;
```

```
color.a = 1.0;
```



# Flat Shading Implementation

- Also, in fragment shader, add keyword **flat** to color received from vertex shader

**flat** in vec4 color;

```
void main()
{
    gl_FragColor = color;
}
```



## References

- Interactive Computer Graphics (6<sup>th</sup> edition), Angel and Shreiner
- Computer Graphics using OpenGL (3<sup>rd</sup> edition), Hill and Kelley