Virtual Memory

CS 502
Spring 99
WPI MetroWest/Southboro Campus

Virtual Memory Outline

• Background
• Demand Paging
• Performance of Demand Paging
• Page Replacement
• Page-Replacement Algorithms
• Allocation of Frames
• Thrashing
• Other Considerations
• Demand Segmentation
**Background**

- Virtual memory -- separation of user logical memory from physical memory.
  - Only part of the program needs to be in memory for execution. Explain.
  - Logical address space can therefore be much larger than physical address space.
  - Need to allow pages to be swapped in and out.
- Virtual memory can be implemented via:
  - Demand paging
  - Demand segmentation

**Demand Paging**

- Bring a page into memory only when it is needed.
  - Less I/O needed
  - Less memory needed
  - Faster response
  - More users
- Page is needed ⇒ reference to it
  - invalid reference ⇒ abort
  - not-in-memory ⇒ bring to memory
Valid–Invalid Bit

- With each page table entry a valid–invalid bit is associated (1 ⇒ in-memory, 0 ⇒ not-in-memory)
- Initially valid–invalid bit is set to 0 on all entries.
- Example of a page table snapshot.

<table>
<thead>
<tr>
<th>Valid–Invalid Bit</th>
<th>Frame</th>
</tr>
</thead>
<tbody>
<tr>
<td>1</td>
<td></td>
</tr>
<tr>
<td>0</td>
<td></td>
</tr>
<tr>
<td>1</td>
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<tr>
<td>0</td>
<td></td>
</tr>
<tr>
<td>1</td>
<td></td>
</tr>
</tbody>
</table>

- During address translation, if valid–invalid bit in page table entry is 0 ⇒ page fault.

Page Fault

- If there is ever a reference to a page, first reference will trap to OS ⇒ page fault.
- OS looks at another table to decide:
  - Invalid reference ⇒ abort.
  - Just not in memory.
- Get empty frame.
- Swap page into frame.
- Reset tables, validation bit = 1.
- Restart instruction:
  - block move
  - auto increment/decrement location
What happens if there is no free frame?

- **Page replacement** – find some page in memory, but not really in use, swap it out.
  - algorithm
  - performance – want an algorithm which will result in minimum number of page faults.
- Same page may be brought into memory several times.

Performance of Demand Paging

- Page Fault Rate $0 \leq p \leq 1.0$
- if $p = 0$, no page faults
- if $p = 1$, every reference is a fault
- Effective Access Time (EAT)

$$EAT = (1 - p) \cdot ma + p \cdot (page\_fault\_overhead + \{swap\_page\_out\} + swap\_page\_in + restart\_overhead)$$
Demand Paging Example

- Memory access time = 1 microsecond
- 50% of the time the page that is being replaced has been modified and therefore needs to be swapped out.
- Swap Page Time = 10 msec = 10,000 µsec

\[
EAT = (1 - p) \cdot 1 + p \cdot (15000)
\]

Page Replacement

- Prevent over-allocation of memory by modifying page-fault service routine to include page replacement.
- Use modify (dirty) bit to reduce overhead of page transfers – only modified pages are written to disk.
- Page replacement completes separation between logical memory and physical memory – large virtual memory can be provided on a smaller physical memory.
**Page Replacement Algorithms**

- Want lowest page-fault rate.
- Evaluate algorithm by running it on a particular string of memory references (*reference string*) and computing the number of page faults on that string.
  - Evaluation is “workload” specific
- In all our examples, the reference string is

\[1, 2, 3, 4, 1, 2, 5, 1, 2, 3, 4, 5.\]

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**First–In–First–Out (FIFO) Algorithm**

- Three Frames

<table>
<thead>
<tr>
<th>1</th>
<th>2</th>
<th>3</th>
<th>4</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td></td>
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</tbody>
</table>

<table>
<thead>
<tr>
<th>1</th>
<th>2</th>
<th>3</th>
<th>4</th>
<th>1</th>
<th>2</th>
<th>5</th>
<th>1</th>
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</tbody>
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- Four Frames

<table>
<thead>
<tr>
<th>1</th>
<th>2</th>
<th>3</th>
<th>4</th>
</tr>
</thead>
<tbody>
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</table>

- FIFO Replacement -- Belady’s Anomaly
  - more frames does not imply less page faults
**Optimal Algorithm**

- Replace page that will not be used for longest period of time.
- Four frames

<table>
<thead>
<tr>
<th>1</th>
<th>2</th>
<th>3</th>
<th>4</th>
<th>1</th>
<th>2</th>
<th>5</th>
<th>1</th>
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</tbody>
</table>

- How do you know this?
- Used for measuring how well your algorithm performs.

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**Least Recently Used (LRU) Algorithm**

- Four Frames

<table>
<thead>
<tr>
<th>1</th>
<th>2</th>
<th>3</th>
<th>4</th>
<th>1</th>
<th>2</th>
<th>5</th>
<th>1</th>
<th>2</th>
<th>3</th>
<th>4</th>
<th>5</th>
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</table>

- Counter implementation
  - Every page entry has a counter; every time page is referenced through this entry, copy the clock into the counter.
  - When a page needs to be changed, look at the counters to determine which are to change
LRU Algorithm (Cont.)

- Stack implementation – keep a stack of page numbers in a double link form:
  - Page referenced:
    - move it to the top
    - requires 6 pointers to be changed
  - No search for replacement

LRU Approximation Algorithms

- Reference bit
  - With each page associate a bit, initially = 0.
  - When page is referenced bit set to 1 (by hardware).
  - Replace the one which is 0 (if one exists). We do not know the order, however.
- Second chance
  - Need reference bit.
  - Clock replacement.
  - If page to be replaced (in clock order) has reference bit = 1, then:
    - set reference bit 0.
    - leave page in memory.
    - replace next page (in clock order), subject to same rules.
**LRU Approximation (Cont.)**

- Enhanced Second Chance – Consider the Reference Bit and the Modify Bit as an ordered pair \((r, m)\)
  - \((0, 0)\): neither recently used nor modified – best page to replace.
  - \((0, 1)\): not recently used, but modified – not quite as good, because the page will need to be written out before replacement.
  - \((1, 0)\): recently used but clean – probably will be used again soon.
  - \((1, 1)\): recently used and modified – probably will be used again soon, and write out will be needed before replacing it.

**Counting Algorithms**

- Keep a counter of the number of references that have been made to each page.
- LFU Algorithm: replaces page with smallest count.
- MFU Algorithm: based on the argument that the page with the smallest count was probably just brought in and has yet to be used.
Allocation of Frames

- Each process needs minimum number of pages.
- Example: IBM 370 -- 6 pages to handle SS MOVE instruction:
  - Instruction is 6 bytes, might span 2 pages.
  - 2 pages to handle from.
  - 2 pages to handle to.
- Two major allocation schemes:
  - fixed allocation
  - priority allocation

Fixed Allocation

- Equal allocation -- e.g., If 100 frames and 5 processes, give each 20 pages.
- Proportional allocation -- Allocate according to the size of process.
  - \( s_i \) = virtual memory size of process \( p_i \)
  - \( S = \Sigma s_i \)
  - \( m \) = total number of frames
  - \( a_i = \text{allocation for } p_i = (s_i / S) \cdot m \)
Priority Allocation

• Use a proportional allocation scheme using priorities rather than size.
• If process $P_i$ generates a page fault,
  – select for replacement one of its frames.
  – select for replacement a frame from a process with lower priority number.

Global vs. Local Allocation

• Global replacement – process selects a replacement frame from the set of all frames; one process can take a frame from another.
• Local replacement – each process selects from only its own set of allocated frames.
Thrashing

- If a process does not have “enough” pages, the page-fault rate is very high. This leads to:
  - low CPU utilization.
  - operating system thinks that it needs to increase the degree of multiprogramming.
  - another process added to the system.
- Thrashing ≡ a process is busy swapping pages in and out.

Thrashing Diagram

- Why does paging work?
- Locality model
  - Process migrates from one locality to another.
  - Localities may overlap.
  - Why does thrashing occur?
    \[ \Sigma \text{ size of locality} > \text{total memory size} \]
**Working Set Model**

- Let $\Delta \equiv$ working-set window $\equiv$ a fixed number of page references; Example: 10,000 instructions
- $WSS_i$ (working set of process $P_i$) = total number of pages referenced in the most recent $\Delta$ (varies in time)
  - If $\Delta$ too small will not encompass entire locality.
  - If $\Delta$ too large will encompass several localities.
  - If $\Delta = \infty$ will encompass entire program.
- $D = \Sigma WSS_i \equiv$ total demand frames
- If $D > m \Rightarrow$ thrashing.
- Policy: if $D > m$, then suspend one of the processes.

**Keeping Track of the Working Set**

- Approximate with interval timer + a reference bit
- Example: $\Delta = 10,000$
  - Timer interrupts after every 5000 time units.
  - Keep in memory 2 bits for each page.
  - Whenever a timer interrupts copy and sets the values of all reference bits to 0.
  - If one of the bits in memory = 1 $\Rightarrow$ page in working set.
- Why is this not completely accurate?
- Improvement = 10 bits and interrupt every 1000 time units
Page–Fault Frequency Scheme

- Establish “acceptable” page-fault rate.
  - If actual rate too low, process loses frame.
  - If actual rate too high, process gains frame.

Other Considerations

- Prepaging
- Pool of Free Frames
- Page size selection
  - fragmentation
  - table size
  - I/O overhead
  - locality
- I/O interlock and addressing
Other Considerations (Cont.)

- Program structure
  - Array A[1024,1024] of integer
  - Each row is stored in one page
  - One frame
  - Program 1
    
    ```
    for j := 1 to 1024 do
    for i := 1 to 1024 do
    A[i; j] := 0;
    ```
    - 1024 x 1024 page faults
  - Program 2
    
    ```
    for j := 1 to 1024 do
    for i := 1 to 1024 do
    A[i; j] := 0;
    ```
    - 1024 page faults

Demand Segmentation

- Used when insufficient hardware to implement demand paging.
- OS/2 allocates memory in segments, which it keeps track of through segment descriptors.
- Segment descriptor contains a valid bit to indicate whether the segment is currently in memory.
  - If segment is in main memory, access continues,
  - If not in memory, segment fault.