



# WPI

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## CS 543: Computer Graphics

# Shading II

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(with lots of help from Prof. Emmanuel Agu :-)

## Recall: Setting Light Properties

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- Define colors and position a light

```
var light_ambient[] = { 0.0, 0.0, 0.0, 1.0 };  
var light_diffuse[] = { 1.0, 1.0, 1.0, 1.0 };  
var light_specular[] = { 1.0, 1.0, 1.0, 1.0 };  
var light_position[] = { 0.0, 0.0, 1.0, 1.0 };
```

← Colors  
← Position

## Recall: Setting Material Properties

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- Define ambient/diffuse/specular reflection and shininess

```
Var mat_amb_diff[] = { 1.0, 0.5, 0.8, 1.0 };  
Var mat_specular[] = { 1.0, 1.0, 1.0, 1.0 };  
Var shininess[] = { 5.0 };
```

← Range: dull 0 – very shiny 128

Refl. coeff.

Pass values to shader...see book code

# Recall: Calculating Color at Vertices

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- Illumination from a light

**Illum = ambient + diffuse + specular**

$$= K_a \times I + K_d \times I \times \cos(\theta) + K_s \times I \times \cos^f(\phi)$$

- If there are N lights

**Total illumination for a point P =  $\Sigma$  (Illum)**

- Sometimes lights or surfaces are colored
- Treat R, G, and B components separately
  - *i.e.*, can specify different RGB values for either light or material

$$\mathbf{Illum}_r = K_{ar} \times I_r + K_{dr} \times I_r \times \cos(\theta) + K_{sr} \times I_r \times \cos^f(\phi)$$

$$\mathbf{Illum}_g = K_{ag} \times I_g + K_{dg} \times I_g \times \cos(\theta) + K_{sg} \times I_g \times \cos^f(\phi)$$

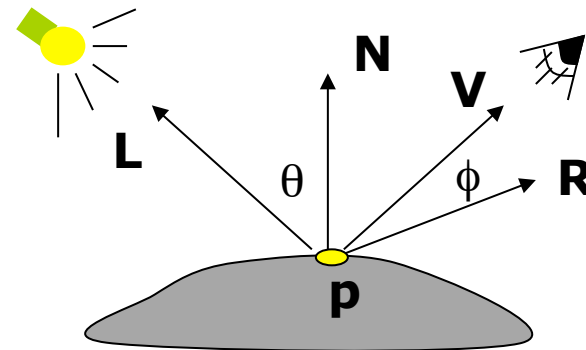
$$\mathbf{Illum}_b = K_{ab} \times I_b + K_{db} \times I_b \times \cos(\theta) + K_{sb} \times I_b \times \cos^f(\phi)$$

# Recall: Calculating Color at Vertices (cont.)

**Illum = ambient + diffuse + specular**

$$= K_a \times I + K_d \times I \times \cos(\theta) + K_s \times I \times \cos^f(\phi)$$

- **$\cos(\theta)$**  and  **$\cos^f(\phi)$**  are calculated as dot products of *Light vector*  $L$ , *Normal*  $N$ , and *Mirror-direction vector*  $R$



- To give

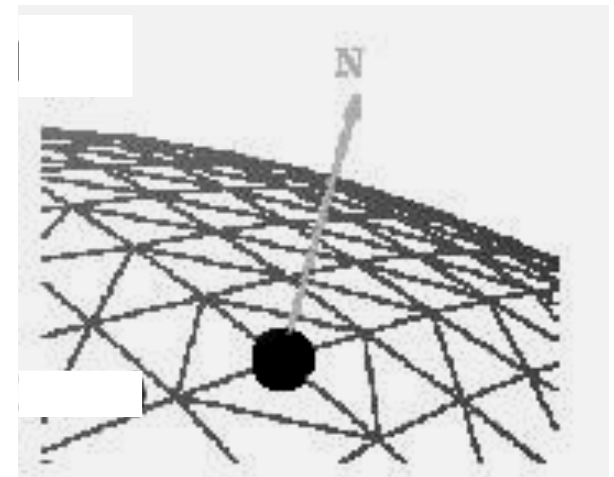
$$\mathbf{Illum} = K_a \times I + K_d \times I \times (N \cdot L) + K_s \times I \times (R \cdot V)$$

# Importance of Surface Normals

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- ❑ Correct normals are essential for correct lighting
- ❑ Associate a normal with each vertex

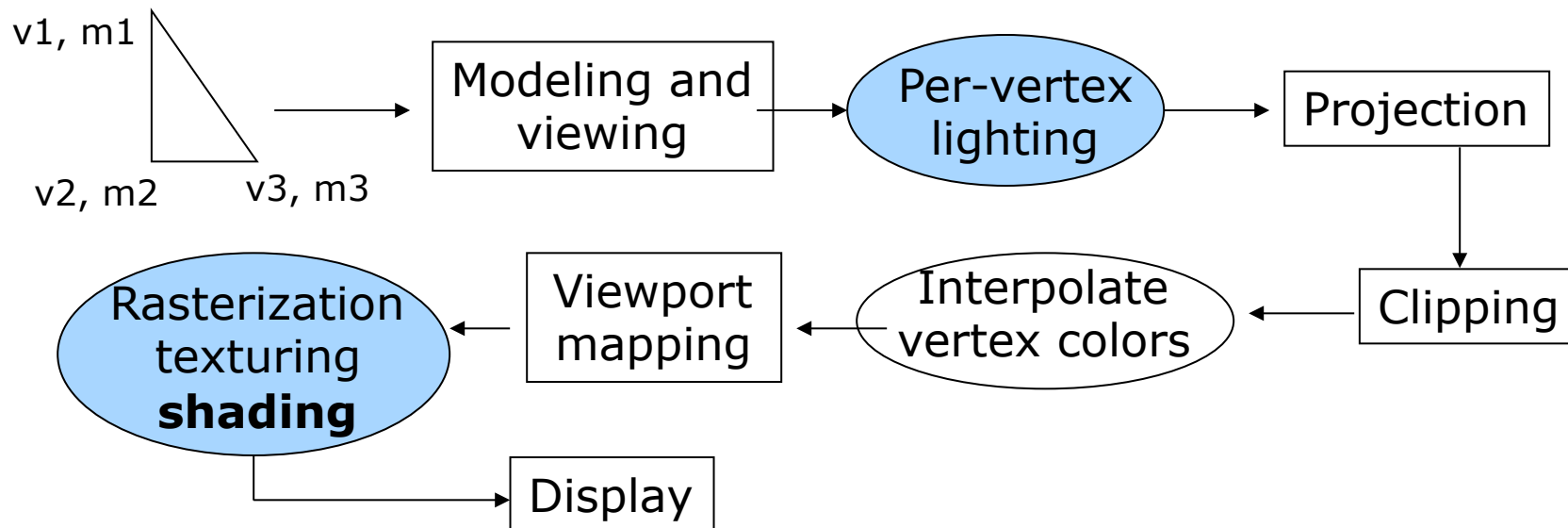
```
normalsArray.push( u, v, n );  
pointsArray.push( x, y, z );  
...
```



- ❑ All normals must be specified in unit length
  - Do in shader:  **$\text{vec4 } NN = \text{vec4}(vNormal, 0);$**

## Lighting Revisited

- Light calculation so far is at vertices
- Pixel may not fall right on vertex
- **Shading**
  - Calculates color of interior pixels
- Where are **lighting** & **shading** performed in the pipeline?

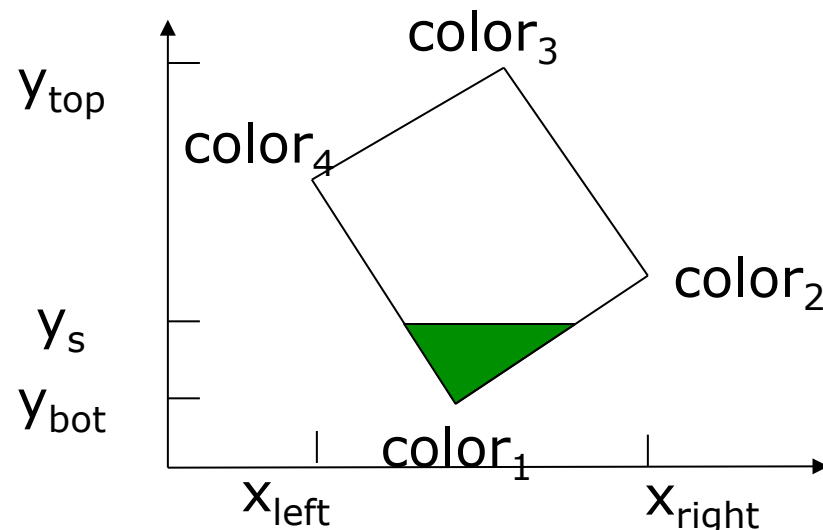


# Example Shading Function

```

for( int y = y_bot; y <= y_top; y++ ) {
  find x_left and x_right
  for( int x = x_left; x < x_right; x++ ) {
    find the color c for this pixel
    put c into the pixel at (x, y)
  }
}

```



- Scans pixels, row by row, calculating color for each pixel

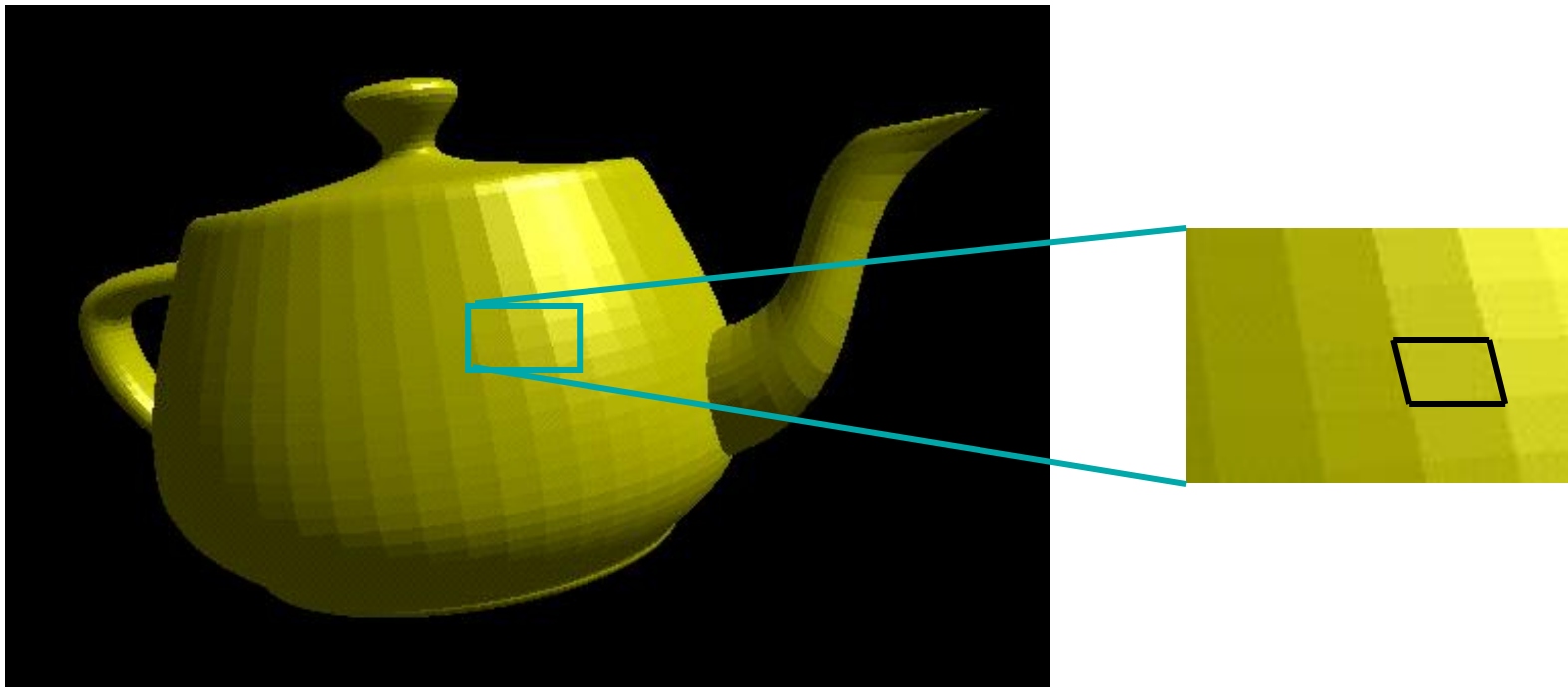


# Polygon Shading Models

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## □ Flat shading

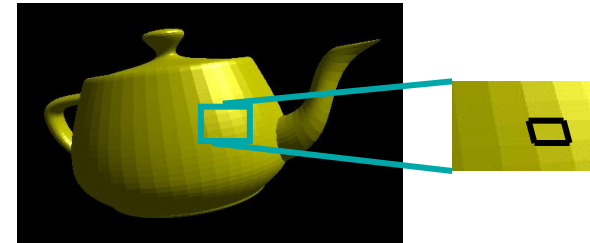
- Compute lighting once and assign the color to the whole polygon (or mesh)



# Flat Shading

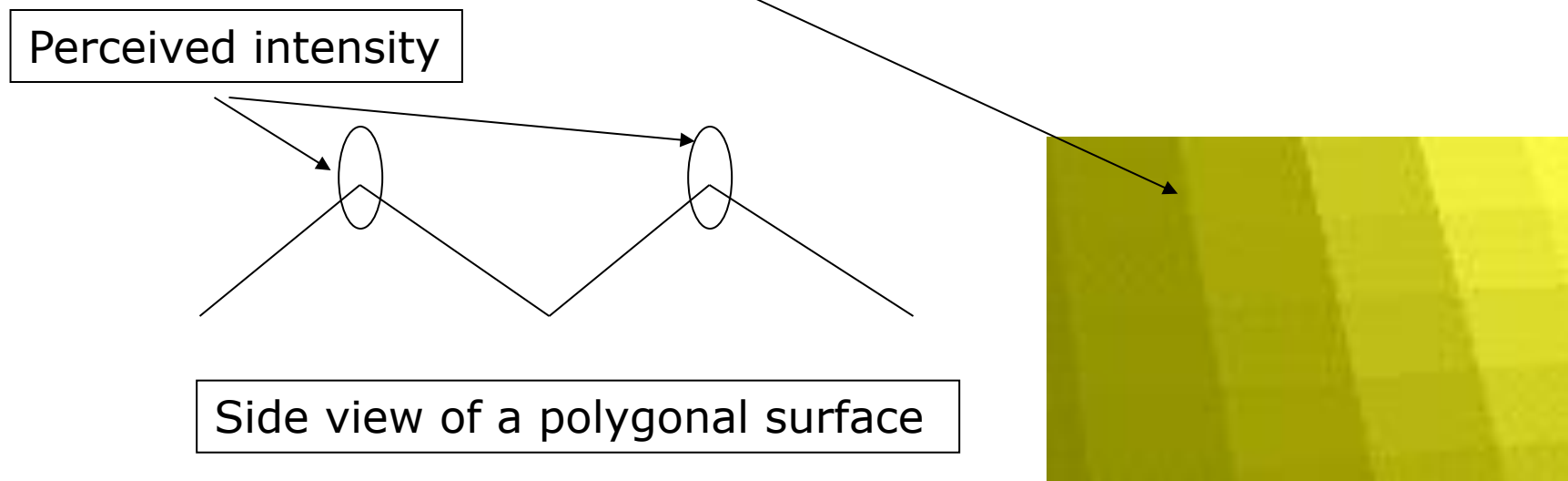
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- Only use one vertex normal and material property to compute the color for the polygon
- Benefit: fast to compute
- Used when
  - Polygon is small enough
  - Light source is far away (why?)
  - Eye is very far away (why?)



# Mach-Band Effect

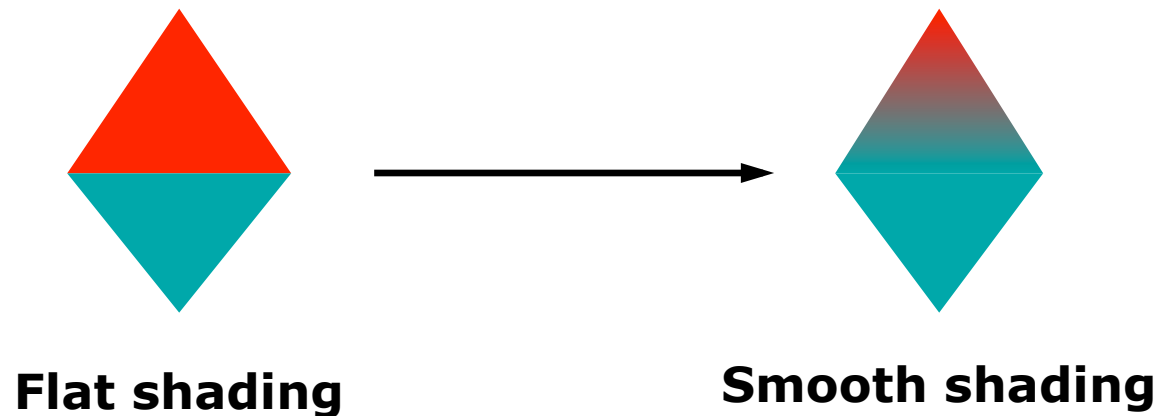
- Flat shading suffers from "mach banding"
  - Human eyes accentuate discontinuities at boundaries



# Smooth Shading

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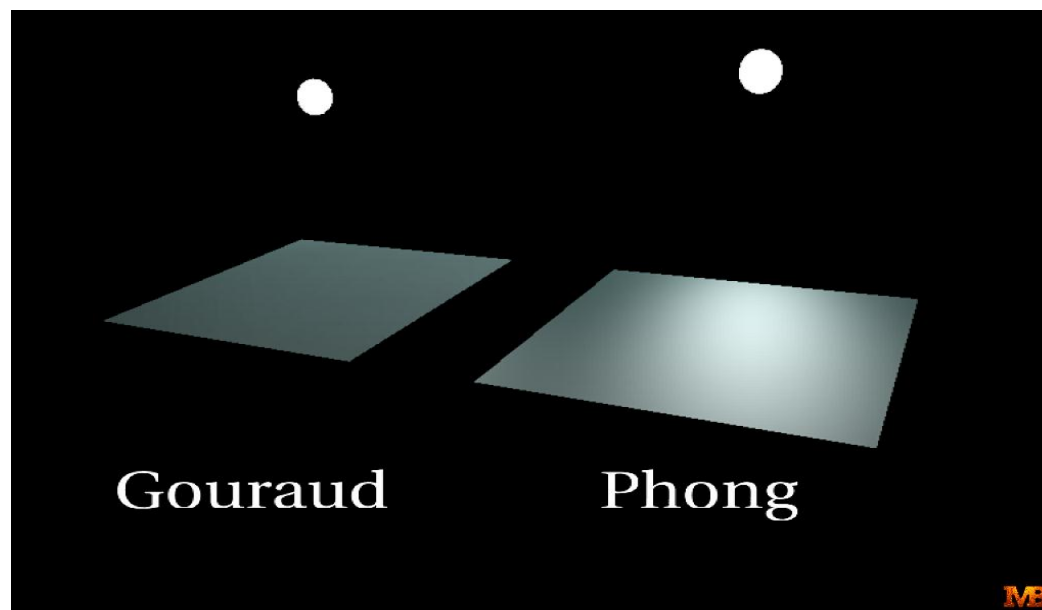
- Fix the mach banding
  - Remove edge discontinuities
- Compute lighting for more points on each face



## Smooth Shading (cont.)

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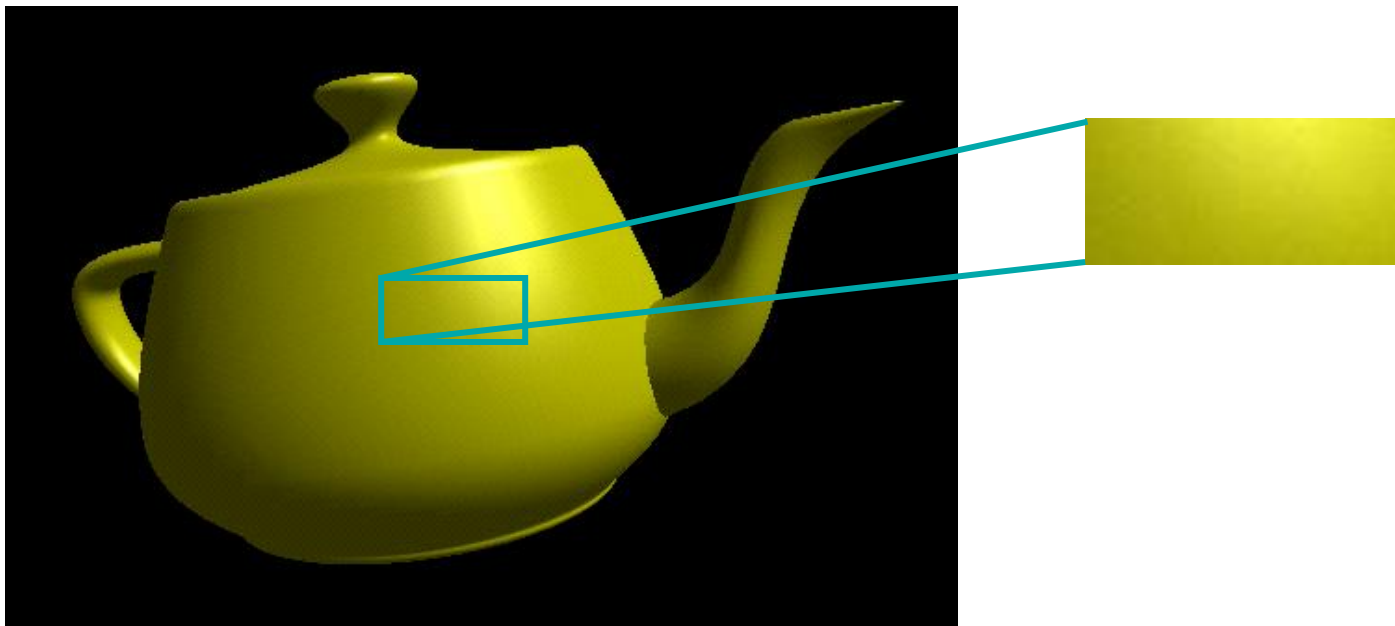
- Two popular methods
  - Gouraud shading (used by OpenGL)
  - Phong shading (better specular highlight, not in OpenGL)



# Gouraud Shading

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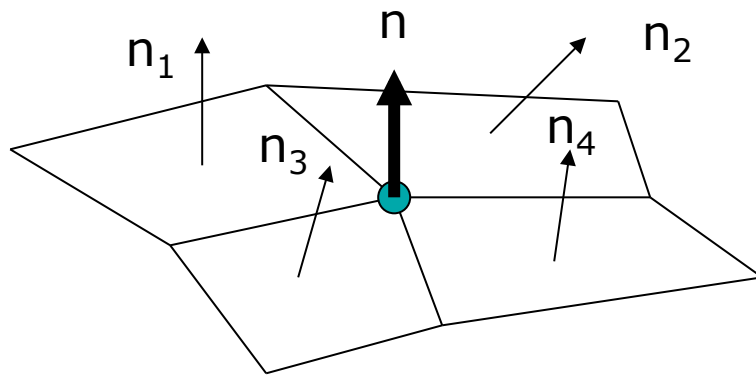
- Lighting is calculated for each of the polygon vertices
- Colors are interpolated for interior pixels



## Gouraud Shading (cont.)

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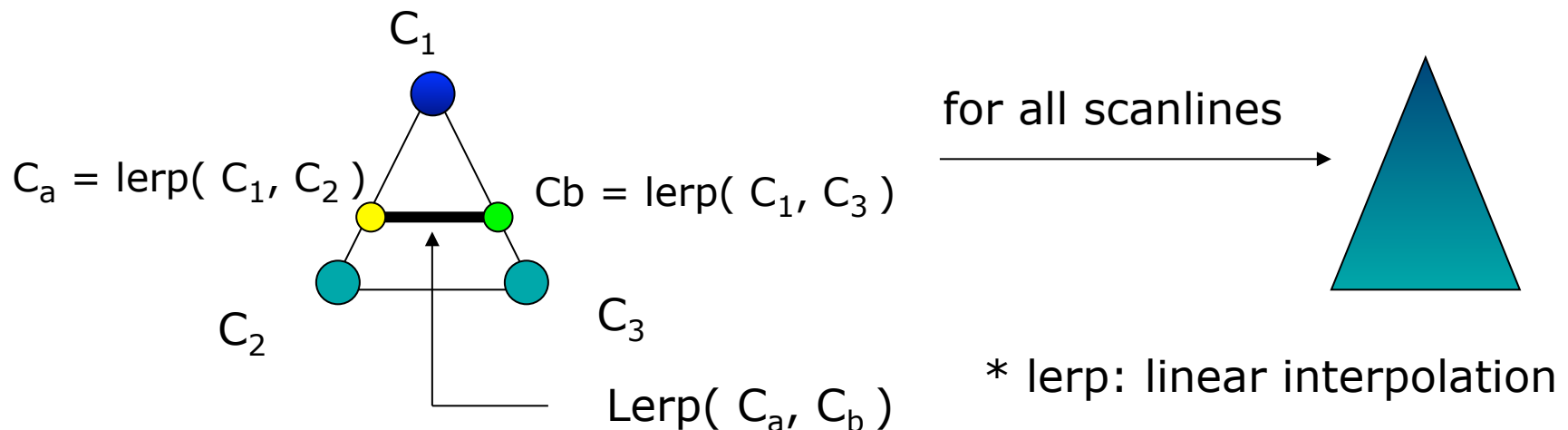
- Per-vertex lighting calculation
- Normal is needed for each vertex
- Per-vertex normal can be computed by averaging the adjacent face normals



$$n = (n_1 + n_2 + n_3 + n_4) / 4.0$$

## Gouraud Shading (cont.)

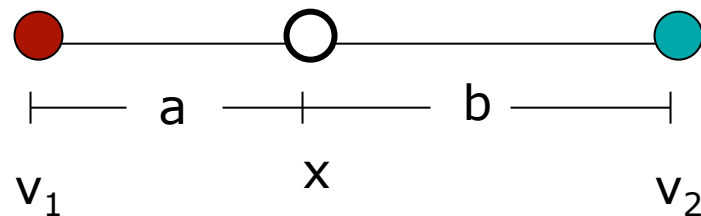
- Compute vertex illumination (color) before the projection transformation
- Shade interior pixels: color interpolation (normals are not needed for interior)





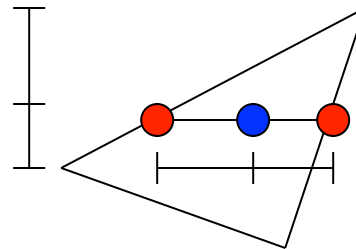
# Gouraud Shading (cont.)

## □ Linear interpolation



$$x = b / (a+b) * v_1 + a / (a+b) * v_2$$

- Interpolate triangle color: use y distance to interpolate the two end points in the scanline, and use x distance to interpolate interior pixel colors



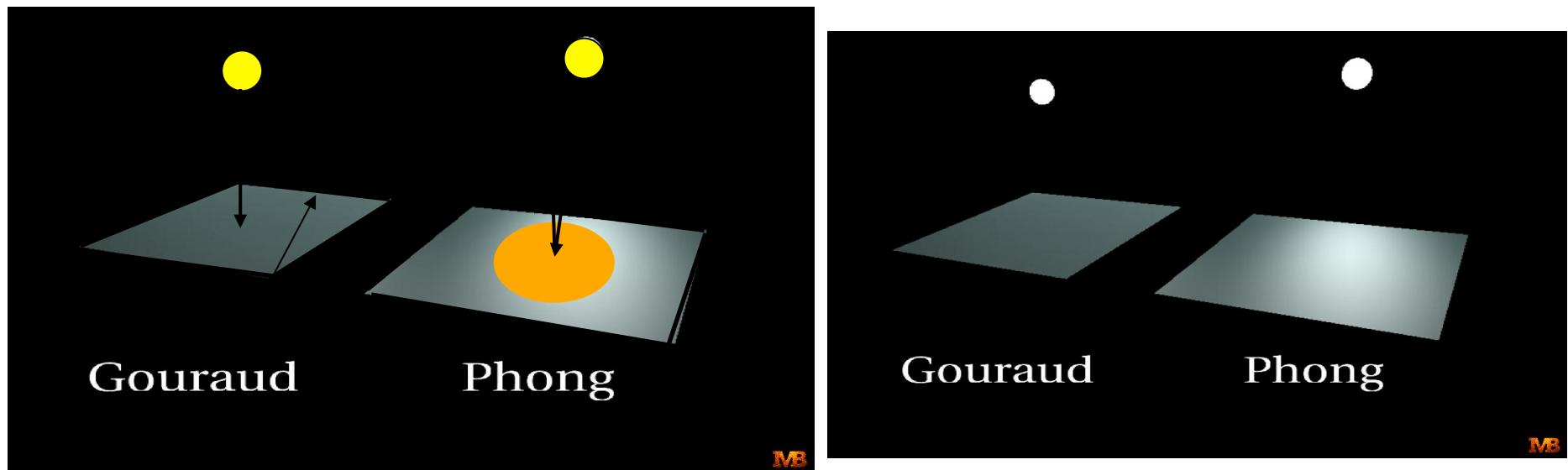
# Gouraud Shading Function

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```
// for each scan line
for( int y = y_bot; y <= y_top; y++ ) {
    find x_left and x_right
    find color_left and color_right
    color_inc = (color_right - color_left) /
                (x_right - x_left)
    for( int x = x_left, c = color_left;
         x < x_right; x++, c += color_inc ) {
        put c into the pixel at (x, y)
    }
}
```

# Gouraud Shading Problem

- Lighting in the polygon interior can be inaccurate



## Phong Shading

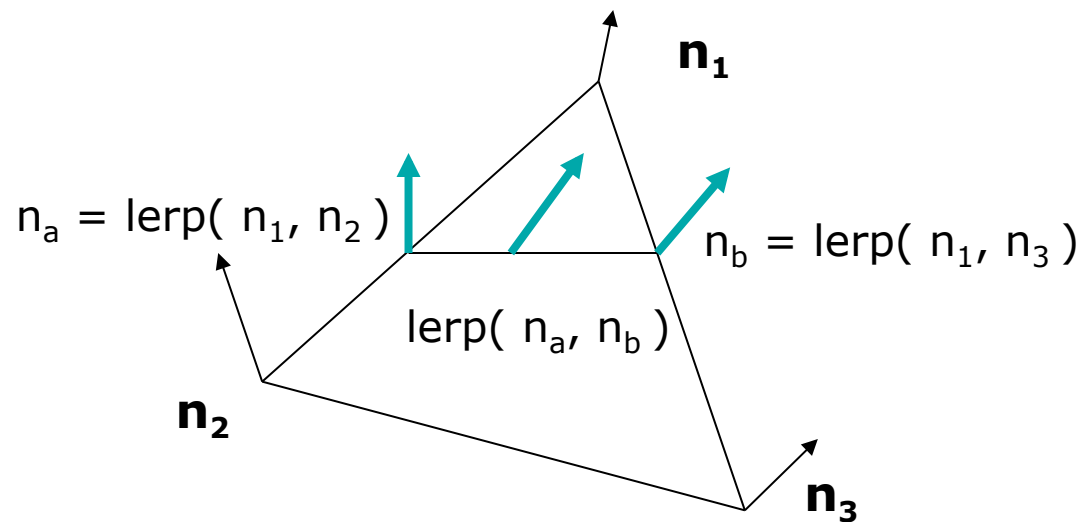
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- Instead of interpolation, we calculate lighting for each pixel inside the polygon (per-pixel lighting)
- Need normals for all the pixels
  - Not provided by user!
- Phong shading algorithm
  - Interpolate the normals across polygon
  - Compute lighting during rasterization
    - Need to map the normal back to world or eye space though

# Phong Shading (cont.)

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## □ Normal interpolation



## □ Slow

- Not supported by OpenGL, but now graphics cards have pixel shaders that can be used to do this quickly