Crash recovery in a distributed data storage system
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April 27, 1979

ABSTRACT

An algorithm is described which guarantees reliable storage of data in a distributed system, even when different portions of the data base, stored on separate machines, are updated as part of a single transaction. The algorithm is implemented by a hierarchy of rather simple abstract machines, and it works properly regardless of crashes of the client or servers. Some care is taken to state precisely the assumptions about the physical components of the system (storage, processors and communications).

KEY WORDS AND PHRASES

data base, operating system, distributed computing, communication, reliability, fault-tolerance, transaction, atomic.
1. Introduction

We consider the problem of crash recovery in a data storage system which is constructed from a number of independent computers. The portion of the system which is running on some individual computer may crash, and then be restarted by some crash recovery procedure. This may result in the loss of some information which was present just before the crash. The loss of this information may, in turn, lead to an inconsistent state for the information permanently stored in the system.

For example, a client program may use this data storage system to store balances in an accounting system. Suppose that there are two accounts, called A and B, which contain $10 and $15 respectively. Further, suppose the client wishes to move $5 from A to B. The client might proceed as follows:

read account A (obtaining $10)
read account B (obtaining $15)
write $5 to account A
write $20 to account B

Now consider a possible effect of a crash of the system program running on the machine to which these commands are addressed. The crash could occur after one of the write commands has been carried out, but before the other has been initiated. Moreover, recovery from the crash could result in never executing the other write command. In this case, account A could be left containing $5 and account B with $15, an unintended result. The contents of the two accounts are inconsistent.

There are other ways in which this problem can arise: accounts A and B are stored on two different machines and one of these machines crashes; or, the client itself crashes after issuing one write command and before issuing the other.

In this paper we present an algorithm for maintaining the consistency of a file system in the presence of these possible errors. We begin, in section 2, by describing the kind of system to which the algorithm is intended to apply. In section 3 we introduce the concept of an atomic transaction. We argue that if a system provides atomic transactions, and the client program uses them correctly, then the stored data will remain consistent.

The remainder of the paper is devoted to describing an algorithm for obtaining atomic transactions. Any correctness argument for this (or any other) algorithm necessarily depends on a formal model of the physical components of the system. Such models are quite simple for correctly functioning devices. Since we are interested in recovering from malfunctions, however, our models must be more complex. Section 4 gives models for storage, processors and communications, and discusses the meaning of a formal model for a physical device.

Starting from this base, we build up the lattice of abstractions shown in figure 1. The second level of this lattice constructs better-behaved devices from the physical ones, by eliminating storage failures and eliminating communications entirely (section 5). The third level consists of two more powerful primitives which work properly in spite of crashes (section 6). Finally, the highest level constructs atomic transactions from these two primitives (section 7). A final section discusses some efficiency and implementation considerations. Throughout we give informal arguments for the correctness of the various algorithms.
2. System overview

Our data storage system is constructed from a number of computers; the basic service provided by such a system is reading and writing of data bytes stored in the system and identified by integer addresses. There are a number of computers which contain client programs (clients), and a number of computers which contain the system (servers); for simplicity we assume that client and server machines are disjoint. Each server has one or more attached storage devices, such as magnetic disks. Some facility is provided for transmitting messages from one machine to another. A client will issue each read or write command as a message sent directly to the server storing the addressed data, so that transfers can proceed with as much concurrency as possible. Figure 2 illustrates the situation.

We follow tradition in using a pair of integers \( \langle f, b \rangle \) to address a byte, where \( f \) identifies the file containing the byte, and \( b \) identifies the byte within the file. A file is thus a sequence of bytes addressed by integers in the range \( 1..n \), where \( n \) is the length of the file. There are two commands available for accessing files: a generalized Read command, and a generalized Write command. The generality allows information associated with a file other than its data bytes to be read and written, for example its length, or protection information associated with the file; these complications are irrelevant to our subject and will not be mentioned again. A client requests the execution of a command by sending a message containing the command to the appropriate server. When the command has been completed, the server sends a message to the client containing a response. In the case of a read command, this response will contain the requested data. For a write command, the response is simply an acknowledgement. It is necessary to provide interlocks between the concurrent accesses of different clients.

It should now be clear that our distributed data storage system is not a distributed data base system. Instead, we have isolated the fundamental facilities required by a data base system, or any other system requiring long-term storage of information; randomly addressable storage of bits, and arbitrarily large updates which are atomic in spite of crashes and concurrent accesses. We claim that this is a sound foundation for a data base system; if it proves to be unsatisfactory, the problem will be inadequate performance.
3. Consistency and transactions

For any system, we say that a given state is consistent if it satisfies some predicate called the invariant of the system. For example, an invariant for an accounting system might be that assets and liabilities sum to zero. The choice of invariant obviously depends on the application, and is beyond the scope of a data storage system. The task of the storage system is to provide facilities which, when properly used, make it possible for a client application program to maintain its invariant in spite of crashes and concurrent accesses.

A suitable form for such facilities is suggested by the following observation. Any computation which takes a system from one state to another can be put into the form

\[
\text{state} := F(\text{state})
\]

where \( F \) is a function without side effects. If we describe the state as the product of the states of a number of components, we can make finer distinctions by writing this as

\[
\text{state} := [ F(\text{Uses}_F(\text{state})) \setminus \text{Unchanged}_F(\text{state}) ]
\]

where \( \text{Uses}_F \) and \( \text{Unchanged}_F \) are projections from the state space into subspaces, such that range(\( F \)) \times range(\( \text{Unchanged}_F \)) is the entire state space. For simplicity we assume that range(\( F \)) \subset range(\( \text{Uses}_F \)).

That is, the assignment actually needs to write only those parts of the state which are actually changed by the computation. Such a computation will clearly be atomic in the presence of crashes if the assignment is atomic in the presence of crashes, i.e., if either all the writes are done, or none of them are. Two such computations \( F \) and \( G \) may run concurrently and still be atomic (i.e., serializable) if range(\( F \)) \cap range(\( \text{Uses}_G \)) = 0 and vice versa.

In pursuit of this idea, we introduce the notion of a transaction (the same concept is used in [Eswaren et. al.], and elsewhere in the database literature, to define consistency among multiple users of a common data base). A transaction is a sequence of read and write commands sent by a client to the file system. The write commands may depend on the results of previous read commands in the same transaction. The system guarantees that after recovery from a system crash, for each transaction, either all of the write commands will have been executed, or none will have been. We call this the atomic property for transactions. The client will indicate the commands of a transaction by surrounding them with Begin and End commands. If the client fails to issue the end transaction command (perhaps because he crashes) then a time-out mechanism will eventually abort the transaction without executing any of the write commands. In addition, transactions appear atomic with respect to other transactions which may be executing concurrently; that is, there exists some serial order of execution which gives the same results.

Assuming this atomic property for transactions, consider how the previous example might be implemented by a client. The client first issues a Begin command, and then continues just as in the example in section 1. After sending the two write commands, he sends End. This transaction moves \$5 from A to B. Notice that the client waits for the responses to the read commands, then computes the new balances, and finally issues write commands containing the new balances.

A client may decide to terminate a transaction before it is completed. For this purpose we have an additional command, Abort. This terminates the transaction, and no write commands issued in the transaction will take effect. Because the system also times out transactions, the Abort command is logically unnecessary, but the action it causes also occurs on a timeout and hence must be implemented in the system.

Thus, we have two groups of commands, which constitute the entire interface between the data storage system and its clients:

Data commands: Read, Write

Control commands: Begin, End, Abort

We shall return to transactions in section 7 after laying some necessary groundwork.
4. The physical system

To show the correctness of our algorithms in spite of imperfect disk storage, processor failures (crashes) and unreliable communications, we must have a formal model of these devices. Given this model, a proof can be carried out with any desired degree of formality (quite low in this paper). The validity of the model itself, however, cannot be established by proof, since a physical system does not have formal properties, and hence its relation to a formal system cannot be formally shown. The best we can do is to claim that the physical system will behave like the formal system with some probability $1 - p$, and that $p$ is small enough. The correctness of this claim can only be established by experience.

In constructing our model, we have tried to represent all the properties of the underlying physical systems, and to assign appropriate probabilities to the various events which can occur. We believe that systems constructed from current hardware can be expected to function as described by the model for years or centuries. The reader must make his own judgment about the truth of this claim.

In order to make our assumptions about possible failures more explicit, and we hope more convincing, we divide the events which occur in the model into two categories: desired and undesired; in a fault-free system only desired events will occur. Undesired events are subdivided into expected and unexpected. Our algorithms are designed to work in the presence of any bounded number of expected events and no unexpected events. The probability $p$ referred to above is therefore the probability of an unexpected event. The value of $p$ can only be estimated by an exhaustive enumeration of possible failure mechanisms. Whether a given $p$ is small enough depends on the needs of the application.

Our general theme is that, while errors may occur, all expected errors will be detected and dealt with before they cause incorrect behavior. In the remainder of this section, we present our model for the three main physical components on which our system depends: disk storage, processors and communications. In the next section, we describe how undesired events are handled; in general this is done by constructing higher-level abstractions for which desired events are the only expected ones.

4.1 Disk storage

Our model for disk storage is a set of addressable pages, where each page contains a status (good, bad) and a block of data; if the status is bad, the data is not meaningful. There are two actions by which a processor can communicate with the disk:

procedure Put(address: Address, data: Dblock)
procedure Get(address: Address) returns (status: (good, looksBad), data: Dblock)

Put does not return status, because things which go wrong when writing on the disk are usually not detected by current hardware, which lacks read-after-write capability. The extension to a model in which a Put can return bad status is trivial.

We consider two kinds of events: those which are the result of the processor actions Get and Put, and those which are spontaneous.

The results of a Get(address: $a$) are:

(desired) If page $a$ is (good, $d$), then returns (good, $d$).
(desired) If page $a$ is bad, then returns looksBad.
(expected) Soft read error: if page $a$ is good, then returns looksBad. Since we tolerate only a bounded number of undesired events, if page $a$ is (good, $d$), then repeating Get a bounded number of times will eventually result in (good, $d$).
(unexpected) Undetected error: if page $a$ is bad, then returns good, or if page $a$ is (good, $d$), then returns (good, $d'$) with $d' \neq d$. 
The effects of a Put(at: a, data: d) are:

(desired) Page a becomes (good, d).
(exected) Write error: page a is unchanged, or page a becomes bad.

The remaining undesired events, called decays, model various kinds of accidents. To describe them we need some preliminaries. Each decay event will damage some set of pages, which are contained in some larger set of pages which is characteristic of the decay. For example, a decay may damage many pages on one cylinder, but no pages on other cylinders; or many pages on one surface, but no pages on other surfaces. We call these characteristic sets decay sets. Two pages are decay related if there is some decay set which contains both. We also assume a partitioning of the disk pages into units, and a time interval $T_D$ called the unit decay time. We assume that any decay set is wholly contained in one unit, and that it is possible to partition each unit into pairs of pages which are not decay-related (in order to construct stable storage; see 5.1). $T_D$ must be very long compared to the time required to read all the disk pages.

A decay is a spontaneous event in which some set of pages, all within some one characteristic decay set, changes from good to bad. We now consider the following spontaneous events:

(expected) Infrequent decay: a decay preceded and followed by an interval $T_D$ during which there is no other decay in the same unit, and the only bad Puts on that unit are to pages in the characteristic set of the decay. Because units can be bounded in size, the stringency of the infrequency assumption does not depend on the total size of the system.

(unexpected) Frequent decay: two decays in the same unit within an interval $T_D$.

(unexpected) Undetected error: some page changes from bad to good, or from (good, d) to (good, $d'$) with $d' \neq d$.

Other events may be obtained as combinations of these events. For example, a Put changing the wrong page could be considered as one in which the addressed page is unchanged (expected) and some other page spontaneously changes to a new good value (unexpected). One consequence of this model is that writing correct data at the wrong address is an unexpected event and hence cannot be tolerated.

4.2 Processors and crashes

Our model of a processor is conventional except for the treatment of crashes. A processor consists of a collection of processes and some shared state. Each process is an automaton with some local state, and makes state transitions (executes instructions) at some finite rate. Instructions can read and write the shared state as well as the local state of the process; some standard kind of synchronization primitive, such as monitors, allows this to be done in an orderly way. For simplicity we consider the number of processes to be fixed, but since a process may enter an idle state in which it is simply waiting to be reinitialized, our model is equivalent to one with a varying but bounded number of processes. The union of the shared state and the process states is the state of the processor. A processor can also interact with the disk storage and the communications as described in sections 4.1 and 4.3.

A crash is an undesired but expected event which causes the state of the processor to be reset to some standard value; because of this effect, the processor state is called volatile state. This implies that the processor retains no memory of what was happening at the time of the crash. Of course the disk storage, or other processors which do not crash, may retain such memory. In a system with interesting long-term behavior, such as ours, a processor recovering from a crash will examine its disk storage and communicate with other processors in order to reach a state which is an acceptable approximation to its state before the crash. Since a crash is expected, it may occur at any time; hence a crash may occur during crash recovery, another crash may occur during recovery from that crash, and so forth.
Our model includes no expected events in the processor other than desired events and crashes. The assumption is that any expected undesired event will be detected (by some kind of consistency checking) and converted into a crash before it affects any other part of the system. It may well be questioned whether this assumption is realistic.

4.3 Communications

Our model for communications is a set of messages, where each message contains a status (good, bad), a block of data, and a destination which is a processor. Since we are not concerned with authentication in this paper, we assume that the source of a message, if it is needed, will be encoded in the data. There are two actions by which a processor can communicate with another one:

procedure Send (to: Processor, data: Mblock)
procedure Receive returns (status: (good, bad), data: Mblock)

The similarity to the actions for disk storage is not accidental. Because messages are not permanent objects, however, the undesired events are somewhat simpler to describe. The possible events are as follows:

The possible results of a Receive executed by processor p are:
  (desired) If a message (good, d, p) exists, returns (good, d) and destroys the message.
  (desired) If a bad message exists, returns bad and destroys the message.

There may be an arbitrary delay before a Receive returns.

The effects of a Send (to: q, data: d) are:
  (desired) Creates a message (good, d, q).

Finally, we consider the following spontaneous events:
  (expected) Lost: some message is destroyed.
  (expected) Duplication: some new message identical to an existing message is created.
  (expected) Decay: some message changes from good to bad.
  (unexpected) Undetected error: some message changes from bad to good, or from (good, d, q) to (good, d', q') with d'≠d or q'≠q.

As with disk storage, other undesired events can be obtained as combinations including these spontaneous events.
5. The stable system

The physical devices described in the previous section are an unsatisfactory basis for the construction of systems. Their behavior is uncomfortably complex; hence there are too many cases to be considered whenever an action is invoked. In this section we describe how to construct on top of these devices a more satisfactory set of virtual devices, with fewer undesired properties and more convenient interfaces. By eliminating all the undesired events, we are able to convert disk storage into an ideal device for recording state, called *stable storage*. Likewise, we are able to convert communications into an ideal device for invoking procedures on a remote processor. By "ideal" in both cases we mean that with these devices our system behaves just like a conventional error-free single-processor system, except for the complications introduced by crashes.

We have not been so successful in concealing the undesired behavior of processors. In fact, the remaining sections of the paper are devoted to an explanation of how to deal with crashes. The methods for doing this rely on some idealizations of the physical processor described in section 5.2.

5.1 *Stable storage*

The disk storage not used as volatile storage for processor state (see 5.2) is converted into *stable* storage with the same actions as disk storage, but with the property that no undesired events can occur (except unexpected ones). Since the only desired events are ideal reads and writes, stable storage is an ideal storage medium, with no failure modes which must be dealt with by its clients.

To construct stable storage, we introduce two successive abstractions, each of which eliminates two of the undesired events associated with disk storage. The first is called *careful disk storage*; its state and actions are specified exactly like those of disk storage, except that the only expected events are a bad write immediately followed by a crash, and infrequent decay. A careful page is represented by a disk page. *CarefulGet* repeatedly does *Get* until it gets a *good* status, or until it has tried *n* times, where *n* is the bound on the number of soft read errors. This eliminates soft read errors. *CarefulPut* repeatedly does *Put* followed by *Get* until the *Get* returns *good* with the data being written. This eliminates write errors which don’t change the page; it also eliminates write errors which leave a bad page, provided there is no crash during the *CarefulPut*. Since crashes are expected, however, this isn’t much use by itself.

A more complicated construction is needed for stable storage. A stable page consists simply of a block of data. In addition to *Get* and *Put*, it has a third action called *Cleanup*. It is represented by an ordered pair of careful disk pages, chosen from the same unit but not decay-related. The definition of units ensures that this is possible, and that we can use all the pages of a unit for stable pages. The value of the data is the data of the first representing page if that page is *good*, otherwise the data of the second page. The representing pages are protected by a monitor which ensures that only one action can be in progress at a time. Since the monitor lock is held in volatile storage and hence is released by a crash, some care must be taken in analyzing what happens when there is a crash during an update operation.

We maintain the following invariant on the representing pages: not more than one of them is *bad*, and if both are *good* they both have the data written by the most recent *StablePut*, except during a *StablePut* action. The second clause must be qualified a little: if a crash occurs during a *StablePut*, the data may remain different until the end of the subsequent crash recovery, but thereafter both pages’ data will be either the data from that *StablePut* or from the previous one. Given this invariant, it is clear that only the desired and the unexpected events for disk pages are possible for stable pages.

Another way of saying this is that *StablePut* is an *atomic* operation: it either changes the page to the desired new value, or it does nothing and a crash occurs. Furthermore, no decay is possible.

The actions are implemented as follows. A *StableGet* does a *CarefulGet* from one of the representing pages, and if the result is bad does a *CarefulGet* from the other one. A *StablePut* does
a *CarefulPut* to each of the representing pages in turn; the second *CarefulPut* must not be started until the first is complete. Since a crash during the first *CarefulPut* must prevent the second one from being started, we can be sure that if the second *CarefulPut* is started, there was no write error in the first one.

The third action, called *Cleanup*, works like this:

Do a *CarefulGet* from each of the two representing pages;

if both return *good* and the same data then

Do nothing

else if one returns *bad* then

{ One of the two pages has decayed, or has suffered a bad write error in a *CarefulPut* which was interrupted by a crash. }

Do a *CarefulPut* of the data block obtained from the *good* address to the *bad* address.

else if both return *good*, but different data then

{ A crash occurred between the two *CarefulPuts* of a *StablePut* }

Choose either one of the pages, and do a *CarefulPut* of its data to the other page.

This action is applied to each stable page after a crash before normal operation of the system begins, and at least every unit decay time $T_D$ thereafter.

To show that the invariant holds, we assume that it holds when stable storage is initialized, and consider all possible combinations of events. The detailed argument is a tedious case analysis, but the essence of it is simple. Both pages cannot both be bad for the following reason. Consider the first page to become bad; it either decayed, or it suffered a bad *Put* during a *StablePut*. In the former case, the other page cannot decay or suffer a bad *Put* during an interval $T_D$, and during this interval a *Cleanup* will fix the bad page. In the latter case, the bad *Put* is corrected by the *CarefulPut* it is part of, unless there is a crash, in which case the *Cleanup* done during the ensuing crash recovery will fix the bad page before another *Put* can be done. If both pages are good but different, there must have been a crash between the *CarefulPuts* of a *StablePut*, and the ensuing *Cleanup* will force either the old or the new data into both pages.

Although we make no use of it in this paper, it is interesting to observe that the method used to implement *StablePut* can actually be used for writing a large amount of data atomically (as long as it fits in half a unit). Instead of using a pair of pages to represent a stable page, we use a pair of arrays of pages, where none of the pages in one array is decay-related to any page in the other. We need to extend to these arrays the property of disk pages that a write does nothing, succeeds, or leaves the page bad; this is easily done by writing a unique identifier into each page, and checking on a *Get* that all the unique identifiers are the same. We also need to know during crash recovery which pages are in the arrays; this can be permanently fixed, or recorded in ordinary stable storage.

The stable storage construction can be extended to deal with disk storage which is less well behaved than ours. For instance, suppose that a *Put*($a$, $d$) can leave ($good$, $d'$) in $p$, with $d' \neq d$. By using three disk pages to represent a stable page, we can handle this possibility. Such increased redundancy can also take care of more frequent decays than we have assumed possible.

To simplify the exposition in the next three sections, we assume that all data is held in stable storage. The cost of protecting against all expected undesired events is significant, however, and it may not be appropriate to pay this cost for all the data recorded in the system. In particular, client data may not all have the same need for protection against decay; typically, much of it can be reconstructed from other information at some tolerable cost, or has a fairly small value to the client. Hence our system makes provision for recording client data with or without the duplication described below. The same is true for the index which the system maintains to enable rapid random access to the data in files; it is cheaper to provide the necessary redundancy by recording the file address for each page with the page itself, and reconstructing the index from this information in case it is lost. The complications associated with doing this correctly are discussed
5.2 Stable processors

A stable processor differs from a physical one in three ways. First, it can make use of a portion of the disk storage to store its volatile state; as with other aspects of a processor, long term reliability of this disk storage is not important, since any failure is converted into a crash of the processor. Thus the disk storage used in this way becomes volatile.

Second, it makes use of stable storage to obtain more useful behavior after a crash, as follows. A process can save its state; after a crash each process is restored to its most recently saved state. Save is an atomic operation. The state is saved in stable storage, using the simple one-page atomic StablePut action. As a consequence, the size of the state for a process is limited to a few hundred bytes. This restriction can easily be removed by techniques discussed later in the paper, but in fact our algorithms do not require large process states. There is also a Reset operation which resets the saved state, so that the process will return to its idle state after a crash.

Third, it makes use of stable storage to construct stable monitors [ref Hoare]. Recall that a monitor is a collection of data, together with a set of procedures for examining and updating the data which have the property that only one process at a time can be executing one of these procedures. This mutual exclusion is provided by a monitor lock which is part of the data. A stable monitor is a monitor whose data, except for the lock, is in stable storage. It has an image in global volatile storage which contains the monitor lock and perhaps copies of some of the monitor data. The monitor's procedures acquire this lock, read any data they need from stable storage, and return the proper results. A procedure which updates the data must do so with exactly one StablePut. Saving the process state is not permitted within the monitor; if it were, a process could find itself running in the monitor after a crash with the lock not set.

Since the lock is not represented in stable storage, it is automatically released whenever there is a crash. This is harmless because a process cannot resume execution within the monitor after a crash (since no saves are permitted there), and the single Put in an update procedure has either happened (in which case the situation is identical to a crash just after leaving the monitor) or has not happened (in which case it is identical to a crash just before entering the monitor).

The procedures of a stable monitor are examples of atomic actions, i.e. actions which either do or do not occur, regardless of crashes. A StablePut is also an atomic action. One of the major purposes of our successive abstractions is to make more powerful actions atomic. It is important to recognize that such actions can only be considered atomic above the level at which they are defined: only the crash recovery procedure which is part of the implementation of stable storage makes a StablePut atomic, and examining the representation of a stable page with lower-level operations such as CarefulGet might reveal partial changes.

The state of a stable processor, unlike that of a physical processor, is not entirely volatile, that is, it does not all disappear after a crash. In fact, we go further and adopt a programming style which allows us to claim that none of its shared state is volatile. We insist that the volatile state of the processor must be simply a cache for its stable state, with one exception. A part of the volatile state may differ from the stable state while a process is executing in the monitor which protects that part of the state. As a consequence, the only effect of a crash is to return all the processes to their most recently saved states; any state shared between processes is not affected by a crash. This fact greatly simplifies reasoning about crashes.

5.3 Remote procedures

It is easy to construct procedure calls from reliable messages and a supply of processes [ref Lauer and Needham], by converting each call into a call message containing the name of the procedure and its parameters, and each return into a return message containing the identity of the caller and
the result. When the messages are unreliable, a little more care is needed: a call message must be resent periodically until a return is received, and duplicate call and return messages must be suppressed. The program at the end of this section has the details. It is written in Pascal, extended with monitors and sets of records, and it calls procedures for communications, a real-time clock, unique identifiers and passing work to idle processes. For simplicity we assume that all remotely called procedures both accept and return a single value of type Value.

In order to match up calls and returns properly, it is essential to have a source of unique identifiers, so that each call message and its corresponding return can be unambiguously recognized. For this purpose stable storage is required, since the identifiers must be unique across crashes of individual processors. A generator of unique identifiers is easily constructed from a stable monitor whose data is a suitably large counter. By incrementing the stable value in large units (say 1000), using it as a base, and keeping intermediate values in a volatile monitor, it is easy to make the disk traffic negligible. Many machines have a specialized form of stable storage called a real-time clock which may also be a suitable source of unique identifiers (if it is sufficiently trustworthy). We want the unique identifiers generated by a particular processor to be increasing numbers, and prefer that successive ones differ by 1 almost all the time (see below). Note that an identifier unique to a particular processor can be made globally unique by concatenating it with the processor's name.

A message can be duplicated by the communications, and a call (with a different identifier) can be duplicated as the result of a timeout or of recovery from a crash of the caller's processor. Duplicate return messages are suppressed by keeping a list of pending calls, required anyway for recognizing valid returns. Duplicate call messages are suppressed by observing that processor p's unique identifiers, which are monotonically increasing, serve as sequence numbers for the call messages, with occasional gaps in the sequence. The receiver keeps track of the largest identifier it has seen from each processor, and ignores call messages with smaller ones. The same mechanism also ensures that when a call is duplicated (by a timeout or crash), the earlier call is executed before the later one, or not at all. This works because the call message for the later call has a larger identifier.

When a receiver crashes it of course forgets all this; hence when it hears from a processor for which it has no record, it must explicitly request that processor's current sequence number and discard all earlier messages. Methods which avoid any such connection protocol, and also make no assumptions about maximum delays in the network, do not work as far as we know.

If messages arrive out of order, this algorithm will cause messages which are not duplicates to be discarded, and performance will suffer; however, by keeping a bit for each of the last k messages which tells whether it has been received, this problem can be alleviated at the cost of k bits per pair of communicating processors. In any reasonable system a very modest value of k will suffice. To preserve the ordering of duplicated calls, the generator of unique identifiers must be advanced by at least k during crash recovery and after a timeout. Otherwise a call message m which is generated before the crash or timeout and delayed for a long time, might arrive after a later call message m has been processed. If m.id > m.id - k, m will not be rejected, since it has not been seen before.

The data structures used to implement remote procedures are all volatile (except for the generator of unique identifiers, discussed earlier). Hence when a processor crashes, it will subsequently ignore any return messages from calls outstanding at the time of the crash. Any activations of remote procedures which it happened to be running at the time of the crash will be forgotten, unless they have done Save operations. In the latter case they will complete and send a return message in the normal way, since all the information needed to do this is in the local state of the process running the remote procedure. To make remote procedures a reliable tool in the presence of crashes, some restrictions are needed on the behavior of the procedure being called remotely. These are discussed in the next section.

We assume from this point on that communication between processors is done only with the remote procedure mechanism; i.e., there will be no uses of Send and Receive except in the program below.
The following program implements remote procedures. It uses Send and Receive for messages, AssignWork and GetWork for assigning work to processes, Now for current time, and UniqueId for unique identifiers. The last is also called remotely.

```
{ Code for the one process which receives messages }
var m: Message; repeat Receive(m);
if m.state = call and OKtoAccept(m) then AssignWork(m); if m.state = return then DoReturn(m) until false;

{ Code for the processes which execute remotely called procedures }
var m: Message; repeat m := GetWork; m.val := m.action(m.val); Send(m.source, m) until false;

{ Make calls }

monitor RemoteCall = begin

```

```
{ Suppress duplicate messages. Called only from receive loop }

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5.4 Restartable and compatible actions

A program statement \( S \) (possibly compound) together with predicates \( P \) and \( Q \) is called a \textit{restartable action} if:

\[
P \{ S \} Q, \text{ i.e., if } P \text{ holds before } S \text{ is executed, } Q \text{ holds afterwards;}
\]

\[
P \text{ holds after any crash which occurs during the execution of } S.
\]

\( P \) is called the \textit{precondition} and \( Q \) the \textit{postcondition} of \( S \) [ref Hoare or something]. By a \textit{partial execution} of \( S \) we mean either a complete execution of \( S \), or an execution of part of \( S \) which is interrupted by a crash. Restartable actions are a useful tool for reasoning about crashes.

A very simple example of a restartable action is the \textit{StablePut} action, with \( P=\text{true} \) and \( Q=\text{the page has the new data} \). In fact, any atomic action with \( P=\text{true} \) is restartable. A sequence \( L \) of \textit{StablePut} actions is also a restartable action, again with \( P=\text{true} \) and \( Q=\text{all the pages have their new data} \). This is true because executing some prefix of \( L \), and then executing \( L \), has the same effect as executing \( L \). For example, if \( L \) is:

\[
A_1, A_2, A_3, A_4, A_5
\]

then doing the following sequence of actions is equivalent to doing \( L \):

\[
A_1, A_2, A_1, A_2, A_3, A_4, A_5.
\]

By induction, executing any number of different prefixes of \( L \), and then executing \( L \), still has the same effect. Thus, doing the following sequence of actions is equivalent to doing \( L \):

\[
A_1, A_2, A_3, A_1, A_2, A_3, A_4, A_1, A_1, A_2, A_3, A_4, A_5.
\]

This is an interesting observation, since we pointed out in section 3 that any computation can be cast in the form

\[
\text{state} := F(\text{state})
\]

where \( F \) is a function without side effects. General composition rules for restartable actions are beyond the scope of this paper.

Consider what happens when there are several possible actions on some shared data, and through concurrency several of these actions are pending. If the shared data is protected by a monitor as described in section 5.2, then only one of the pending actions will gain access to the data. If there were no possibility of crashes, then this would be a satisfactory situation; i.e. there will appear to be a series of atomic acts on the shared data. On the other hand, a crash may interrupt some partially completed action, and after crash recovery a different one of the pending actions may gain access.

Here is a specific example. Suppose we have some data which represents a set, with two possible actions: \textit{Erase}, which sets the set to empty by removing the elements one at a time; and \textit{IsMember}. Suppose that \textit{Erase} is designed to be interrupted by a crash, and in such a situation it will appear to have removed some but not all members (hence is restartable). Suppose that we start off with \( a \) and \( b \) in the set, one process \( P \) testing \( a \) and \( b \) for membership in the set, and another process \( Q \) calling \textit{Erase}. The following is a possible sequence of events:

\( Q \) enters the monitor, and succeeds in removing \( a \) from the set.

The system crashes and recovers.

\( P \) enters the monitor, finds that \( a \) is not a member, and exits the monitor.

\( P \) re-enters the monitor, finds that \( b \) is a member, and exits the monitor.

\( Q \) re-enters and completes the \textit{Erase}.

In this case, there does indeed appear to have been a series of atomic actions on the data: test \( b \) successfully for membership, erase the set, test \( a \) unsuccessfully for membership. Unfortunately, \( P \) performed the membership tests in the opposite order. This inconsistency would not happen with monitors and without crashes.
There are two straightforward solutions for this problem. The first is simply to design the clients of a data structure so that between them they never have more than one pending action on the data. This would lead to little concurrency, and may actually be impossible to guarantee. Thus, we would prefer to avoid this solution. A second solution is to store the monitor lock in stable storage. After a crash, we can discover which process was in the monitor and arrange that at the point of recovery that process re-enters the monitor. Monitor entry and exit would now involve disk activity, which would make monitors quite expensive.

Shared data which spans more than one machine presents additional problems. It is possible to protect this data by a monitor, if the lock is kept on some one machine, and in its stable storage. However, this now makes monitors even more inefficient than in the single machine case, since the one machine will tend to be a bottleneck.

As a way out of these difficulties, we introduce compatible actions. Compatible actions will provide fewer guarantees than those provided by monitor actions without crashes, but the guarantees will be useful and obtainable in the presence of crashes and without monitor locks in stable storage. Consider the history of some shared data. There will be periods during which one or more actions are in progress or pending (if there is a monitor lock). There will also be idle periods when no action is in progress or pending. Call the collection of actions which occur between two idle periods a jumble; it includes the actions which are repeated because of timeouts or crash recovery. Note that pairs of actions may be in the same jumble without occurring simultaneously. We now say that the actions on a shared set of data are compatible if at the end of each jumble, however executed with intervening crashes, it appears that the individual actions had been executed one at a time in some order. We do not require that this order appear the same to a calling process (consider the example above). Clearly, compatible actions must be restartable (consider the collections consisting of each action by itself). Furthermore, restartable atomic actions on a stable monitor are compatible. As a refinement, if we can restrict the behavior of clients by partitioning the set of actions so that all actions in any actual jumble come from the same partition, then we need only require compatibility among the actions in each partition.
6. Stable sets and compound actions

Based on stable storage, stable processors, and remote compatible actions, we can construct two
more complex objects, from which it is then straightforward to build atomic transactions. The base
established in the previous section has the following elements:

- stable storage, with an ideal atomic write operation (StablePut) for data blocks of a few
  hundred bytes;
- stable processes which can save their local state, which revert to that state after a crash, and
  which can execute procedures on more than one processor provided the procedures are
  compatible actions;
- stable monitors protecting data in stable storage, provided all the data is on a single
  processor, and the update operations involve only a single Put;
- no volatile data;

In this system the existence of separate processors is logically invisible. However, we want our
algorithms to have costs which depend only on the amount and distribution of the data being
accessed, and not on the total size of the system. This means that interrogating every processor in
the system must be ruled out, for example. Also, the cost of recovering from a crash of one
processor must not depend on the number of processors in the system. Rather, it should be fixed,
or at most be proportional to the number of processes affected, i.e., the processes running on the
processor which crashes. Finally, it should be possible to distribute the work of processing a
number of transactions evenly over all the processors, without requiring any single processor to be
involved in all transactions.

In order to handle arbitrarily large transactions, we need arbitrarily large stable storage objects,
instead of the fixed size pages provided by stable storage, and we need arbitrarily large atomic
actions instead of the fixed size ones provided by stable monitors. The purpose of this section is to
construct these things.

6.1 Stable sets

A stable set is a set of records, each one somewhat smaller than a stable page. The stable set itself
is named by a unique identifier, and may contain any number of records. All the operations on
stable sets are restartable, and all except Create and Erase return an error indication unless executed
between a Create and the next Erase. A stable set has the following atomic operations:

Create(t: ID) creates a stable set named by t. If such a set already exists, it does nothing.

Insert(s, t: StableSet, new: Record) inserts new into both sets; one might be nil. Insert into
n sets for any fixed n would also be possible, but is not needed for our application.

Overwrite(s, t: StableSet, old, new: Record) requires that old was inserted into s and t by a
single Insert or a previous Overwrite. It removes old from s and t and inserts new into s
and t.

IsEmpty(s: StableSet) returns true if s is empty, false otherwise.

IsMember(s: StableSet, r: Record) returns true if r is in s, false otherwise.

There are also two non-atomic operations:

Enumerate(s: StableSet, p: procedure) calls p with each element of s in turn. We will write
such operations in the form for r in s do ... for readability.

Erase(s: StableSet) which enumerates the elements of s and removes each one from s and
the other set it is in. If, s does not exist, Erase does nothing.

These operations have all the obvious properties of set operations. Since Enumerate and Erase are
not atomic, we specify them more carefully: Enumerate will produce at least all the items Inserted
before the enumeration starts, if no Erase has been done; it will not produce any items which have
not been Inserted by the time it is over.
If one of the atomic operations, say \( A \), is done while one of the non-atomic ones, say \( N \), is in progress, \( A \) may behave as though it had been done before \( N \) started, or after \( N \) completed. Each \( A \) done while \( N \) is in progress makes this choice independently; thus a process doing first \( A_1 \) and then \( A_2 \) may find that \( A_1 \) behaves as though \( N \) is complete, and \( A_2 \) behaves as though \( N \) has not started. Even if \( N \) fails to complete (because of a crash), \( A \) may behave as though \( N \) had completed; e.g., if \textit{Erase} has removed an element, \textit{IsMember} will report that it is gone, even though other elements of the set may not yet have been erased.

In spite of these complications, all the actions on a stable set are compatible. The reason for the complications is that tighter synchronization is not needed for our purposes and is tricky to provide. Sensible users of this abstraction will refrain from starting atomic operations while non-atomic ones are in progress.

We have two implementations for stable sets. The first is designed to work efficiently on a single processor, and is extremely simple. We permanently allocate a set of pages in stable storage, with known addresses, to represent stable sets; these pages are called the \textit{pool}. On each page we store an item of the following type:

```plaintext
type Item = record case tag: (empty, element) of
  empty: ();
  element: (s, t: ID, r: Record) end
```

The pages of the pool are initialized to \textit{empty}. The elements of a set \( ss \) are those values \( rr \) for which there exists a representing page in the pool, i.e., one containing an \textit{element} item \( i \) with \( i.r = rr \) and \( i.s = ss \) or \( i.t = ss \). To do \textit{Insert}(\( ss, tt, rr \)) we find an \textit{empty} page and write into it the item \( (tag = \text{element}, s = ss, t = tt, r = rr) \). To do \textit{IsEmpty}, \textit{IsMember} and \textit{Enumerate} we search for all the relevant representing pages. To do \textit{Overwrite}(\( ss, tt, oo, nn \)) we find the page representing \( (ss, tt, oo) \) and overwrite it with \( (ss, tt, nn) \). Note that \textit{Insert} and \textit{Overwrite} are atomic, as claimed above, since each involves just one \textit{Put}.

A practical implementation maintains a more efficient representation of the sets in volatile storage, and reconstructs this representation after a crash by reading all the pages in the pool. To make better use of stable storage, it also orders the pages of the pool in a ring, stores several items in each page, implements the \textit{Erase} operation by writing an \textit{erased} item rather than removing each item of the set, and recovers the space for the elements of erased sets as it cycles around the ring. The details of all this do not require any new ideas.

The utility of the pool implementation is limited by the need to read all the pages in the pool after a crash. We do not want to read all the pages of all the pools in the system when one processor crashes. Therefore a \textit{wide} stable set, which spans more than one processor, requires a different approach. We assume that the value of a record determines the processor on which it should be stored (for both sets into which it is inserted), and that the unique identifier of the set determines a processor called the \textit{root processor} of the set. The idea is to have a stable set called a \textit{leaf} on each processor, and to use another stable set, called the \textit{root} and stored on the root processor, to keep track of all the processors involved. All these sets can be implemented in pools. Each record stored in the root contains only a processor name; the records in the leaves contain the elements of the wide set. Operations involving a single record are directed to its processor, and are implemented in the obvious way. \textit{IsEmpty}, \textit{Erase} and \textit{Enumerate} are directed to the root, which uses the corresponding operation of each leaf set in turn.

The only tricky point is to ensure that elements are not added to a leaf until its processor is registered in the root set. To accomplish this, the \textit{Insert} operations check whether the leaf set is empty, and if so they first call the root set's \textit{Insert} to add the leaf processor. As a consequence, \textit{Insert} is no longer an atomic operation within the implementation, but since extra entries in the root set are not visible to the user of the wide set, it is still atomic at that level.
6.2 Compound atomic actions

We need to be able to take a complex action, requiring many atomic steps, and make the entire action atomic, i.e. ensure that it will be carried out completely once it has been started. If the action \( R \) is compatible and is invoked from a processor which never crashes, then this goal will be met, because the invoking processor will keep timing out and restarting \( R \) until it is finally completed. Thus, for example, if we assume that the client of our data storage system never crashes, then the remote compatible actions of section 5.4 are sufficient to provide atomic transactions. Since we do not want to assume that any processor never crashes, least of all the client’s, something more is needed.

In fact, what is needed is simply a simulation of a processor with a single process which never crashes, and our stable processors already provide such a thing. Consider the following procedure, to be executed by a stable process:

\[
\text{procedure } A = \begin{align*}
\text{begin} \quad & \text{Save; } R; \quad \text{Reset} \quad \text{end}
\end{align*}
\]

If \( R \) is a compatible action, then \( A \) is an atomic compatible action. This is clear from a case analysis. If it crashes before the \text{Save}, nothing has been done. If it crashes after the \text{Reset}, \( R \) has been done completely and will not be done again because the saved state has been erased. If it crashes between the \text{Save} and the \text{Reset}, it will resume after the \text{Save} and restart \( R \). The resulting execution sequence is equivalent to a single execution of \( R \), by the definition of a restartable action. If other compatible actions on the same data are going on at the same time, the result is equivalent to a single execution of \( R \) together with those other actions, by the definition of compatibility.
7. Transactions

In this section we present algorithms for the atomic transactions discussed in section 3. The central idea behind them is that a transaction is made atomic by performing it in two phases:

First, record the information necessary to do the writes in a set of intentions, without changing the data stored by the system. The last action taken in this phase is said to commit the transaction.

Second, do the writes, actually changing the stored data.

If a crash occurs after the transaction is committed but before all the changes to stored data have been done, the second phase is restarted. This restart happens as many times as necessary to make get all the changes made. Any algorithm which works in this way is called a two-phase commit [ref Gray].

To preserve the atomic property, the writing of the intentions set must itself be atomic. More precisely, consider the change from a state in which it is still possible to abort the transaction (i.e. none of the changes have been recorded in the files in such a way that they can be seen by any other transaction), to one in which aborting is no longer possible, and hence crash recovery must complete the transaction. This change is the point at which the transaction is committed. It must be atomic, and hence must be the result of a single Put action. The intentions set may be of arbitrary size, but it must be represented in such a way that its existence has no effect on the file data until this final Put has been done. In addition, care must be taken that the intentions are properly cleaned up after the transaction has been committed or aborted.

This idea is implemented using stable sets and compound atomic actions. The intentions are recorded in a stable set, and the locks needed to make concurrent transactions atomic are recorded in another stable set. The complex operation of committing the transaction (including carrying out the writes) is made into a compound atomic action. To complete the argument, we must show that the various operations are compatible.

We present algorithms for the following procedures to be called by clients: Begin, Read, Write, End, and Abort. The client is expected to call Begin on one of the servers, which we call the coordinator for the transaction. Begin returns a transaction identifier. The client then calls Read and Write any number of times on various servers, directing each call to the server holding the file pages addressed by the call. These calls may be done from separate processes within the client. When all the client's Write calls have returned, he calls either End or Abort on the coordinator.

If the client fails to wait for all his Writes to return, no harm will be done to the file servers, but their resulting behavior may not be that intended by the client. Each of the actions is designed to be atomic and restartable; thus even in the presence of server crashes, lost messages and crashed clients they are either fully performed or not performed at all. However, if the client does not repeat each Write call until it returns, he will be unable to determine which Writes actually occurred. Similarly, if he calls End before all Writes have returned, he can not be sure which of the outstanding ones will be included in the transaction.

We use the following data structures:

A transaction identifier (TI) is simply a unique identifier.

An Intention is a record containing

\( t \): a TI;
\( p \): a page address \( PA = \) record file identifier, page number in file end;
\( a \): an action \( RW = (\text{read, write}) \);
\( d \): data to be written.

Actually \( t \) and \( p \) are identifiers for the stable sets in which an Intention is recorded; we shall ignore this distinction to keep the programs shorter.

A transaction flag (TF) is a record containing

\( t \): a TI;
ph: the phase of the transaction, \( \text{Phase} = \{\text{nonexistent, running, committed, aborted}\} \).

On each of the server machines we maintain sets containing these objects, and stable monitors protecting these sets, as follows:

For each file page \( p \), at the server holding the file page,
- a stable set \( p\).locks \) (whose elements are Intentions which are interpreted as locks),
- a stable monitor protecting this set.

For each transaction \( t \), at the coordinator for the transaction,
- a root for a wide stable set \( L\).intentions \) (containing Intentions which are interpreted as data which will be written when the transaction ends). A leaf of this set will exist on each server on which a file page is written or read under this transaction.

At each server \( s \),
- a stable set \( s\).flags \) (containing transaction flags),
- a stable monitor protecting this set.

We first introduce two entry procedures on the set of transaction flags; these are not accessible to the client:

entry procedure \( \text{SetPhase}(t\!:\!TI, \text{desiredPhase}\!:\!\text{Phase}\ {\{\text{not nonexistent}\}}) = \begin{align*}
\text{case GetPhase}(t) \text{ of}
\ &\text{committed, aborted}: \{\text{do nothing}\}; \\
\ &\text{running}: \text{overwrite with} \langle t, \text{desiredPhase}\rangle; \\
\ &\text{nonexistent}: \text{if desiredPhase} = \text{running} \text{ then insert} \langle t, \text{running}\rangle \text{ in flags} \{\text{else nothing}\}
\end{align*}
endcase;

\end{align*}

entry function \( \text{GetPhase}(t\!:\!TI): \text{phase} = \begin{align*}
\text{if} \langle t, \text{phase}\rangle \in \text{flags} \text{ then return} \text{phase} \text{ else return nonexistent} \text{ end.}
\end{align*}

The SetPhase procedure is an atomic restartable action. It is designed so that the phase of a transaction will go through three steps: nonexistent, running, and then either committed or aborted. Moreover, only setting it to running can remove it from the nonexistent phase, and it will change from running to either aborted or committed exactly once.

Now we introduce the five client callable procedures. Two are entry procedures of the stable monitor for a page. Each should return an error if the page is not stored on this server, but this detail is suppressed in the code:

entry function \( \text{Read}(t\!:\!TI, p\!:\!PA): \text{Data} = \begin{align*}
\text{var noConflict}\!:\!\text{Boolean}; \text{begin}
\ &\text{repeat noConflict} := \text{true};
\ &\text{for} \ i \ \text{in} \ p\).locks \ \text{do} \text{if} \ i.t\neq t \ \text{and} \ i.a\!\Rightarrow\text{write} \ \text{then} \ noConflict := \text{false}
\ &\text{until noConflict;}
\ &\text{Insert}(p\).locks, Lintentions, \langle \text{read}, \text{nil}\rangle); \text{return StableGet}(p) \text{ end;}
\end{align*}

entry procedure \( \text{Write}(t\!:\!TI, p\!:\!PA, d\!:\!Data) = \begin{align*}
\text{var noConflict}\!:\!\text{Boolean}; \text{var} \ d'\!:\!d; \text{begin}
\ &\text{repeat noConflict} := \text{true}; \ d' := d;
\ &\text{for} \ i \ \text{in} \ p\).locks \ \text{do}
\ &\ &\text{if} \ i.t\neq t \ \text{then} \ noConflict := \text{false}
\ &\ &\text{else if} \ i.a =\text{write} \ \text{then} \ d' := i.d;
\ &\text{until noConflict;}
\ &\text{if} \ d'\neq d \ \text{then} \text{Overwrite}(p\).locks, Lintentions, \langle \text{write}, d'\rangle, \langle \text{write}, d\rangle)
\ &\text{else} \text{Insert}(p\).locks, Lintentions, \langle \text{write}, d\rangle) \text{ end;}
\end{align*}

The other three, which control the start and end of the transaction, are not monitor entry
procedures. The End and Abort procedures which complete a transaction do so by calling an internal procedure Complete.

procedure Begin(t: TI =
    const t = UniqueID(); begin SetPhase(t, running); CreateWideStableSet(t); return t end;

function End(t: TI): Phase = return Complete(t, committed)

function Abort(t: TI): Phase = return Complete(t, aborted)

function Complete(t: TI, desiredResult: Phase {committed or aborted only}): Phase = begin
    if GetPhase(t) = nonexistent then return nonexistent;
    Save {process state}; SetPhase(t, desiredResult);
    {now the transaction is committed or aborted}
    if GetPhase(t) = committed then
        for i in t.intentions do if i.a = write then StablePut(i.p, i.d);
        Erase(t.intentions) {also erases all corresponding entries in all p.locks};
    Reset {process state}; return GetPhase(t) end;

A transaction will terminate either through an End or an Abort. Both of these commands may be running simultaneously, either because of a confused client, or because Abort is being locally generated by a server at the same time as a client calls End. Moreover, the remote procedure call mechanism can result in several instances of either End or Abort in simultaneous execution. In any case, the phase will change to either aborted or committed and remain with that value; which of these occurs determines the outcome of the transaction. Thus it is phase which makes Abort and End compatible.

We make four claims:

1. If phase changes from running to committed, then all Write commands completed before End was first entered will be reflected in the file data.
2. The only changes to file data will be as a result of Write commands directed to this transaction.
3. If phase changes from running to aborted, then no Write commands will be reflected.
4. After the first End or Abort completes, the wide stable set for i will have been erased and will remain erased and empty.

Claim 4 follows from the fact that both End and Abort eventually call Erase(t). Thus the set will have been erased. The set can not be recreated because the only call on set creation is in the Begin action, and each time Begin is called it will use a new unique id. Claim 3 follows from the fact that the only writes to file data pages occur in the End procedure; these writes will not occur if the End procedure discovers that phase has been set to aborted; finally, once phase has been set to aborted, it will remain set to aborted. Claim 2 follows from the fact that only Write can add intentions with a = write to t.

Claim 1 follows from several facts. The fundamental one is that the body of End (following the Save and up to the Reset) is a restartable action. This action has two possible outcomes, depending on the value of phase after the SetPhase. If phase = committed, then the restartable action does nothing. If phase = committed, then it remains so forever, and End will embark on some useful work. This work will include StablePut(i.p, i.d) for any write intention i enumerated from set t. Any Write(t, p, c) command completed before End was called will have made such an entry in t, and the enumeration will produce it. All such entries will be produced because there will be no call on Erase(t) until at least one enumeration has completed without interruption from crashes.
8. Refinements

Many refinements to the algorithms of the last three sections can be made. A few have been pointed out already, and a number of others are collected in this section. Most of them are incorporated in a running system which embodies the ideas of this paper [ref Israel et al.]

8.1 File representation

A file can conveniently be represented by a page containing an index array of pointers to data pages, which in turn contain the bytes (or the obvious tree which generalizes this structure). With this representation, we can record and carry out intentions without having to write all the data into the intentions set, read it out, and finally write it into the file. Instead, when doing a $Write(p, d)$ we allocate a new stable page, write $d$ into it, and record the address of the new page in the intention. Then only the addresses need to be copied into the index when carrying out the intentions. This scheme allows us to handle the data only once, just as in a system without atomic transactions. It does have one drawback: if pages are updated randomly in a large file, any physical contiguity of the file pages will soon be lost. As a result, sequential access will be slower, and the space required to store the index will increase, since it will not be possible to compress its contents.

8.2 Ordering of actions

It is easy to see that the sequential for loop in $End$ can be done in parallel, since all the data on which it operates is disjoint.

A more interesting observation is that the writing of intentions into the $t$ and $p$ sets can be postponed until just before $End$ is called. In this way it is likely that all the intentions can be written in a single $StablePut$, even for a fairly large transaction. The effect of this optimization is that the client's $Write$ calls will not return until just before the $End$; a new procedure, say $GetReady$, would have to be added so that the client can inform the servers that he wants responses to his $Write$s. We can carry this idea one step further, and move the $GetReady$ call from the client to the coordinator, which does it as part of $End$ before committing the transaction. For this to work, the client must tell the coordinator what responses to $Write$s he is expecting (e.g., by giving the unique identifiers of the calls) so that the coordinator can assume responsibility for checking that the responses are in fact received. In addition, the other servers must return their $Write$ responses to the coordinator in response to his $GetReady$, rather than to the client.

A consequence of this scheme is that a crash of any server $s$ is likely to force transactions in progress involving $s$ to be aborted, since the intentions held in volatile storage at $s$ will be lost, and the client is no longer repeating his $Write$ calls until he gets the return which indicates that the intentions have been recorded in stable storage. If crashes are not too frequent this is not objectionable, since deadlocks will cause occasional transaction aborts in any case.

A more attractive consequence is that write locks will not be set until just before the $End$, thus reducing the interval during which data cannot be read by other transactions [ref Gifford]. In order to avoid undue increases in the number of transactions aborted for deadlock, it may be necessary to resort to an "intending to write" lock which delays other transactions also intending to write, without affecting readers. These intricacies are beyond the scope of this paper.

8.3 Aborts

In a practical system it is necessary to time out and automatically abort transactions which run too long (usually because the client has crashed) or which deadlock. The latter case can be detected by some explicit mechanism which examines the locks, or it can be inferred from a timeout. In any case, these automatic aborts add no logical complexity to the scheme described in section 7, which is already prepared to receive an $Abort$ from the client at any time.
When a deadlock occurs because of a conflict between read and write locks, a less drastic action than aborting the transaction holding the read lock is possible, namely to simply notify the client that it was necessary to break his read locks. He then can choose to abort the transaction, reread the data, or decide that he doesn't really care. It is necessary to require that the client explicitly approve each broken read lock before committing the transaction. The implications of this scheme are discussed in more detail elsewhere [ref Israel, Gifford].

8.4 Redundancy of the index

Since the index which maps file addresses into disk addresses is frequently written, it would be nice to avoid the two writes required by straightforwardly implementing it in stable storage. If each data page records its file address, then the index can be reconstructed from the data pages (by scanning the disk), and it will not be necessary to store it redundantly. Some care must be taken, however, with the interaction between this idea and the idea of recording intentions as changes to the index.

The difficulty is that with this latter scheme, a Write for an uncommitted transaction has already constructed a final version of the new data page, indistinguishable from the old version from the point of view of a disk scan which is trying to rebuild a lost index. We cannot solve this problem by modifying the new data page after committing the transaction, since such a modification requires precisely the disk write we are trying to avoid. Instead, we must use the intentions to sort things out when the scan finds two contenders \( p_1 \) and \( p_2 \) for the role of page \( p \). If we make the rule that the old page is erased before the intention for the new page is erased, and we can tell that \( p_2 \) was written after \( p_1 \), then we can distinguish the following cases:

- No intention is recorded: there must have been a crash between writing \( p_2 \) and the intention. Erase \( p_2 \) and put \( p_1 \) in the index.
- There is an intention "\( p_1 := p_2 \)"; put \( p_1 \) in the index; if the intention is committed, it will eventually be carried out and will replace \( p_1 \) with \( p_2 \).

The necessary ordering of the pages can be obtained by writing a sequence number \( sn \) into the header, or in a variety of other ways. Two bits of sequence number are sufficient if interpreted as an integer mod 4, which is incremented by 1 for each new page; \( p_2 \) follows \( p_1 \) iff \( p_2 - sn \cdot p_1 - sn = 1 \mod 4 \), and vice versa; exactly one of these conditions must hold. This form of sequence number has the drawback that it is necessary to know \( p_1, sn \) before writing \( p_2 \). Using UniqueID instead requires more bits in the header but does not have this drawback.

8.5 Convenience features

It is straightforward to make Read and Write work on arbitrary sequences of bytes rather than on pages, and to do their locking to the nearest byte. Some care must be taken with the data structures for the locks, however, since it is not practical to make a lock record for each byte, and hence locks must now be recorded on ranges of bytes.

It is also easy to modify Read so that a transaction can read back the data it has written, rather than seeing the old data as in the program of section 7. Of course, other transactions will still have to wait, or see the old data as discussed in section 8.2.
Conclusions

We have defined a facility (transactions) which clients can use to perform complex updates to distributed data in a manner which maintains consistency in the presence of system crashes and concurrency. Our algorithm for implementing transactions requires only a small amount of communication among servers. This communication is proportional to the number of servers involved in a transaction, rather than the size of the update. We have described the algorithm through a series of abstractions, together with informal correctness arguments.

References


Figure 1. The lattice of abstractions
Figure 2. The System Structure